

The solid-state diode - Experiment 13

```
In[1]:= << CurveFit`
```

CurveFit for Mathematica v7.x thru v11.x, Version 1.96, 4/4/2018

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Note: The plot labels write the current units as A, but the data is in mA and the processing is done with this kept in mind. The plot labels have not been modified because this was noticed after all plots were completed and CurveFit does not save intermediary datasets, so recreating the plots would have been prohibitively time-consuming.

Testing the PN junction theory

We fit our data for the IV-curves of our diodes at room temperature and dry ice temperature to test how closely the data follows the theory presented in the lab manual. We also fit several regions of each dataset to test the theory in different regimes.

```
In[169]:= (* We start by writing a function that commits the fit parameters for each region
of each dataset to a list with structure {region, a, siga, b, sigb,  $\tilde{\chi}^2$ }. Region
and  $\tilde{\chi}^2$  have to be entered manually, looking through CurveFit code,
documentation and variables does not show  $\tilde{\chi}^2$  being stored as a variable. *)
```

```
(* Initializing list *)
fitParam = {};
```

```
In[79]:= (* Committing fit parameters to list. *)
commitFit[region_, chisq_] := AppendTo[fitParam, {region, a, siga, b, sigb, chisq}];
```

```
In[6]:= SetDirectory[StringJoin[NotebookDirectory[], "Diode"]];
```

Silicon diode - Room Temperature

Whole dataset (bad points removed)

For all datasets we remove the lowest data point both for the high-current and low-current data. In lab we observed a discrepancy between measurements at the same current when the measurement corresponded to the lowest-current data point of both the high- and low- current datasets. There was no such discrepancy when the same measurement was not the lowest-current point on a dataset, indicating a hardware issue. Therefore we disregard both those points in the following analysis.

```

In[170]:= With[ {name = SystemDialogInput["FileOpen",
      {DataFileName, {"data files" -> {"*.dat", "*.mca"}, "all files" -> {"*"}}}]},
      If[ name != $Canceled,
        LoadFile[name]]
    ]

In[171]:= NRangeRemove /@ {1, 1, 17, 17}

In[172]:= With[{x = SetXRange[ LinearDataPlot[], Log -> False,
      Label -> "Set the X values for the range you wish to keep." ]},
      Print[x];

      XRangeKeep[Sequence @@ x]
    ]

{-0.0154283, 0.755987}

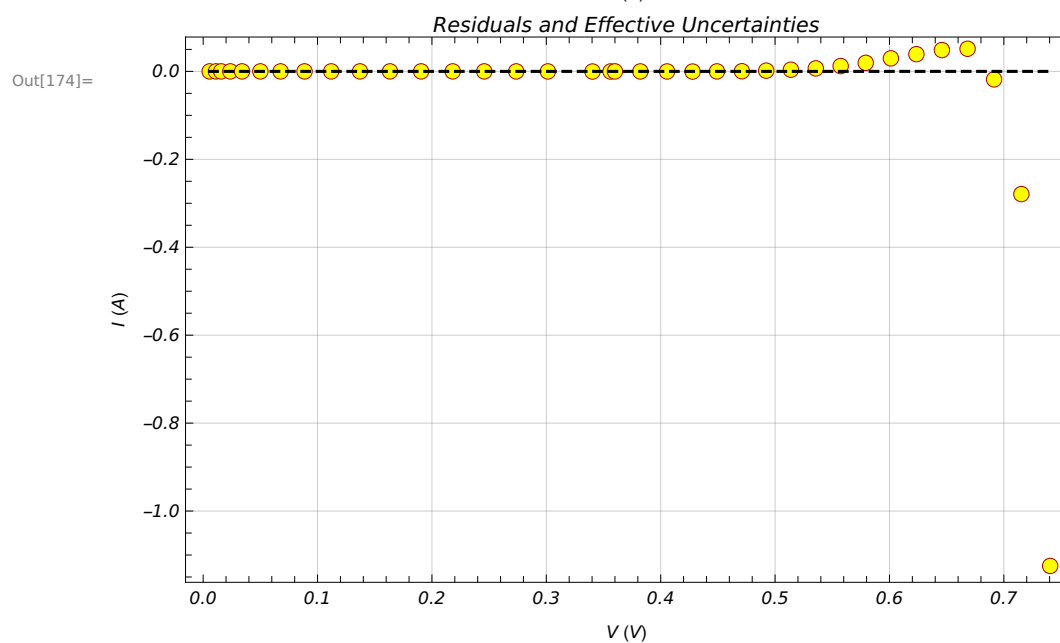
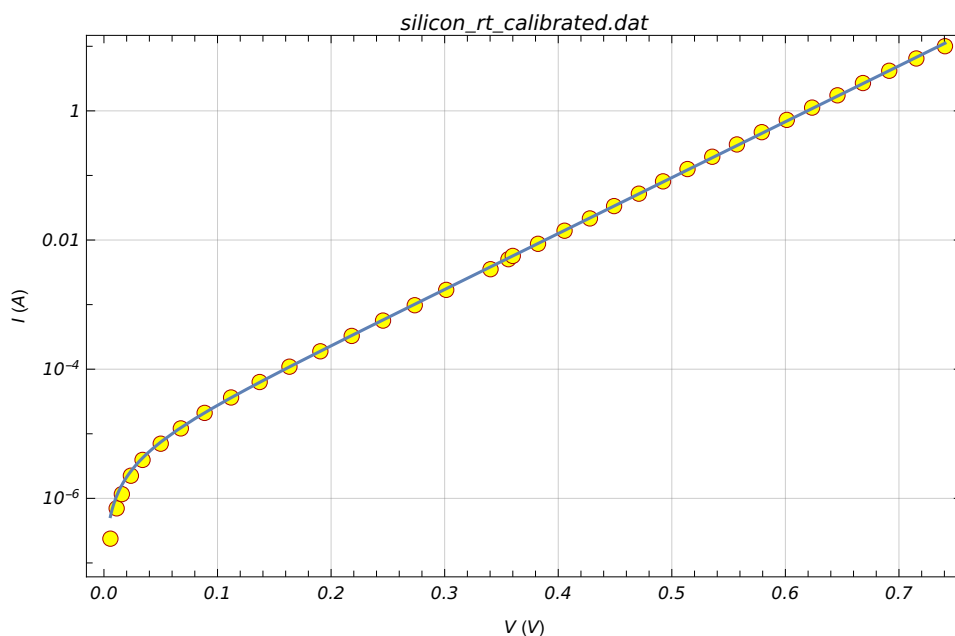
n= 36

0 points removed.

In[173]:= DiodeFit[]

```

In[174]:= `LogDifferencePlot[FrameLabel → {"V (V)", "I (A)"}]`



$$y(x) = a \left(\exp[b x] - 1 \right)$$

$$a = 4.35498 \times 10^{-6} \quad b = 19.927$$

$$\sigma_a = 4.65343 \times 10^{-9} \quad \sigma_b = 0.00180498 \quad \chi^2 / (n-2) = 512.572$$

In[175]:= `commitFit[{-0.015428312500000001`, 0.7559873125`}, 512.5724700933897`];`

Low voltage

```

In[176]:= With[ {name = SystemDialogInput["FileOpen",
      {DataFileName, {"data files" -> {"*.dat", "*.mca"}, "all files" -> {"*"}}}}],
      If[ name != $Canceled,
        LoadFile[name]]
    ]

In[177]:= NRangeRemove /@ {1, 1, 17, 17};

In[178]:= With[{x = SetXRange[ LinearDataPlot[], Log -> False,
      Label -> "Set the X values for the range you wish to keep." ]},
      Print[x];

      XRangeKeep[Sequence @@ x]
    ]

{-0.0154283, 0.1484}

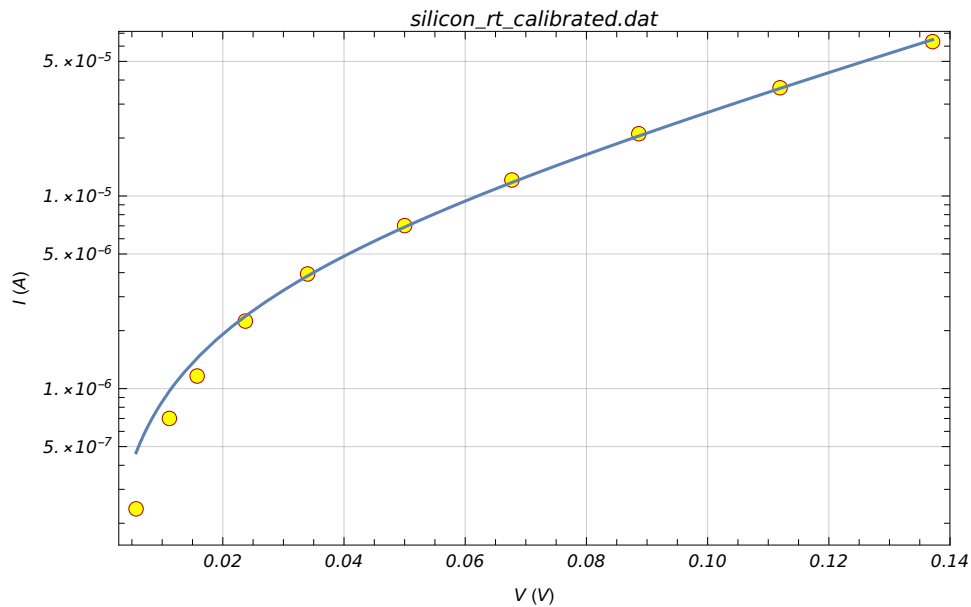
n= 10

26 points removed.

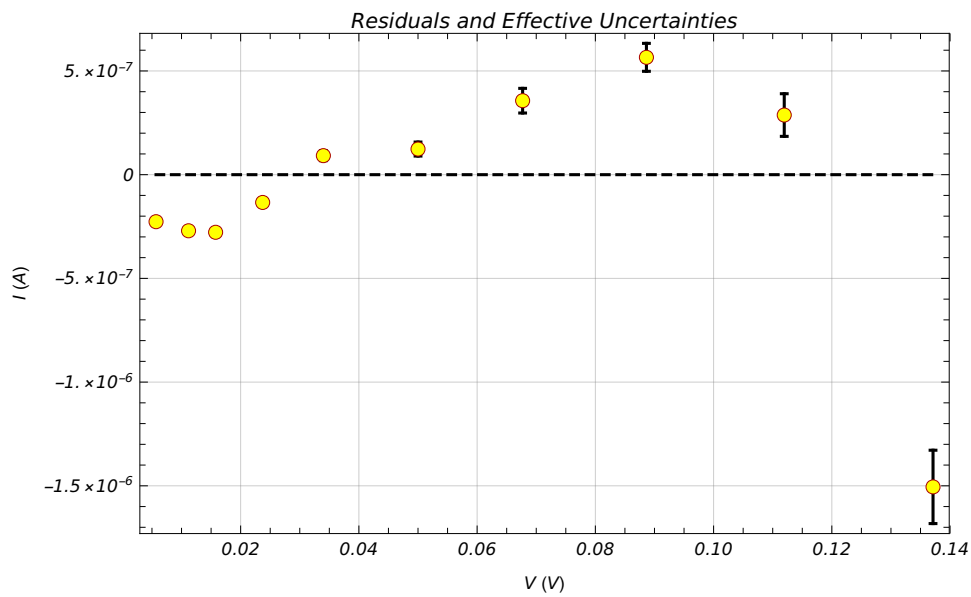
In[179]:= DiodeFit[]

