

# Experiment 20 - The Geiger-Müller Detector

```
In[1]:= << CurveFit`
CurveFit for Mathematica v7.x thru v11.x, Version 1.96, 4/4/2018
Caltech Sophomore Physics Labs, Pasadena, CA

In[*]:= (* We export the data from the lab notebook for analysis in CurveFit. *)
SetDirectory[NotebookDirectory[]];
v0vp = {{ "S V0(V)", "Vp(V)", { 800, {2.96, 2.94, 2.98}},
  {790, {2.48, 2.42, 2.46}}, {780, {1.88, 1.88, 1.82}}, {770, {1.34, 1.38, 1.38}},
  {760, {0.92, 0.912, 0.928}}, {750, {0.480, 0.484, 0.480}},
  {740, {0.119, 0.120, 0.122}}, {738, {0.0736, 0.0704, 0.0712}},
  {800, {3.02, 2.96, 3.00}}, {825, {3.92, 3.96, 3.92}}, {850, {4.76, 4.72, 4.72}},
  {875, {5.68, 5.52, 5.68}}, {900, {6.64, 6.52, 6.64}}, {812, {3.46, 3.46, 3.40}},
  {837, {4.28, 4.24, 4.32}}, {862, {5.08, 5.16, 5.16}}, {887, {6.08, 6.08, 5.96}}};

(* Match first element of list to every element
of corresponding sublist to split data into tuples. *)
match[list_] := If[StringTake[ToString[list[[1]]], 1] == "S", {list},
  Table[{list[[1]], list[[2]][[i]]}, {i, 1, Length[list[[2]]}]];
v0vpDat = Flatten[Table[match[v0vp[[i]]], {i, 1, Length[v0vp]}], 1];
td = {{ "S V0(V)", "td(us)", {780, 83},
  {800, 80}, {820, 78}, {840, 74}, {880, 70}, {920, 66}, {950, 68}}};

Export["v0vp.dat", v0vpDat];
Export["td.dat", td];
```

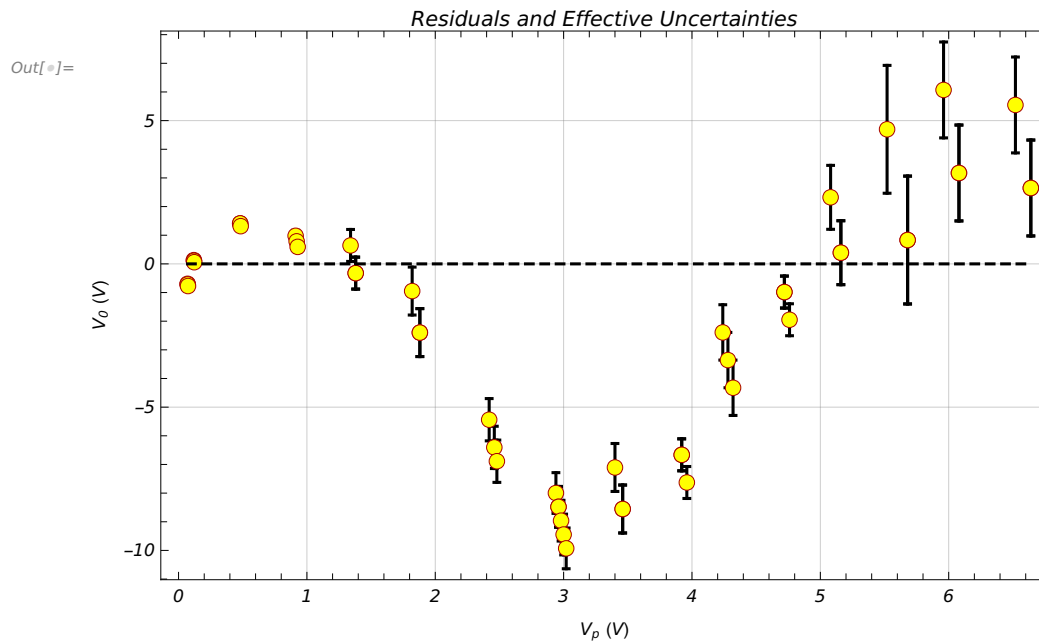
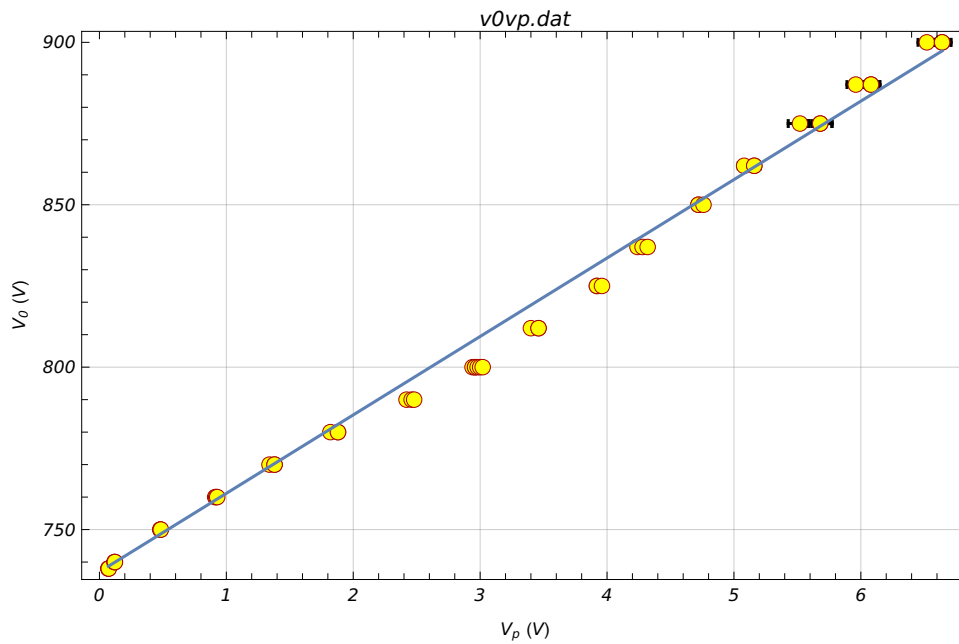
---