```

```
In[180]:= LogDifferencePlot[FrameLabel → {"V (V)", "I (A)"}]
```



```
Out[180]=
```



$$y(x) = a \left(\exp[b x] - 1 \right)$$

$$a = 3.55954 \times 10^{-6} \quad b = 21.5518$$

$$\sigma_a = 2.24398 \times 10^{-8} \quad \sigma_b = 0.0548155 \quad \chi^2 / (n-2) = 170.084$$

```
In[181]:= commitFit[{-0.015428312500000001`, 0.1484`}, 170.08393446581536`];
```

Medium voltage

```

In[182]:= With[ {name = SystemDialogInput["FileOpen",
      {DataFileName, {"data files" -> {"*.dat", "*.mca"}, "all files" -> {"*"}}}}],
      If[ name != $Canceled,
        LoadFile[name]]
    ]

In[183]:= NRangeRemove /@ {1, 1, 17, 17};

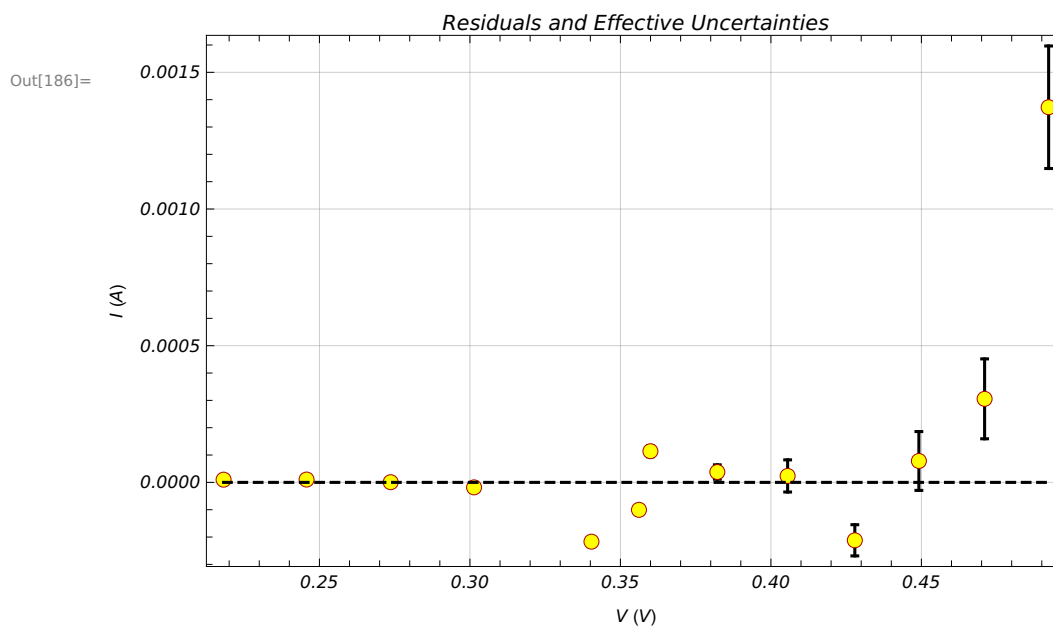
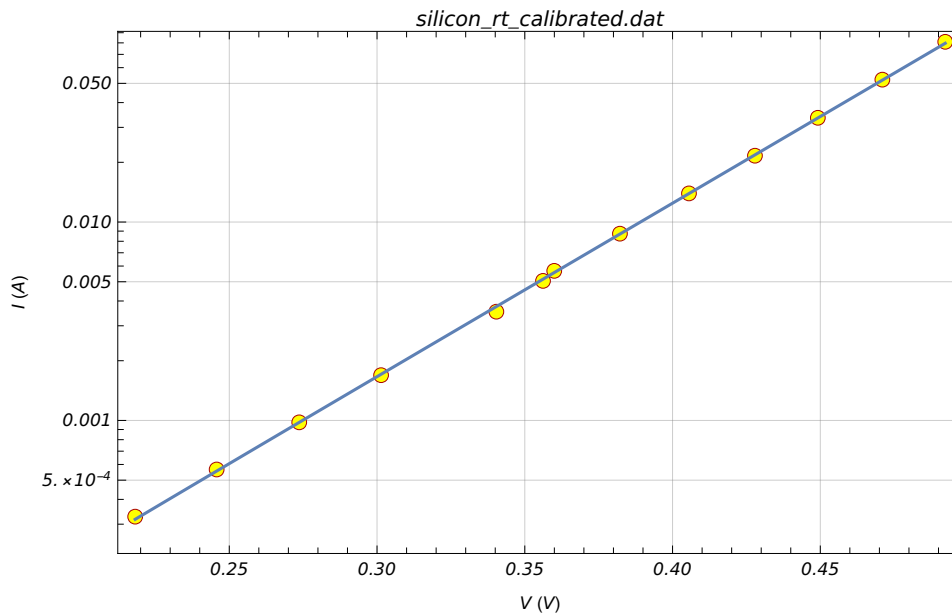
In[184]:= With[{x = SetXRange[ LinearDataPlot[], Log -> False,
      Label -> "Set the X values for the range you wish to keep." ]},
      Print[x];

      XRangeKeep[Sequence @@ x]
    ]
    {0.206, 0.5024}
    n= 13
    23 points removed.

In[185]:= DiodeFit[]

```

```
In[186]:= LogDifferencePlot[FrameLabel → {"V (V)", "I (A)"}]
```



$$y(x) = a \left(\exp[b x] - 1 \right)$$

$$a = 3.99897 \times 10^{-6} \quad b = 20.1083$$

$$\sigma_a = 1.53239 \times 10^{-8} \quad \sigma_b = 0.0101499 \quad \chi^2 / (n-2) = 41.4013$$

```
In[187]:= commitFit[{0.20600000000000002`, 0.5024000000000001`}, 41.401251771117565`];
```

High voltage

```

In[188]:= With[ {name = SystemDialogInput["FileOpen",
      {DataFileName, {"data files" -> {"*.dat", "*.mca"}, "all files" -> {"*"}}}}],
      If[ name != $Canceled,
        LoadFile[name]]
    ]

In[189]:= NRangeRemove /@ {1, 1, 17, 17};

In[190]:= With[{x = SetXRange[ LinearDataPlot[], Log -> False,
      Label -> "Set the X values for the range you wish to keep." ]},
      Print[x];

      XRangeKeep[Sequence @@ x]
    ]

    {0.501, 0.755987}

    n= 11

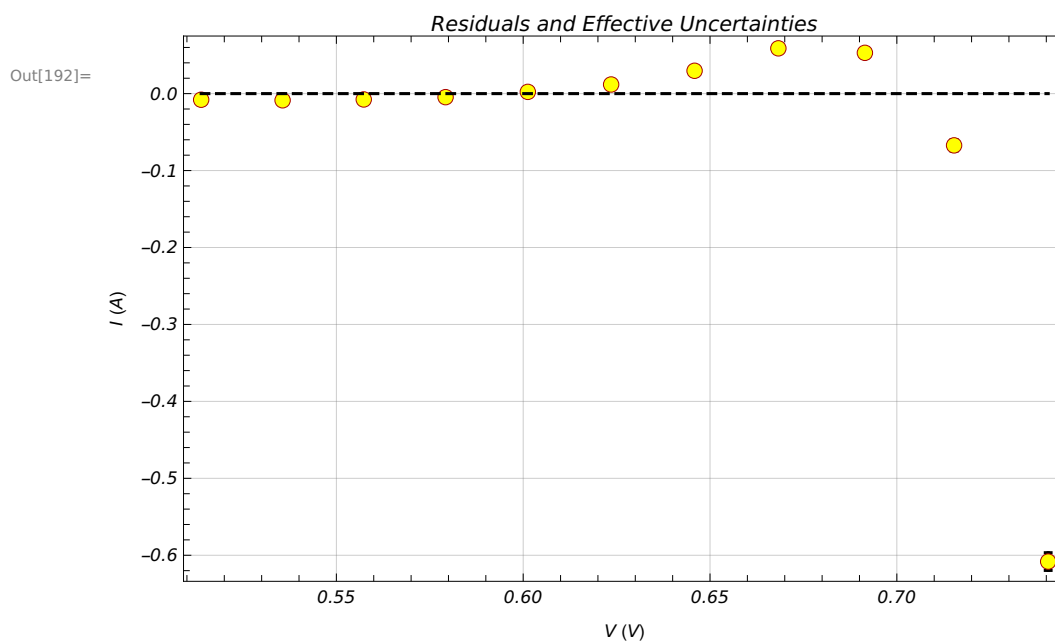
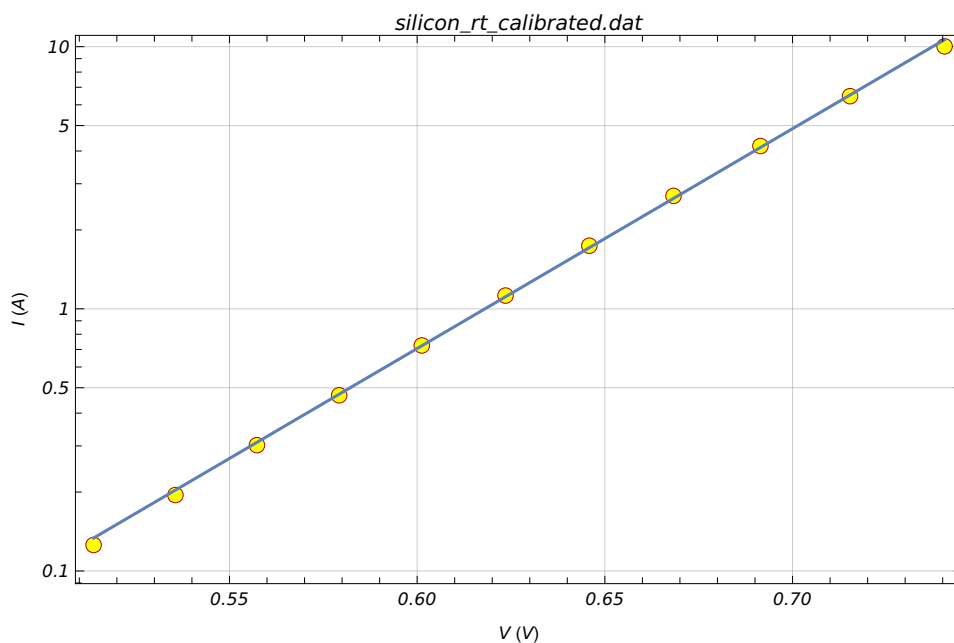
    25 points removed.

In[191]:= DiodeFit[]

```



```
In[192]:= LogDifferencePlot[FrameLabel → {"V (V)", "I (A)"}]
```



$$y(x) = a \left(\exp[b x] - 1 \right)$$

$$a = 6.56404 \times 10^{-6} \quad b = 19.3088$$

$$\sigma_a = 2.94935 \times 10^{-8} \quad \sigma_b = 0.00677837 \quad \chi^2 / (n-2) = 626.02$$

```
In[193]:= commitFit[{0.501`, 0.7559873125`}, 626.0195037513873`];
```

```
In[194]:= (* We store the collected data in a separate dataset for silicon
diode at room temp and re-initialize fitParam for further use. *)
siliconRT = fitParam;
```

```
In[195]:= fitParam = {};
```

Silicon diode - Dry Ice Temperature

Whole dataset (bad points removed)

```
In[197]:= With[ {name = SystemDialogInput["FileOpen",
      {DataFileName, {"data files" -> {"*.dat", "*.mca"}, "all files" -> {"*"}}}]},
  If[ name != $Canceled,
    LoadFile[name]]
]

In[198]:= NRangeRemove /@ {1, 1, 17, 17}

In[199]:= With[{x = SetXRange[ LinearDataPlot[], Log -> False,
  Label -> "Set the X values for the range you wish to keep." ]},
  Print[x];

  XRangeKeep[Sequence @@ x]
]

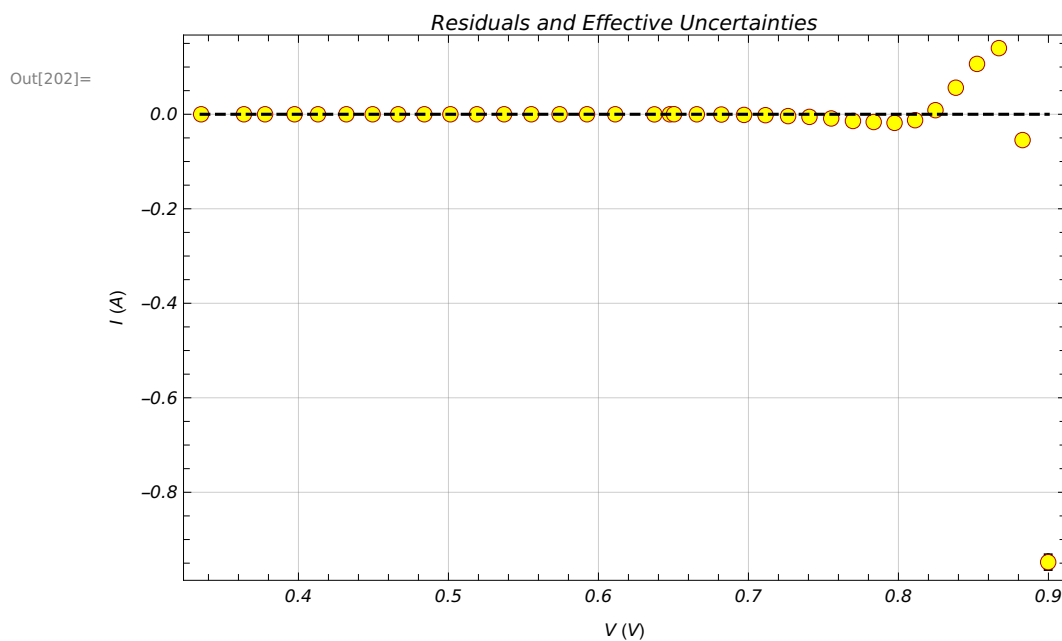
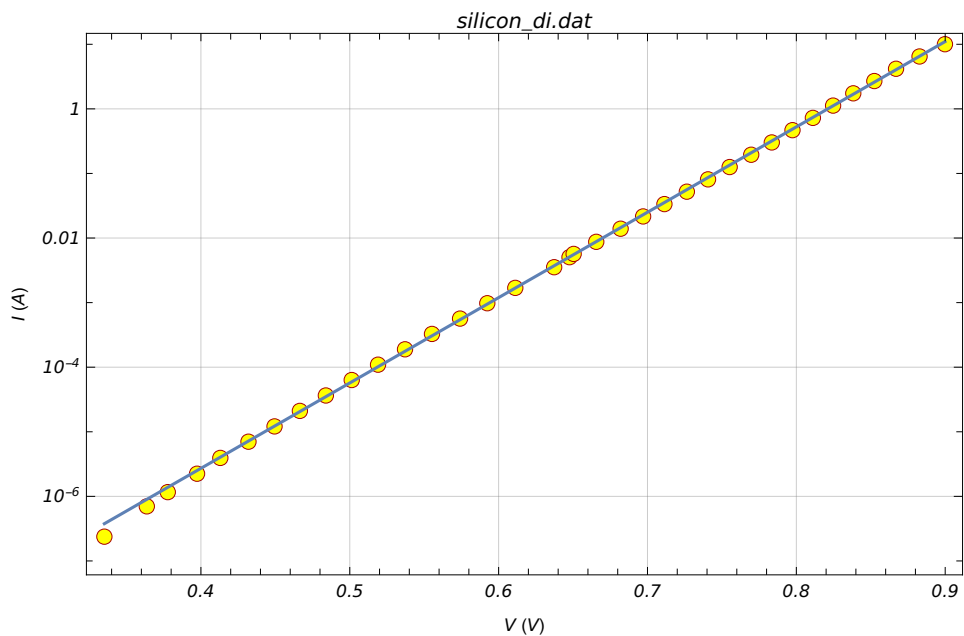
{0.323086, 0.911654}

n= 36

0 points removed.

In[201]:= DiodeFit[]
```

```
In[202]:= LogDifferencePlot[FrameLabel -> {"V (V)", "I (A)"}]
```



$$y(x) = a \left(\text{Exp}[b x] - 1 \right)$$

$$a = 1.40303 \times 10^{-11} \quad b = 30.4339$$

$$\sigma_a = 3.64541 \times 10^{-14} \quad \sigma_b = 0.00323305 \quad \chi^2 / (n-2) = 453.09$$

```
In[203]:= commitFit[{0.32308562499999993`, 0.911654375`}, 453.08954952184655`];
```

Low voltage

```

In[204]:= With[ {name = SystemDialogInput["FileOpen",
      {DataFileName, {"data files" -> {"*.dat", "*.mca"}, "all files" -> {"*"}}}}],
      If[ name != $Canceled,
        LoadFile[name]]
    ]

In[205]:= NRangeRemove /@ {1, 1, 17, 17};

In[206]:= With[{x = SetXRange[ LinearDataPlot[], Log -> False,
      Label -> "Set the X values for the range you wish to keep." ]},
      Print[x];

      XRangeKeep[Sequence @@ x]
    ]

{0.323086, 0.5102}

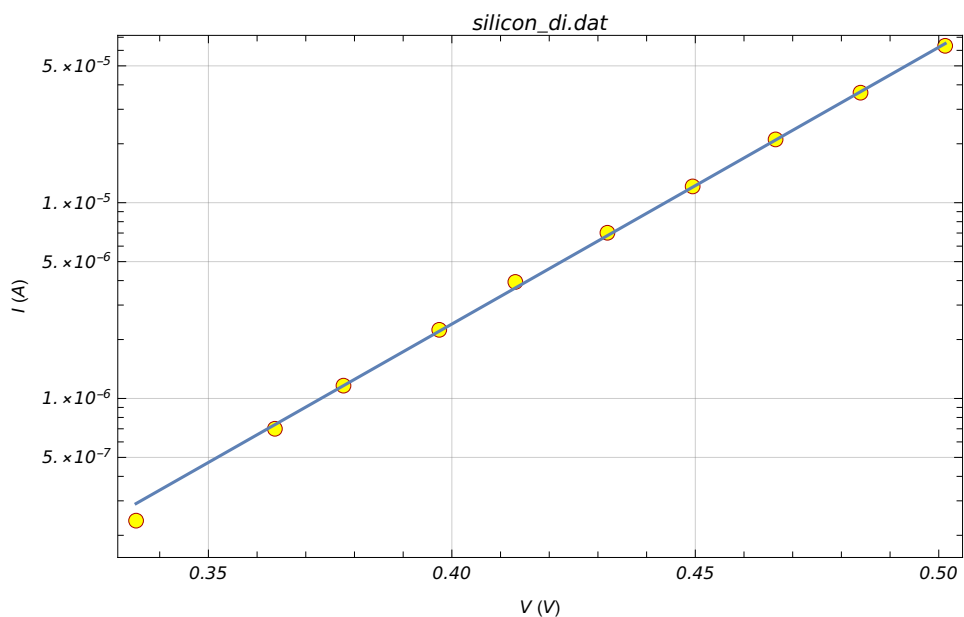
n= 10

26 points removed.

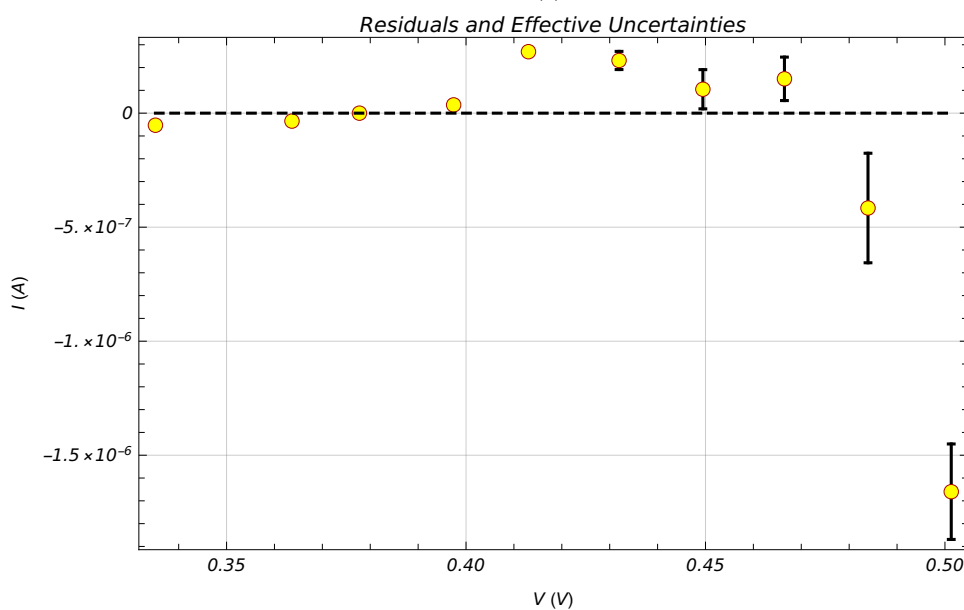
In[207]:= DiodeFit[]