## Determining $V_{Th}$

The threshold voltage  $V_{Th}$  is the smallest bias voltage for which Townsend cascades occur, i.e. the smallest  $V_0$  for which pulses are detected. Therefore, our determination of  $V_0$  will be carried out by performing a (linear) fit of  $V_0$  against  $V_p$  and observing the y-intercept of the fit, essentially extrapolating to the point where the pulses just vanish.

```
In[*]:= With[ {name = SystemDialogInput["FileOpen",  
      {DataFileName, {"data files" -> {"*.dat", "*.mca"}, "all files" -> {"*"}}}]},  
      If[ name != $Canceled,  
        LoadFile[name]]  
    ]  
  
In[*]:= CalculateYsigmas[]  
  
In[*]:= SwitchXXandYY[]  
  
In[*]:= LinearFit[]
```

```
In[ ]:= LinearDifferencePlot[FrameLabel -> {"Vp (V)", "V0 (V)"}]
```



```
y(x) = a + b x
a= 736.996      b= 24.15
σa= 0.0157803  σb= 0.0336788  χ2/(n-2)= 100.683
```

We observe a relatively bad linear fit indicated by the large  $\tilde{\chi}^2$  and the clear trend in the residuals. As we calculated in the pre-lab, this indicates that some of our data points were taken with a  $V_0$  for which the thin-sheath approximation does not hold, and therefore neither does our derived linear relation between  $V_p$  and  $V_0$ .