```

In[208]:= **LogDifferencePlot**[FrameLabel → {"V (V)", "I (A)"}]



Out[208]=



$$y(x) = a \left(\exp[b x] - 1 \right)$$

$$a = 5.30356 \times 10^{-12} \quad b = 32.5559$$

$$\sigma_a = 8.93198 \times 10^{-14} \quad \sigma_b = 0.0372247 \quad \chi^2 / (n-2) = 92.7384$$

In[209]:= **commitFit**[{0.32308562499999993`, 0.5102`}, 92.73844942065703`];

Medium voltage

```

In[210]:= With[ {name = SystemDialogInput["FileOpen",
      {DataFileName, {"data files" -> {"*.dat", "*.mca"}, "all files" -> {"*"}}}}],
      If[ name != $Canceled,
        LoadFile[name]]
    ]

In[211]:= NRangeRemove /@ {1, 1, 17, 17};

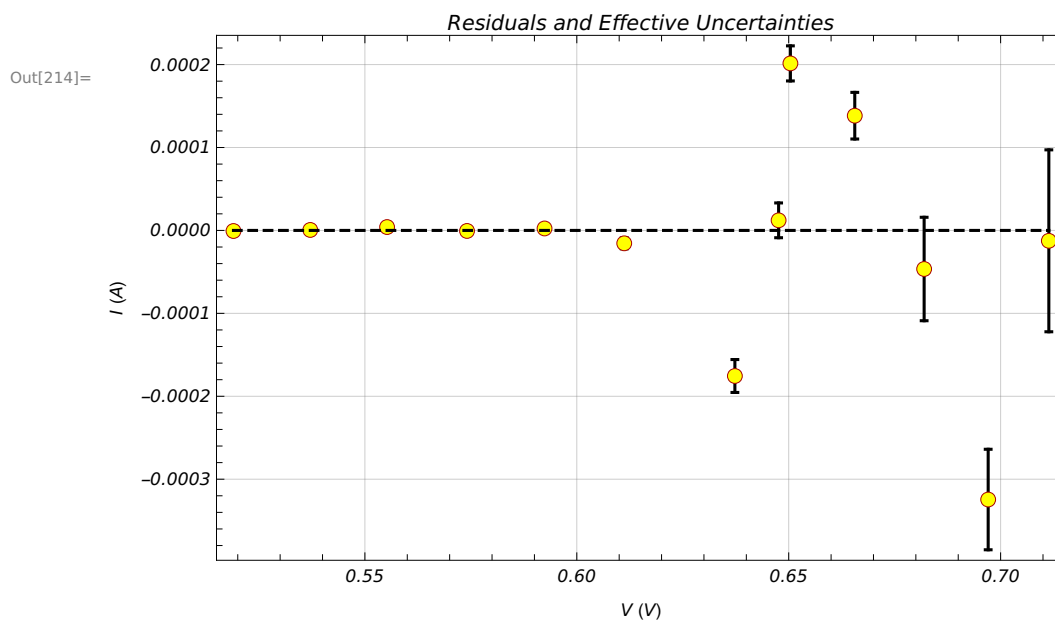
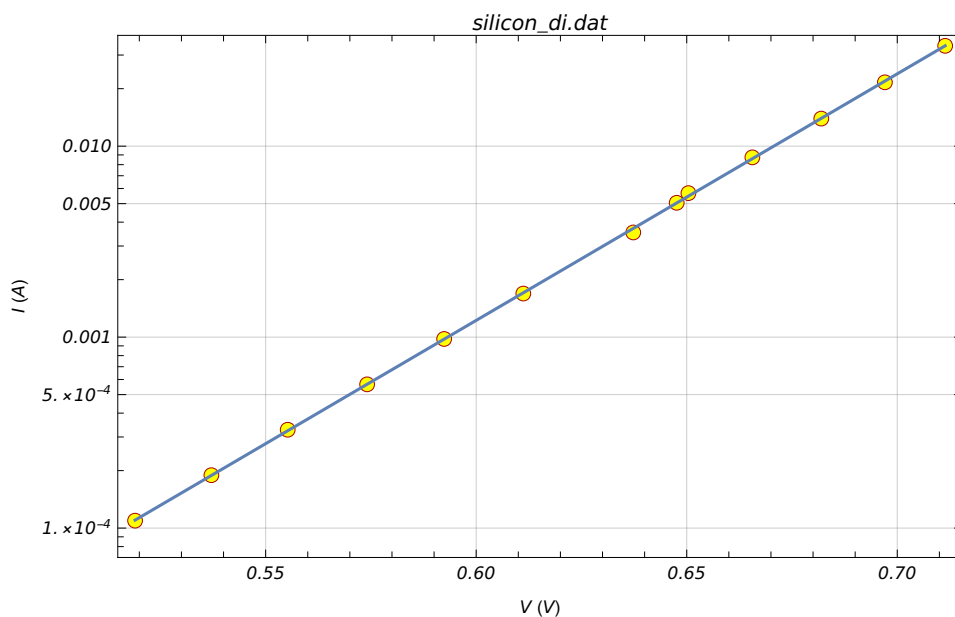
In[212]:= With[{x = SetXRange[ LinearDataPlot[], Log -> False,
      Label -> "Set the X values for the range you wish to keep." ]},
      Print[x];

      XRangeKeep[Sequence @@ x]
    ]
{0.5082, 0.7202}
n= 13
23 points removed.

In[213]:= DiodeFit[]

```

```
In[214]:= LogDifferencePlot[FrameLabel -> {"V (V)", "I (A)"}]
```



$$y(x) = a \left(\exp[b x] - 1 \right)$$

$$a = 2.19361 \times 10^{-11} \quad b = 29.7281$$

$$\sigma_a = 2.20064 \times 10^{-13} \quad \sigma_b = 0.0158754 \quad \chi^2 / (n-2) = 21.9023$$

```
In[215]:= commitFit[{0.5082`, 0.7202000000000001`}, 21.90234094658127`];
```

High voltage

```

In[216]:= With[ {name = SystemDialogInput["FileOpen",
      {DataFileName, {"data files" -> {"*.dat", "*.mca"}, "all files" -> {"*"}}}}],
      If[ name != $Canceled,
        LoadFile[name]]
    ]

    NRangeRemove /@ {1, 1, 17, 17};

In[217]:= With[{x = SetXRange[ LinearDataPlot[], Log -> False,
      Label -> "Set the X values for the range you wish to keep." ]},
      Print[x];

      XRangeKeep[Sequence @@ x]
    ]

    {0.7176, 0.911867}

    n= 13

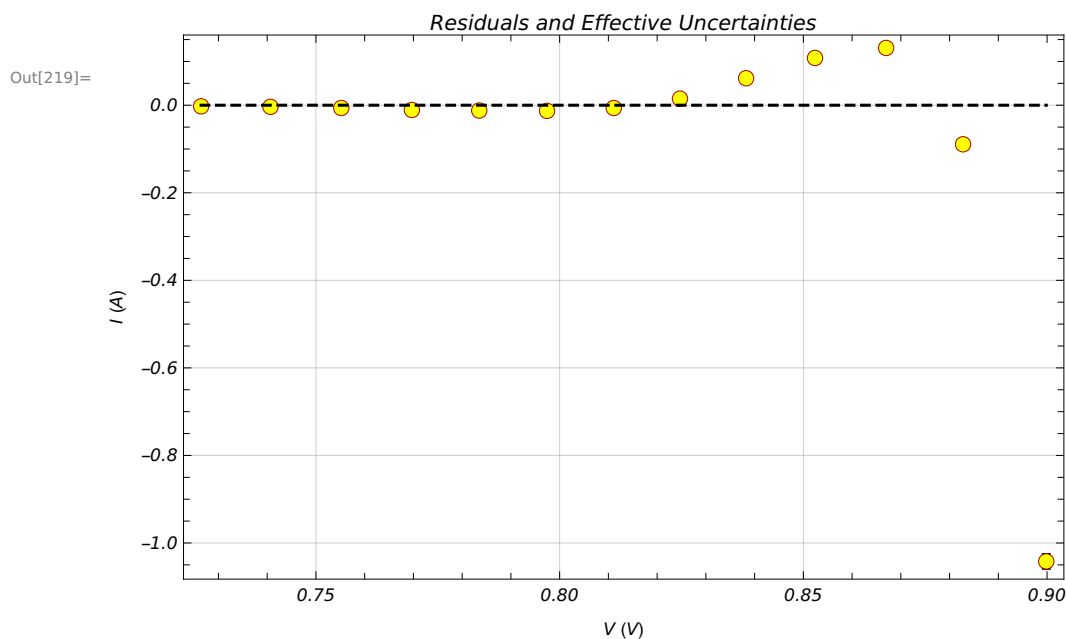
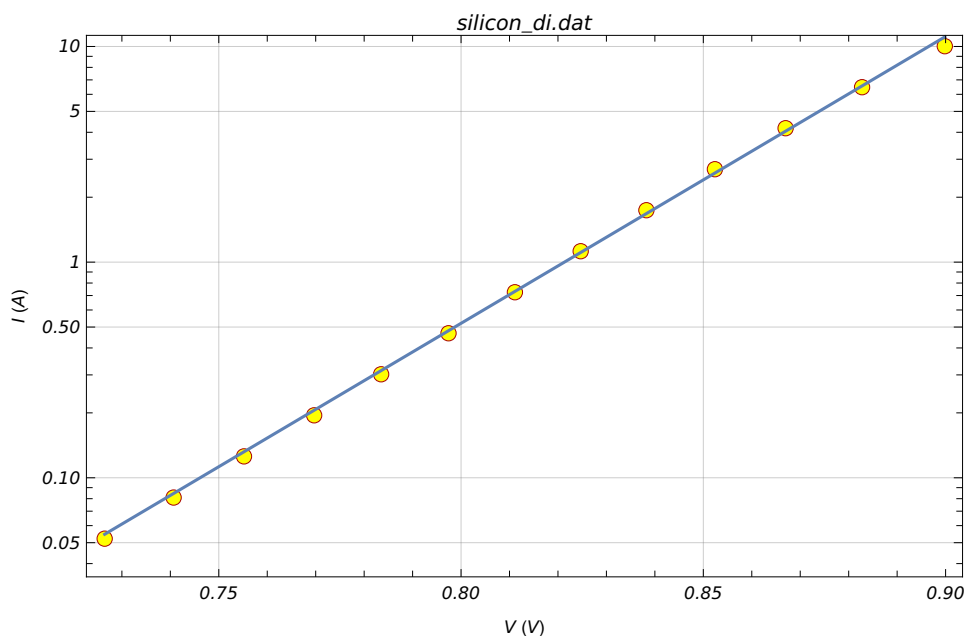
    27 points removed.

In[218]:= DiodeFit[]

```



```
In[219]:= LogDifferencePlot[FrameLabel → {"V (V)", "I (A)"}]
```



$$y(x) = a \left(\exp[b x] - 1 \right)$$

$$a = 1.19161 \times 10^{-11} \quad b = 30.625$$

$$\sigma_a = 1.24639 \times 10^{-13} \quad \sigma_b = 0.0122291 \quad \chi^2 / (n-2) = 785.199$$

```
In[220]:= commitFit[{0.7176`, 0.9118667291666667`}, 785.1993496718917`];
```

```
In[221]:= (* We store the collected data in a separate dataset for silicon
            diode at room temp and re-initialize fitParam for further use. *)
siliconDI = fitParam;
```

```
In[222]:= fitParam = {};
```

Germanium diode - Room Temperature

Whole dataset (bad points removed)

```
In[227]:= With[ {name = SystemDialogInput["FileOpen",
      {DataFileName, {"data files" -> {"*.dat", "*.mca"}, "all files" -> {"*"}}}]},
  If[ name != $Canceled,
    LoadFile[name]]
]

In[228]:= NRangeRemove /@ {1, 1, 17, 17}

In[229]:= With[{x = SetXRange[ LinearDataPlot[], Log -> False,
  Label -> "Set the X values for the range you wish to keep." ]},
  Print[x];

  XRangeKeep[Sequence @@ x]
]

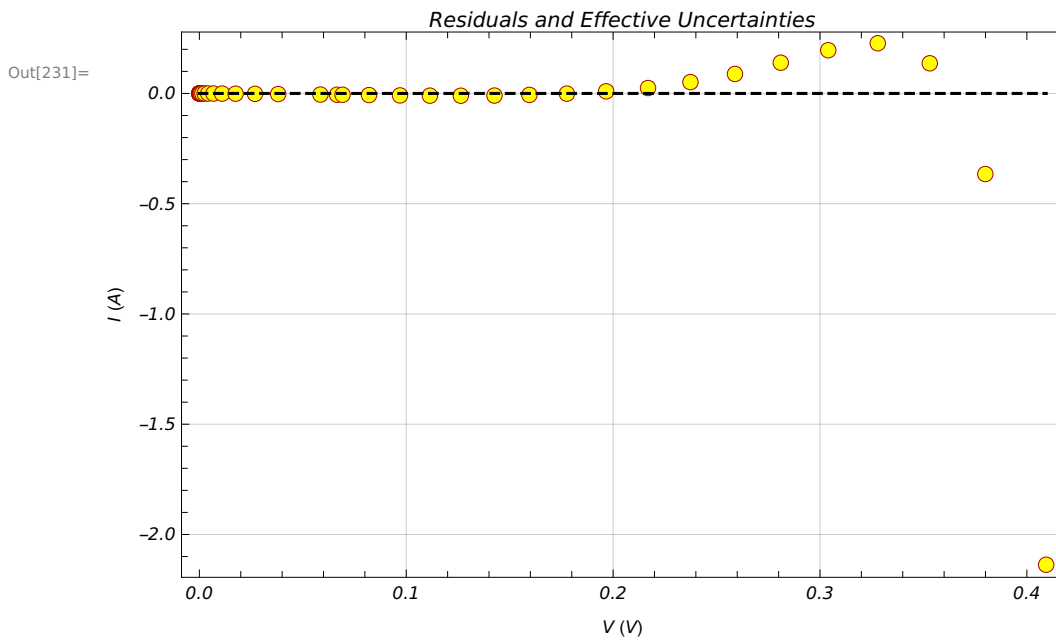
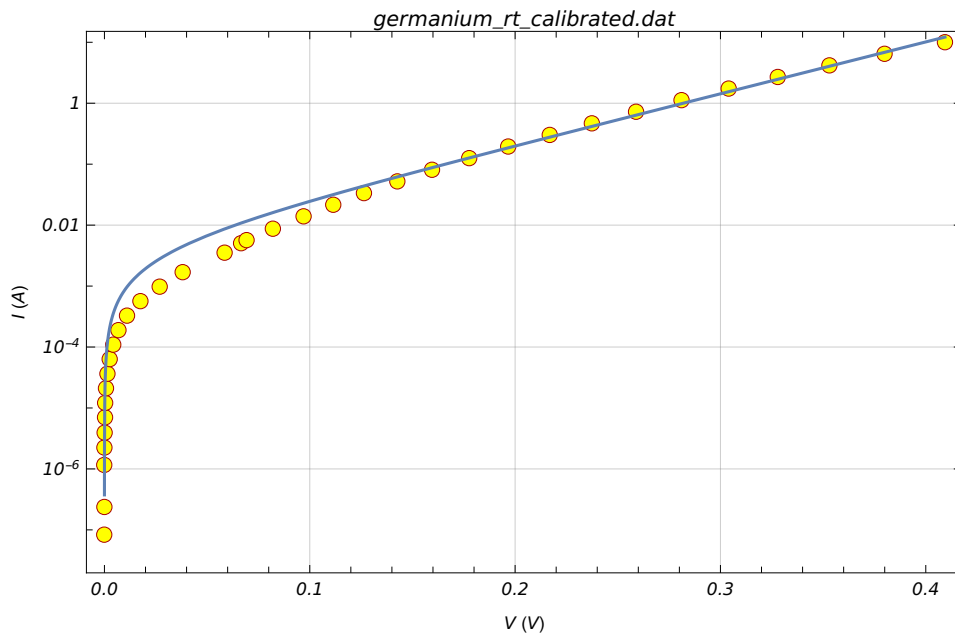
{-0.00877563, 0.417906}

n= 36

0 points removed.

In[230]:= DiodeFit[]
```

In[231]:= `LogDifferencePlot[FrameLabel → {"V (V)", "I (A)"}]`



$$y(x) = a \left(\exp[b x] - 1 \right)$$

$$a = 0.00403687 \quad b = 19.5712$$

$$\sigma_a = 5.81426 \times 10^{-6} \quad \sigma_b = 0.00438953 \quad \chi^2 / (n-2) = 10170.8$$

In[232]:= `commitFit[{-0.008775625`, 0.41790562499999995`}, 10170.77697297076`];`