We have estimated the upper threshold for linear behavior to be around 800V, and this is indeed around where we observe a change in behavior. Therefore we remove the data points taken with  $V_0 > 800\text{ V}$  and perform a linear fit again. We also remove the data points we used for the point-estimate of  $V_{Th}$ , as those were taken at very low signal-to-noise ratios and are prone to error. The small  $V_0$  measurements do however show some loss of linearity in  $V_p$  against  $V_0$ , possibly just due to measurement error for the reason mentioned, but this may also be due to a defect in our model at low bias voltages.

```
In[ ]:= With[ {name = SystemDialogInput["FileOpen",
      {DataFileName, {"data files" -> {"*.dat", "*.mca"}, "all files" -> {"*"}}}}],
  If[ name != $Canceled,
    LoadFile[name]]
]

In[ ]:= With[{x = SetXRange[ LinearDataPlot[], Log -> False,
  Label -> "Set the X values for the range you wish to keep." ]},
  Print[x];

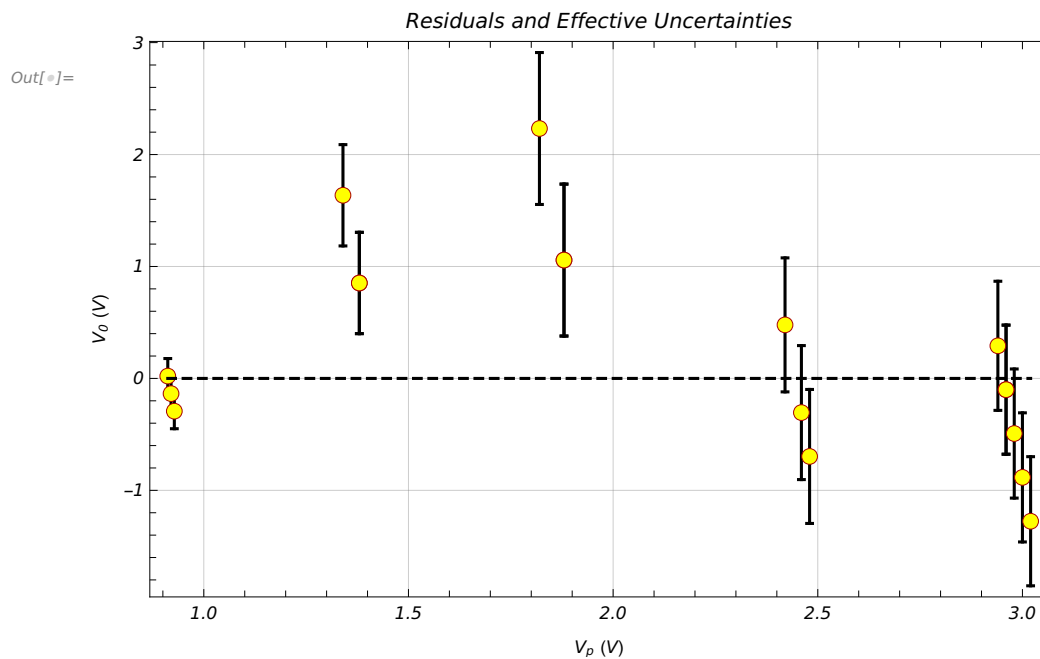
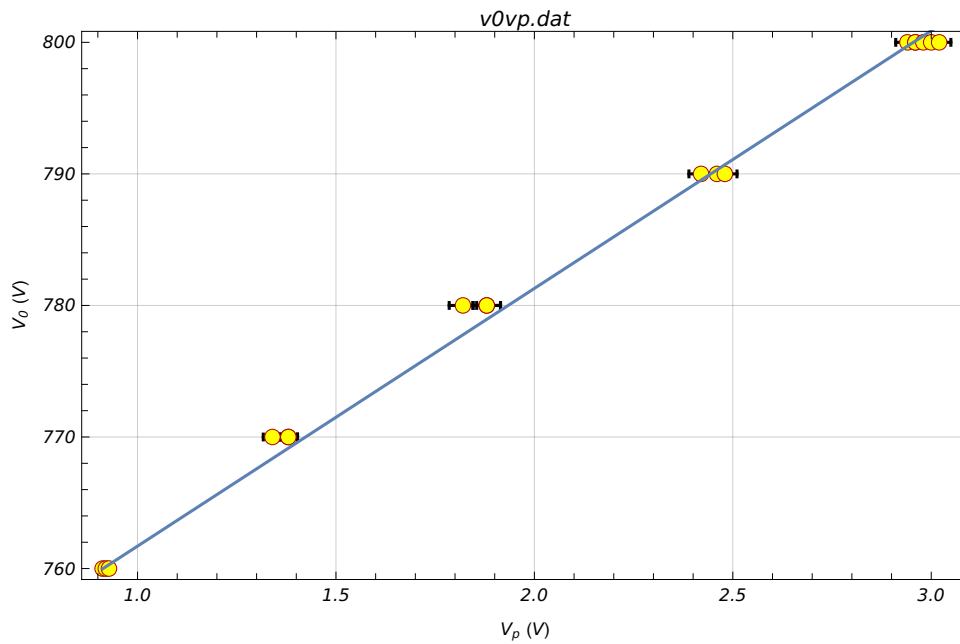
  XRangeKeep[Sequence@@x]
]

In[ ]:= CalculateYsigmas[]

In[ ]:= SwitchXXandYY[]

In[ ]:= LinearFit[]
```

```
In[ ]:= LinearDifferencePlot[FrameLabel -> {"Vp (V)", "V0 (V)"}]
```



```

y(x) = a + b x
a=      b=
742.113 19.5905
σa=      σb=      χ2 / (n-2) =
0.161309 0.111408 3.16602

```

As expected, we observe a much better fit as indicated by the relatively low  $\tilde{\chi}^2$ . The residuals do appear to show a (much less discernible) trend, again possibly showing that a linear model is not quite adequate, but they are mostly within error and therefore should be perfectly fine to use for the following analysis.

From the y-intercept of our linear plot, we can estimate  $V_{Th} = 742.1 \pm 0.2 \text{ V}$ . We observe that this is relatively close to our in-lab point estimate of 738 V.