Low voltage

```

In[233]:= With[ {name = SystemDialogInput["FileOpen",
      {DataFileName, {"data files" -> {"*.dat", "*.mca"}, "all files" -> {"*"}}}}],
      If[ name != $Canceled,
        LoadFile[name]]
    ]

In[234]:= NRangeRemove /@ {1, 1, 17, 17};

In[235]:= With[{x = SetXRange[ LinearDataPlot[], Log -> False,
      Label -> "Set the X values for the range you wish to keep." ]},
      Print[x];

      XRangeKeep[Sequence @@ x]
    ]

{-0.00877563, 0.0908}

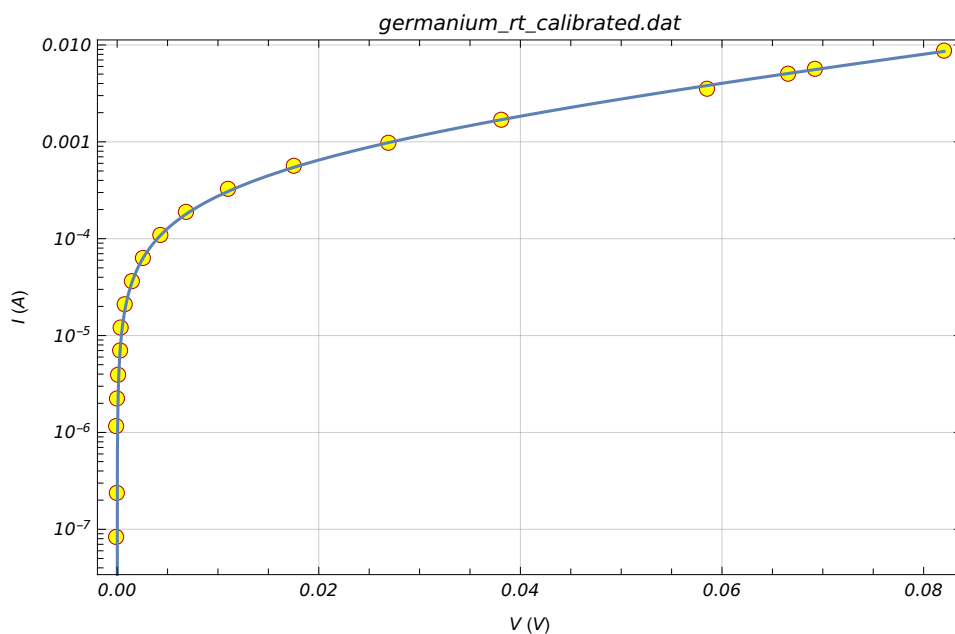
n= 20

16 points removed.

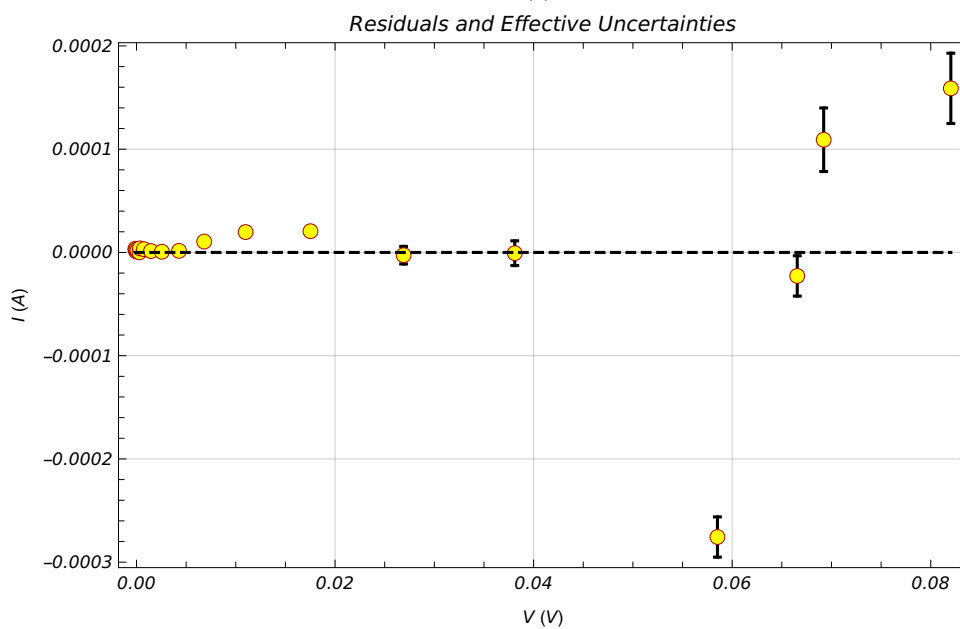
In[236]:= DiodeFit[]

```

In[237]:= `LogDifferencePlot[FrameLabel → {"V (V)", "I (A)"}]`



Out[237]=



$$y(x) = a \left(\exp[b x] - 1 \right)$$

$a =$	$b =$
0.000777601	30.326
$\sigma_a =$	$\sigma_b =$
7.22748×10^{-6}	0.124108
	$\chi^2 / (n-2) =$
	16.2077

In[238]:= `commitFit[{-0.008775625`, 0.0908`}, 16.207728611078206`];`

Medium voltage

```

In[239]:= With[ {name = SystemDialogInput["FileOpen",
      {DataFileName, {"data files" -> {"*.dat", "*.mca"}, "all files" -> {"*"}}}}],
      If[ name != $Canceled,
        LoadFile[name]]
    ]

In[240]:= NRangeRemove /@ {1, 1, 17, 17};

In[241]:= With[{x = SetXRange[ LinearDataPlot[], Log -> False,
      Label -> "Set the X values for the range you wish to keep." ]},
      Print[x];

      XRangeKeep[Sequence @@ x]
    ]
{0.104, 0.2466}

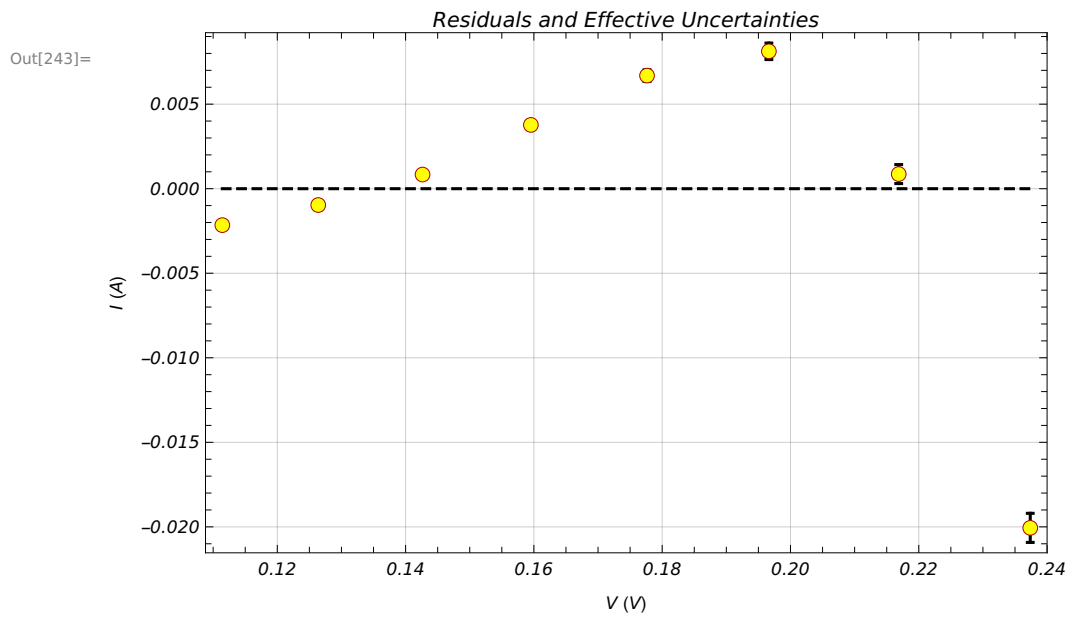
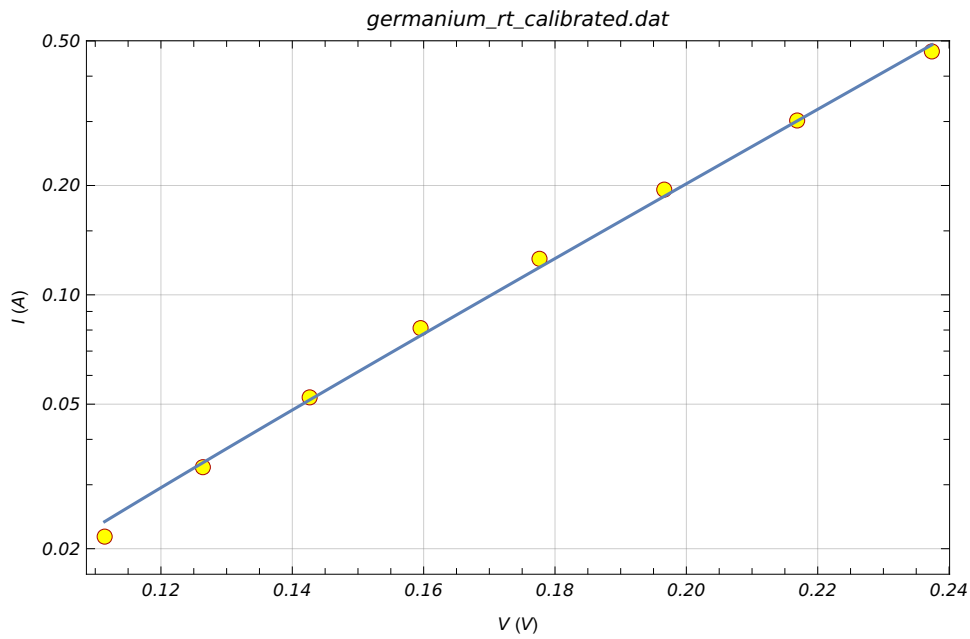
n= 8

28 points removed.

In[242]:= DiodeFit[]

```

In[243]:= `LogDifferencePlot[FrameLabel → {"V (V)", "I (A)"}]`



$$y(x) = a \left(\exp[b x] - 1 \right)$$

$$a = 0.00188447 \quad b = 23.4242$$

$$\sigma_a = 7.52439 \times 10^{-6} \quad \sigma_b = 0.0209988 \quad \chi^2 / (n-2) = 411.611$$

In[244]:= `commitFit[{0.10400000000000001`, 0.2466`}, 411.61120822450107`];`

High voltage

```

In[245]:= With[ {name = SystemDialogInput["FileOpen",
      {DataFileName, {"data files" -> {"*.dat", "*.mca"}, "all files" -> {"*"} }}}},
      If[ name != $Canceled,
        LoadFile[name]]
    ]

In[246]:= NRangeRemove /@ {1, 1, 17, 17};

In[247]:= With[{x = SetXRange[ LinearDataPlot[], Log -> False,
      Label -> "Set the X values for the range you wish to keep." ]},
      Print[x];

      XRangeKeep[Sequence @@ x]
    ]

{0.2473, 0.417906}

n= 7

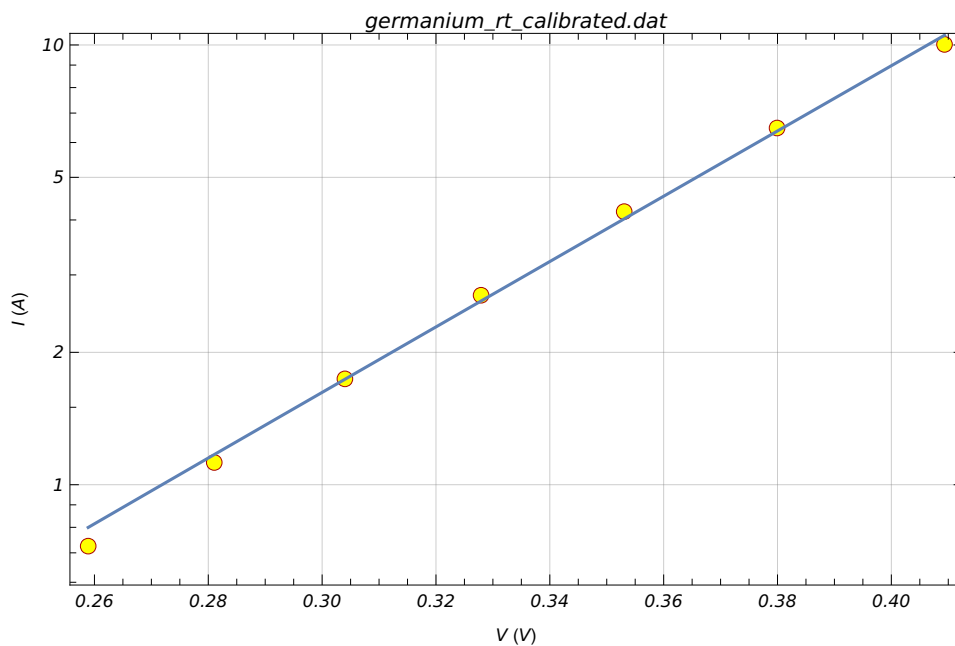
29 points removed.

In[248]:= DiodeFit[]

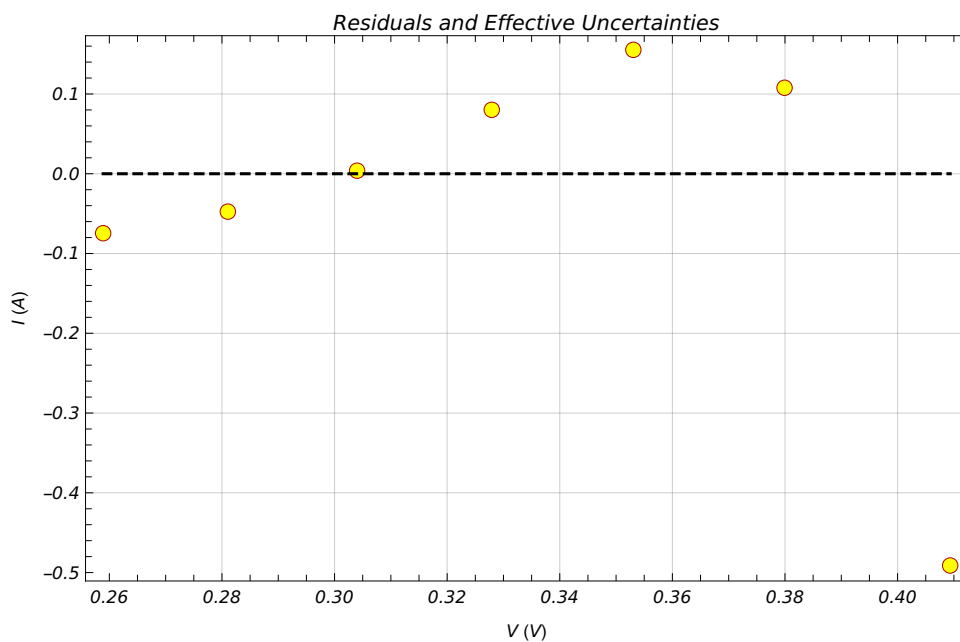
```



```
In[249]:= LogDifferencePlot[FrameLabel → {"V (V)", "I (A)"}]
```



```
Out[249]=
```



$$y(x) = a \left(\exp[b x] - 1 \right)$$

$$a = 0.0097824$$

$$b = 17.0552$$

$$\sigma_a = 0.0000209918$$

$$\sigma_b = 0.00600576$$

$$\chi^2 / (n-2) = 4168.84$$

```
In[250]:= commitFit[{0.2473`, 0.41790562499999995`}, 4168.841482732459`];
```

```
In[251]:= (* We store the collected data in a separate dataset for silicon
            diode at room temp and re-initialize fitParam for further use. *)
germaniumRT = fitParam;
```

```
In[252]:= fitParam = {};
```

Germanium diode - Dry Ice Temperature

Whole dataset (bad points removed)

```
In[255]:= With[ {name = SystemDialogInput["FileOpen",
      {DataFileName, {"data files" -> {"*.dat", "*.mca"}, "all files" -> {"*"}}}]},
  If[ name != $Canceled,
    LoadFile[name]]
]

In[256]:= NRangeRemove /@ {1, 1, 17, 17};

In[257]:= With[{x = SetXRange[ LinearDataPlot[], Log -> False,
  Label -> "Set the X values for the range you wish to keep." ]},
  Print[x];

  XRangeKeep[Sequence @@ x]
]

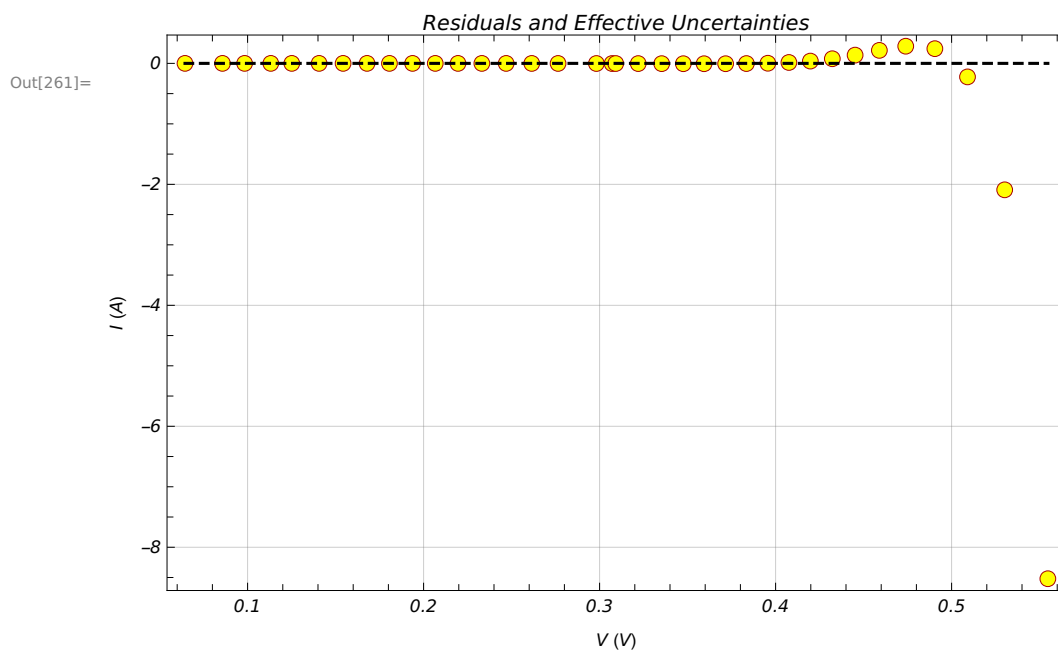
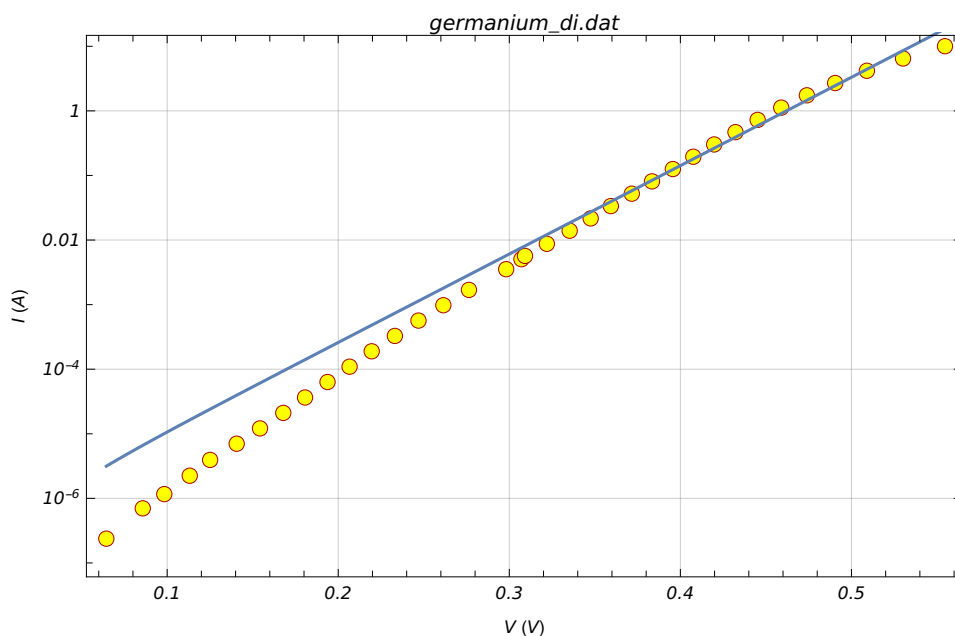
{0.0528011, 0.564946}

n= 36

0 points removed.

In[260]:= DiodeFit[]
```

```
In[261]:= LogDifferencePlot[FrameLabel → {"V (V)", "I (A)"}]
```



$$y(x) = a \left(\text{Exp}[b x] - 1 \right)$$

$$a = 4.75907 \times 10^{-7} \quad b = 31.5107$$

$$\sigma_a = 1.21462 \times 10^{-9} \quad \sigma_b = 0.00551868 \quad \chi^2 / (n-2) = 43186.9$$

```
In[262]:= commitFit[{0.05280110416666667`, 0.5649458958333333`}, 43186.93739403151`];
```