## Determining RC time constant in CI mode, $\tau$

The long-term exponential decay of the Charge Integrated pulse is used to determine the RC time constant,  $\tau$ , of the circuit in RC mode. We will then use  $\tau$  to calculate C, the total capacitance of the circuit.

```
In[ ]:= With[ {name = SystemDialogInput["FileOpen", {DataFileName,
    {"Tek waveform files" -> {"*.csv", "*.tsv"}, "all files" -> {"*"} } }],
    If[ name != $Canceled,
        LoadTekFile[name]]
    ]

In[ ]:= With[{x = SetXRange[ LinearDataPlot[], Log -> False,
    Label -> "Set the X values for the range you wish to keep." ]},
    Print[x];

    XRangeKeep[Sequence @@ x]
    ]

In[ ]:= DecayingExponentialLLFit::usage
Out[ ]:= DecayingExponentialLLFit[ ] fits data with:
y = a eb x + c + d (x - xmin)
Important: b must be negative (i.e. decaying exponential).

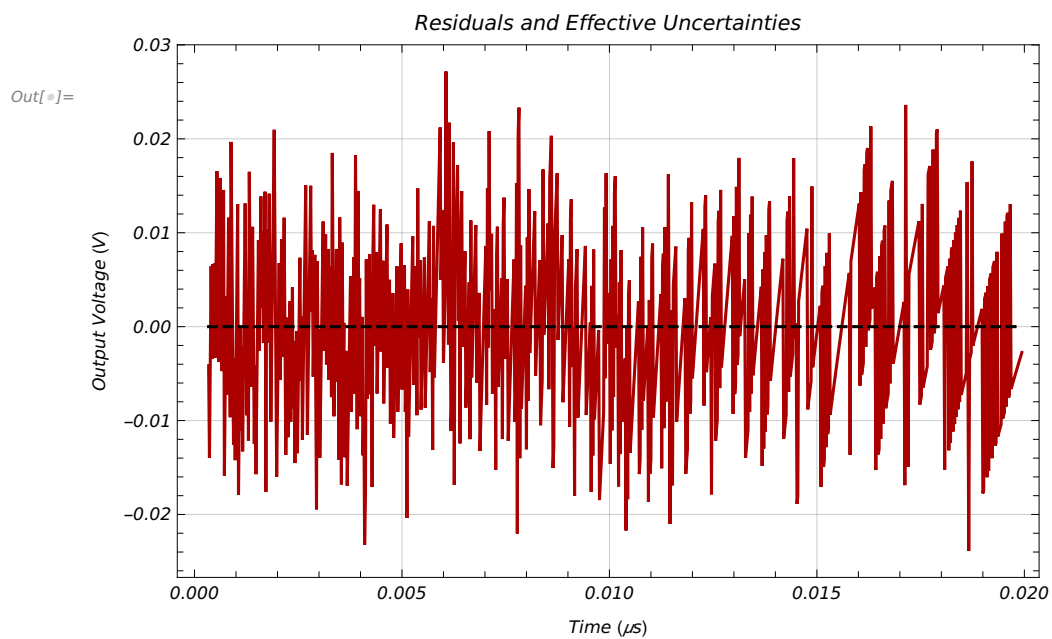
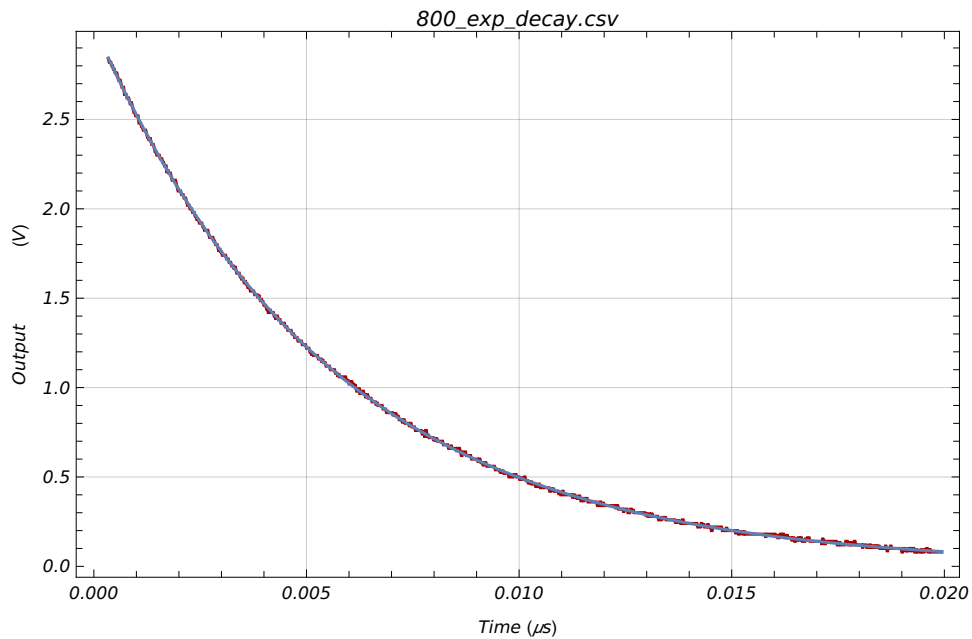
Set the value of the variable: region1
to the x-location where the linear background becomes dominant before
calling this function. It must be true that: xmin < region1 < xmax.

DecayingExponentialLLFit[r1] sets region1 = r1 and then does the fit.

In[ ]:= With[{x =
    SetX[ LogDataPlot[], Log -> False, Label -> "Set the X value for region1." ]},
    Print[x];

    DecayingExponentialLLFit[x]
    ]
```

```
In[ ]:= LinearDifferencePlot[FrameLabel -> {"Time (μs)", "Output Voltage (V)"}]
```



$$y(x) = a \exp[b x] + c + d (x - x_{\min})$$

|                 |              |              |              |              |
|-----------------|--------------|--------------|--------------|--------------|
| a=              | b=           | c=           | d=           | $x_{\min}$ = |
| 3.0368          | -179.662     | -0.0126833   | 0.560741     | 0.00034      |
| $\sigma_a$ =    | $\sigma_b$ = | $\sigma_c$ = | $\sigma_d$ = |              |
| 0.00814618      | 0.656363     | 0.00894566   | 0.425192     |              |
| Std. deviation= |              |              |              |              |
| 0.00887417      |              |              |              |              |

```
In[70]:=  $\tau = \frac{-1}{b} \left\{ 1, \frac{-\text{Abs}[\text{sigb}]}{b} \right\} (* s *)$ ;
ScientificForm[\tau, 3]
```

```
Out[71]//ScientificForm=
{5.57 × 10-3, 2.03 × 10-5}
```

```
In[72]:=  $\text{cap} = \frac{\tau}{(5 * 10^6)} (* F *)$ ;
ScientificForm[cap, 4]
```

```
Out[73]//ScientificForm=
{1.113 × 10-9, 4.067 × 10-12}
```

We obtain a reasonable fit as far as we can tell by the amplitude and distribution of the residuals (we have a single decay curve and therefore cannot perform a goodness-of-fit test). This gives us an estimate of  $\tau = 5.56 \pm 0.02$  ms, from which we calculate  $C = \frac{\tau}{R} = 1.113 \pm 0.004$  nF. Note that we have an underestimate on the uncertainty, as we do not know the tolerance of the 5M $\Omega$  resistance.

## Extracting relevant data from oscilloscope traces

### Helper functions to process data

```
In[*]:= (* We write a function to commit fit parameters to a list for each dataset. *)
```

```
(* Initialize list *)
fitParam = {};
```

```
(* We will create a list with the structure
```

```
{V0, {{a, b, siga, sigb # below Ve}, {a, b, siga, sigb # above Ve}}}.
```

```
IMPORTANT: Need to start inputting values with parameters below Ve,
then above Ve. The reg argument can be either 'l' for below Ve,
or 'm' for above Ve. *)
```

```
addValues[v0_, reg_] := Module[
  {index},
  If[
    ToString[reg] == "l",
    fitParam = Join[fitParam, {{v0, {{a, b, siga, sigb}, {}}}},
  ],
  If[
    ToString[reg] == "m",
    (index = Position[fitParam[[All, 1]], v0][[1]][[1]]);
    fitParam[[index]][[2]][[2]] = {a, b, siga, sigb}
  ]
]
```



```

];

(* We also create a list for the  $V_p$  data. In order to find  $V_p$ ,
we smooth the dataset to get rid of high-
frequency electrical noise by performing a moving average,
then select the maximum value. *)

(* Initialize list *)
vpVal = {};

(* We create a list with structure { $V_0, V_p$ } *)
vpValues[filename_, v0_] := Module[
  {data, dataAvg, maxIndex, max},
  (
    LoadTekFile[filename];
    Pause[3];
    SaveFile[StringReplace[filename, "csv" → "dat"]];
    Pause[3];
    data = Import[StringReplace[filename, "csv" → "dat"]];
    dataAvg = MovingAverage[data[[All, 2]], 20];
    Export[StringReplace["avg_%",
      "%" → StringReplace[filename, "csv" → "dat"]], dataAvg];
    maxIndex = Ordering[dataAvg, -1][[1]];
    max = dataAvg[[maxIndex]];
    vpVal = Join[vpVal, {{v0, max}}];
  )
];

```

## Processing data for analysis

```

In[ ]:= (* We use our functions to store the data we pull from the fits
of long and short timescale data for different bias voltages. *)

(* We start with the  $V_e$  data,
looping through the following commands for every dataset. *)

In[ ]:= With[ {name = SystemDialogInput["FileOpen", {DataFileName,
  {"Tek waveform files" -> {"*.csv", "*.tsv"}, "all files" -> {"*"}}}]},
  If[ name != $Canceled,
    LoadTekFile[name]]
]

```

```

In[ ]:= With[{x = SetXRange[LinearDataPlot[], Log -> False,
    Label -> "Set the X values for the range you wish to keep." ]},
    Print[x];

    XRangeKeep[Sequence@@x]
]

In[ ]:= LinearFit[]

In[ ]:= addValues[780, m]

In[ ]:= fitParam

Out[ ]:= {{760, {{0.14211, 87988.4, 0.000164461, 196.71},
    {0.197137, 61789.1, 0.00289608, 1169.96}}},
    {770, {{0.148238, 131204., 0.000222133, 362.729},
    {0.263943, 87402.8, 0.00241459, 959.95}}},
    {780, {{0.122872, 200817., 0.00040219, 532.662},
    {0.253494, 138604., 0.00536139, 2236.4}}}}

In[ ]:= SetDirectory["Geiger Muller"]

In[ ]:= (* For safekeeping *)
Export["fitParam.dat", fitParam];

(* Now for the Vp data *)

In[ ]:= files = {{760, "760_long.csv"}, {770, "770_long.csv"}, {780, "780_long.csv"}};
vpValues[#[[2]], #[[1]]] & /@ files

In[ ]:= vpVal

Out[ ]:= {{760, 0.9252}, {770, 1.3836}, {780, 1.902}}

In[ ]:= (* For safekeeping *)
Export["vpVal.dat", vpVal];

```

## Extracting $V_e$ , $V_p$ and $\frac{dV_{out}}{dt}$ data from processed traces

```

In[ ]:= (* We create a list with structure {V0,Ve,σVe} by calulating Ve from our
fit data and propagating uncertainties. We Flatten fitParam to make the
uncertainty propagation more readable by avoiding messy indexing. *)
veInt = Partition[Flatten[fitParam], 9];
veVal = Module[
  {ve, a1, b1, siga1, sigb1, a2, b2, siga2, sigb2},
  (
    a1 = 2; b1 = 3; siga1 = 4; sigb1 = 5; a2 = 6; b2 = 7; siga2 = 8; sigb2 = 9;
    Table[
      {
        veInt[[i]][[1]],
        ve = (veInt[[i]][[a1]] * veInt[[i]][[b2]] - veInt[[i]][[a2]] * veInt[[i]][[b1]]) /
          (veInt[[i]][[b2]] - veInt[[i]][[b1]]),
        ve * Sqrt[
          Sqrt[
            (veInt[[i]][[a1]] * veInt[[i]][[b2]]
              (Sqrt[
                (veInt[[i]][[siga1]]^2 + (veInt[[i]][[sigb2]]^2))
              ])^2 +
            (veInt[[i]][[a2]] * veInt[[i]][[b1]]
              (Sqrt[
                (veInt[[i]][[siga2]]^2 + (veInt[[i]][[sigb1]]^2))
              ])^2) /
            (veInt[[i]][[a1]] *
              veInt[[i]][[b2]] - veInt[[i]][[a2]] * veInt[[i]][[b1]])
            )^2 +
          (Sqrt[
            (veInt[[i]][[sigb2]]^2 + (veInt[[i]][[sigb1]]^2))
          ])^2
        ],
      },
      {i, 1, Length[veInt]}
    ]
  ]
]

Out[ ]:= {{760, 0.326914, 0.0132689}, {770, 0.494825, 0.00996239}, {780, 0.544507, 0.0200946}}

```

```

In[*]:= (* We create a list with structure {V0,dVout/dt,σdVout/dt}. *)
dvOut = Module[
  {b2, sigb2},
  (
    b2 = 7; sigb2 = 9;
    Table[
      {veInt[[i]][[1]], veInt[[i]][[b2]], veInt[[i]][[sigb2]]},
      {i, 1, Length[veInt]}
    ]
  )
]

Out[*]= {{760, 61789.1, 1169.96}, {770, 87402.8, 959.95}, {780, 138604., 2236.4}}

(* We already have a list with structure {V0,Vp}. We only have one sweep
for each bias voltage and we did not obtain the peak value using a fit,
therefore we do not have accurate, independent estimates for the uncertainty
in Vp. To attempt a better error propagation in the following analysis,
we simply observe the standard deviation of the fit for the exponential
decay trace to be ~0.0089 V and use this as a somewhat arbitrary
estimate of the uncertainty in our values for Vp. As mentioned *)

In[*]:= vpValUnc = Table[Flatten[{vpVal[[i]], 0.0089}], {i, 1, Length[vpVal]}]
Out[*]= {{760, 0.9252, 0.0089}, {770, 1.3836, 0.0089}, {780, 1.902, 0.0089}}

```

## Determining $r_{s0}$

We calculate  $r_{s0}$  from our data and propagate uncertainties using  $r_{s0} = a(b/a)^{V_e/V_p}$ .

```

In[*]:= (* We define a function to calculate rs0
for each V0 from the processed datasets above. *)
rs0[veUnc_, vpUnc_] :=
Module[
  {aDim, bDim, rs0List},
  (
    aDim = 0.3135 * 10-3 (* m *); bDim = 7.62 * 10-3 (* m *);
    rs0List = aDim (bDim/aDim)veUnc[[2]]/vpUnc[[2]]
      {1, Log[bDim/aDim]  $\frac{\text{veUnc}[[2]]}{\text{vpUnc}[[2]]}$  Sqrt[ $\left(\frac{\text{veUnc}[[3]]}{\text{veUnc}[[2]]}\right)^2 + \left(\frac{\text{vpUnc}[[3]]}{\text{vpUnc}[[2]]}\right)^2$ ]}];
    {vpUnc[[1]], rs0List[[1]], rs0List[[2]]}
  )
]

```

```
In[ ]:= rs0Val = Table[rs0[veVal[[i]], vpValUnc[[i]]], {i, 1, Length[vpVal]}]
```

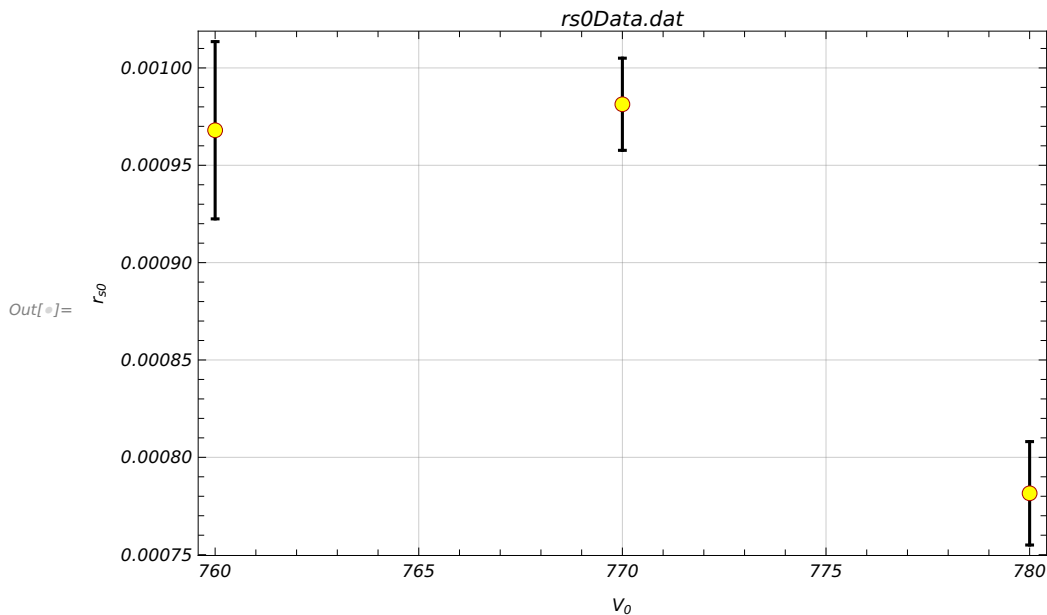
```
Out[ ]:= {{760, 0.000967994, 0.000045523},
          {770, 0.000981341, 0.0000236684}, {780, 0.000781524, 0.0000265562}}
```

```
In[ ]:= rs0Table =
  Join[{{"V0(V)", "rs0 (10-4 m)"}, Table[{rs0Val[[i]][[1]], StringReplace["%1 ± %2",
    {"%1" → ToString[NumberForm[rs0Val[[i]][[2]] * 104, 3]], "%2" → ToString[
      NumberForm[rs0Val[[i]][[3]] * 104, 2]]}], {i, 1, Length[rs0Val]}]]];
Grid[rs0Table, Alignment → Left, Spacings → {2, 1}, Frame → All,
  ItemStyle → "Text", Background → {{Gray, None}, {LightGray, None}}]
```

| $V_0(V)$ | $r_{s0} (10^{-4} m)$ |
|----------|----------------------|
| 760      | $9.68 \pm 0.46$      |
| 770      | $9.81 \pm 0.24$      |
| 780      | $7.82 \pm 0.27$      |

```
In[ ]:= Export["rs0Data.dat", rs0Val];
```

```
In[ ]:= LinearDataPlot[FrameLabel → {"V0", "rs0"}]
```



Because of the scarcity of the data, and the fact that we only have rough estimates on the uncertainties (since we only have a single trace for each data point), it is difficult to infer any sort of relation between  $V_0$  and  $r_{s0}$ . Even disregarding those issues, we do not observe a clear trend in the table above or by plotting the three data points.

## Determining mobility of $\text{Ne}^+$

```
In[140]:= (* We use a package I wrote to help with propagation of uncertainties. *)
<< SimpleErrorPropagation`
```

```
In[142]:= errorFunction = PropagateUncertainties[
```

$$\frac{(rs0 \log[b/a])^2}{vP \left( v0 - \frac{cp}{cd} \left( \frac{1}{2} vP - vE \right) \right)} dVOut, \{rs0, vP, cp, vE, dVOut\}] // \text{Simplify}$$

$$\text{Out[142]} = \sqrt{\left( \left( 1.50903 \times 10^{25} cp^2 dVOut^2 rs0^4 sigmaVE^2 vP^2 + \right. \right. \\ \left. 1.50903 \times 10^{25} dVOut^2 rs0^4 sigmaCp^2 \left( vE - \frac{vP}{2} \right)^2 vP^2 + \right. \\ \left. 102.011 rs0^4 sigmaDVOut^2 vP^2 \left( 3.84615 \times 10^{11} cp vE + v0 - 1.92308 \times 10^{11} cp vP \right)^2 + \right. \\ \left. 408.042 dVOut^2 rs0^2 sigmaRs0^2 vP^2 \left( 3.84615 \times 10^{11} cp vE + v0 - 1.92308 \times 10^{11} cp vP \right)^2 + \right. \\ \left. 1.50903 \times 10^{25} dVOut^2 rs0^4 sigmaVP^2 \left( 1. cp vE + 2.6 \times 10^{-12} v0 - 1. cp vP \right)^2 \right) / \\ \left( vP^4 \left( 3.84615 \times 10^{11} cp vE + v0 - 1.92308 \times 10^{11} cp vP \right)^4 \right) \Bigg)$$

```
In[143]:= μ[v0_, vP_, vE_, rs0_, cp_, dVOut_, sigmaVP_, sigmaVE_,
```

$$\text{sigmaRs0_, sigmaCp_, sigmaDVOut_}] := \left\{ \frac{(rs0 \log[b/a])^2}{vP \left( v0 - \frac{cp}{cd} \left( \frac{1}{2} vP - vE \right) \right)} dVOut, \right.$$

$$\sqrt{\left( \left( 1.5090314822808658 \cdot 10^{25} cp^2 dVOut^2 rs0^4 sigmaVE^2 vP^2 + 1.5090314822808658 \cdot 10^{25} \right. \right. \\ \left. dVOut^2 rs0^4 sigmaCp^2 \left( vE - \frac{vP}{2} \right)^2 vP^2 + 102.01052820218655 \cdot rs0^4 sigmaDVOut^2 \right. \\ \left. vP^2 \left( 3.846153846153846 \cdot 10^{11} cp vE + v0 - 1.923076923076923 \cdot 10^{11} cp vP \right)^2 + \right. \\ \left. 408.0421128087462 \cdot dVOut^2 rs0^2 sigmaRs0^2 vP^2 \right. \\ \left. \left( 3.846153846153846 \cdot 10^{11} cp vE + v0 - 1.923076923076923 \cdot 10^{11} cp vP \right)^2 + \right. \\ \left. 1.5090314822808658 \cdot 10^{25} dVOut^2 rs0^4 sigmaVP^2 \right. \\ \left. \left( 1. \cdot cp vE + 2.6000000000000002 \cdot 10^{-12} v0 - 1. \cdot cp vP \right)^2 \right) / \\ \left( vP^4 \left( 3.846153846153846 \cdot 10^{11} cp vE + v0 - 1.923076923076923 \cdot 10^{11} cp vP \right)^4 \right) \Bigg) \Bigg\}$$

```
In[146]:= mobility =
  Partition[Flatten[Table[{vpValUnc[[i]][[1]],  $\mu_n$ [vpValUnc[[i]][[1]] (* v0 *) ,
    vpValUnc[[i]][[2]] (* vp *) , veVal[[i]][[2]] (* ve *) , rs0Val[[i]][[2]]
    (* rs0 *) , cap[[1]] (* c *) , dvOut[[i]][[2]] (* dvOut *) ,
    vpValUnc[[i]][[3]] (* sigmavp *) , veVal[[i]][[3]] (* sigmave *) ,
    rs0Val[[i]][[3]] (* sigmars0 *) , cap[[2]] (* sigmacp *) ,
    dvOut[[i]][[3]] (* sigmadvOut *)}], {i, 1, Length[vpValUnc]}], 3]

Out[146]= {{760, 0.000900461, 0.0000869232},
  {770, 0.000896119, 0.0000448031}, {780, 0.000741873, 0.0000528969}}
```

```
In[147]:= mobilityTable = Join[{{"V0(V)", " $\mu_d$  ( $10^{-4}$  m2V-1s-1)"}},
  Table[{mobility[[i]][[1]], StringReplace["%1  $\pm$  %2",
    {"%1"  $\rightarrow$  ToString[NumberForm[mobility[[i]][[2]] * 104, 3]], "%2"  $\rightarrow$  ToString[
    NumberForm[mobility[[i]][[3]] * 104, 2]]}], {i, 1, Length[mobility]}]];
Grid[mobilityTable, Alignment  $\rightarrow$  Left, Spacings  $\rightarrow$  {2, 1}, Frame  $\rightarrow$  All,
  ItemStyle  $\rightarrow$  "Text", Background  $\rightarrow$  {{Gray, None}, {LightGray, None}}]
```

Out[148]=

| $V_0(V)$ | $\mu_d(10^{-4} \text{ m}^2\text{V}^{-1}\text{s}^{-1})$ |
|----------|--|
| 760      | $9. \pm 0.87$  |
| 770      | $8.96 \pm 0.45$  |
| 780      | $7.42 \pm 0.53$  |

We now convert our mobility values to mobilities at standard pressure using the conversion factor determined in the pre-lab.

```
In[149]:= stdMobility = Table[{mobility[[i]][[1]],  $\frac{\text{mobility}[[i]][[2]]}{760} * 425,$ 
   $\frac{\text{mobility}[[i]][[3]]}{760} * 425$ }, {i, 1, Length[mobility]}]

Out[149]= {{760, 0.000503547, 0.0000486084},
  {770, 0.000501119, 0.0000250544}, {780, 0.000414863, 0.0000295805}}
```

```

In[152]:= stdMobilityTable = Join[{"V0 (V)", "μd (10-4 m2V-1s-1)"},
  Table[{stdMobility[[i]][[1]], StringReplace["%1 ± %2",
    {"%1" → ToString[NumberForm[stdMobility[[i]][[2]] * 104, 3]],
    "%2" → ToString[NumberForm[stdMobility[[i]][[3]] * 104, 2]]}],
    {i, 1, Length[stdMobility]}]];
Grid[stdMobilityTable, Alignment → Left, Spacings → {2, 1}, Frame → All,
  ItemStyle → "Text", Background → {{Gray, None}, {LightGray, None}}]

```

Out[153]=

| V <sub>0</sub> (V) | μ <sub>d</sub> (10 <sup>-4</sup> m <sup>2</sup> V <sup>-1</sup> s <sup>-1</sup> ) |
|--------------------|---|
| 760                | 5.04 ± 0.49   |
| 770                | 5.01 ± 0.25   |
| 780                | 4.15 ± 0.3  |

We observe very similar mobilities for the bias voltages of 760V and 770V, both being higher than what we would expect for Ne<sup>+</sup> and lower than what we would expect for Br<sup>+</sup>. This is somewhat expected for a mixture of ions with different mobilities, although we would need more information to better qualify this statement. The mobility for a bias voltage of 780V, however, appears to be very close to the expected mobility of Ne<sup>+</sup>. Again, it is difficult to make any conclusive statements given the scarcity of the data.