Low voltage

```

In[263]:= With[ {name = SystemDialogInput["FileOpen",
        {DataFileName, {"data files" -> {"*.dat", "*.mca"}, "all files" -> {"*"}}}}],
        If[ name != $Canceled,
            LoadFile[name]]
    ]

In[264]:= NRangeRemove /@ {1, 1, 17, 17};

In[265]:= With[{x = SetXRange[ LinearDataPlot[], Log -> False,
        Label -> "Set the X values for the range you wish to keep." ]},
        Print[x];

        XRangeKeep[Sequence @@ x]
    ]

    {0.0528011, 0.1999}

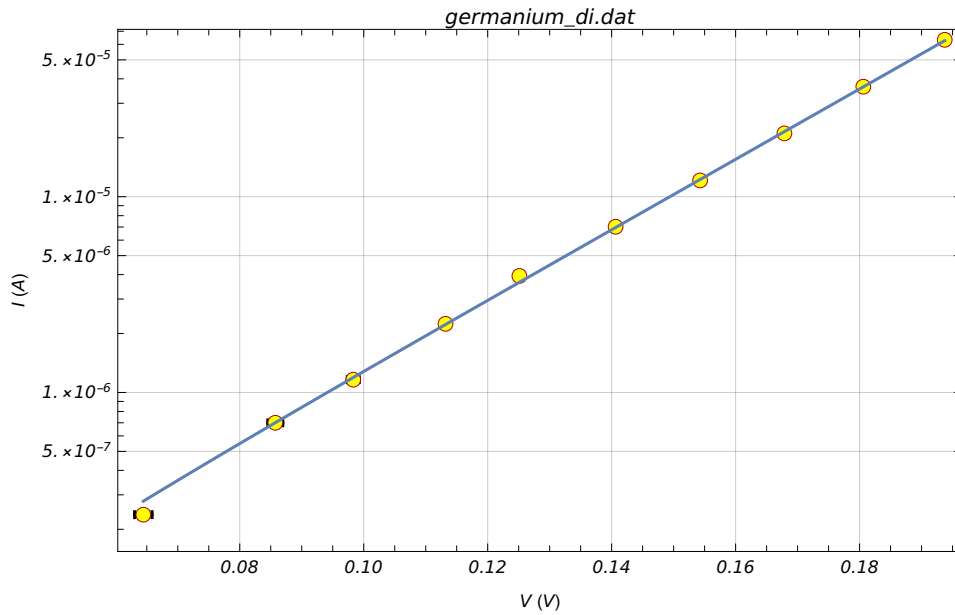
    n= 10

    26 points removed.

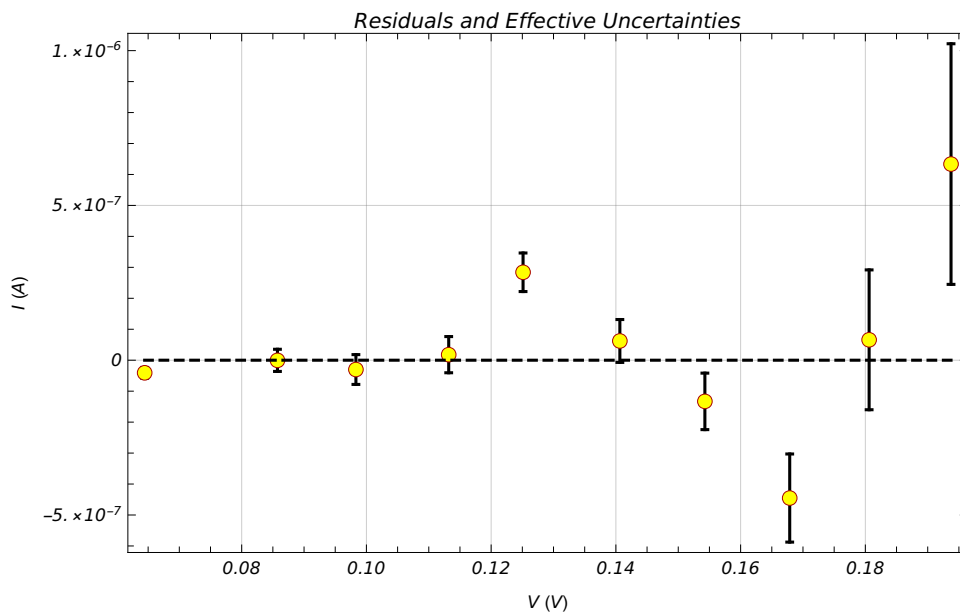
In[266]:= DiodeFit[]

```

In[267]:= `LogDifferencePlot[FrameLabel -> {"V (V)", "I (A)"}]`



Out[267]=



$$y(x) = a \left(\exp[b x] - 1 \right)$$

$$a = 2.08452 \times 10^{-8} \quad b = 41.3377$$

$$\sigma_a = 5.04666 \times 10^{-10} \quad \sigma_b = 0.140402 \quad \chi^2 / (n-2) = 5.28525$$

In[268]:= `commitFit[{0.05280110416666667, 0.19990000000000002}, 5.285252955291375];`

Medium voltage

```

In[271]:= With[ {name = SystemDialogInput["FileOpen",
      {DataFileName, {"data files" -> {"*.dat", "*.mca"}, "all files" -> {"*"}}}}],
      If[ name != $Canceled,
        LoadFile[name]]
    ]

In[272]:= NRangeRemove /@ {1, 1, 17, 17};

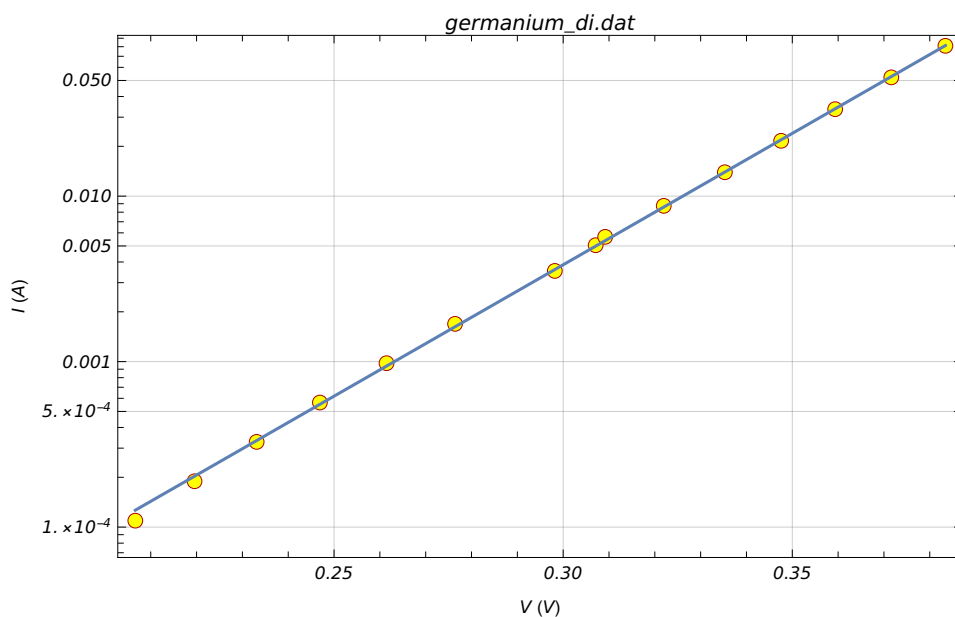
In[273]:= With[{x = SetXRange[ LinearDataPlot[], Log -> False,
      Label -> "Set the X values for the range you wish to keep." ]},
      Print[x];

      XRangeKeep[Sequence @@ x]
    ]
{0.2008, 0.3901}
n= 15
21 points removed.

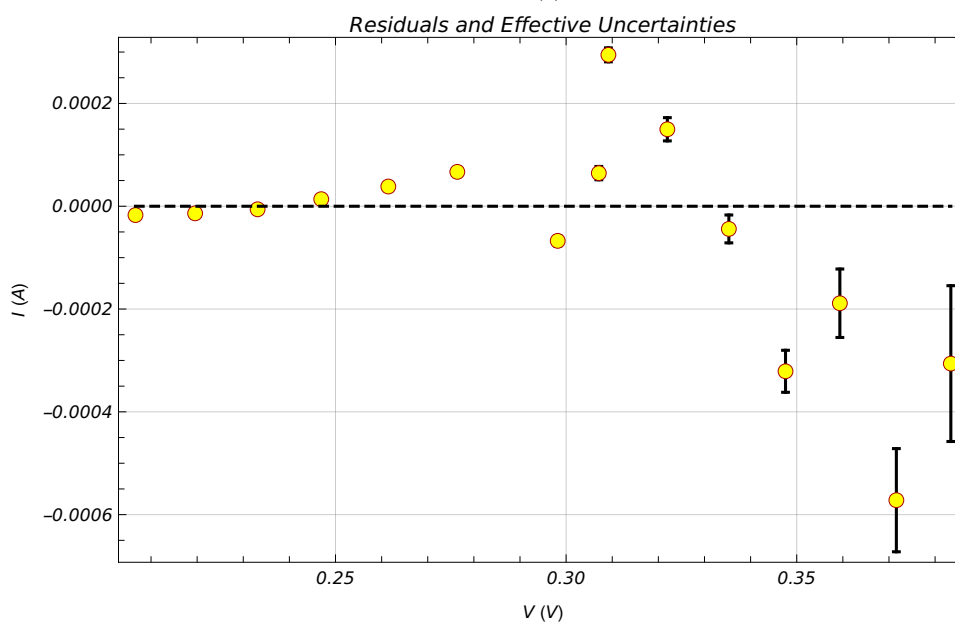
In[274]:= DiodeFit[]

```

```
In[275]:= LogDifferencePlot[FrameLabel -> {"V (V)", "I (A)"}]
```



```
Out[275]=
```



$$y(x) = a \left(\exp[b x] - 1 \right)$$

$$a = 6.61959 \times 10^{-8} \quad b = 36.5684$$

$$\sigma_a = 3.635 \times 10^{-10} \quad \sigma_b = 0.0163476 \quad \chi^2 / (n-2) = 139.803$$

```
In[276]:= commitFit[{0.2008`, 0.3901`}, 139.80254205738402`];
```

High voltage

```

In[739]:= With[ {name = SystemDialogInput["FileOpen",
      {DataFileName, {"data files" -> {"*.dat", "*.mca"}, "all files" -> {"*"}}}}],
      If[ name != $Canceled,
        LoadFile[name]]
    ]

In[740]:= NRangeRemove /@ {1, 1, 17, 17};

In[741]:= With[{x = SetXRange[ LinearDataPlot[], Log -> False,
      Label -> "Set the X values for the range you wish to keep." ]},
      Print[x];

      XRangeKeep[Sequence @@ x]
    ]

{0.4148, 0.564946}

n= 9

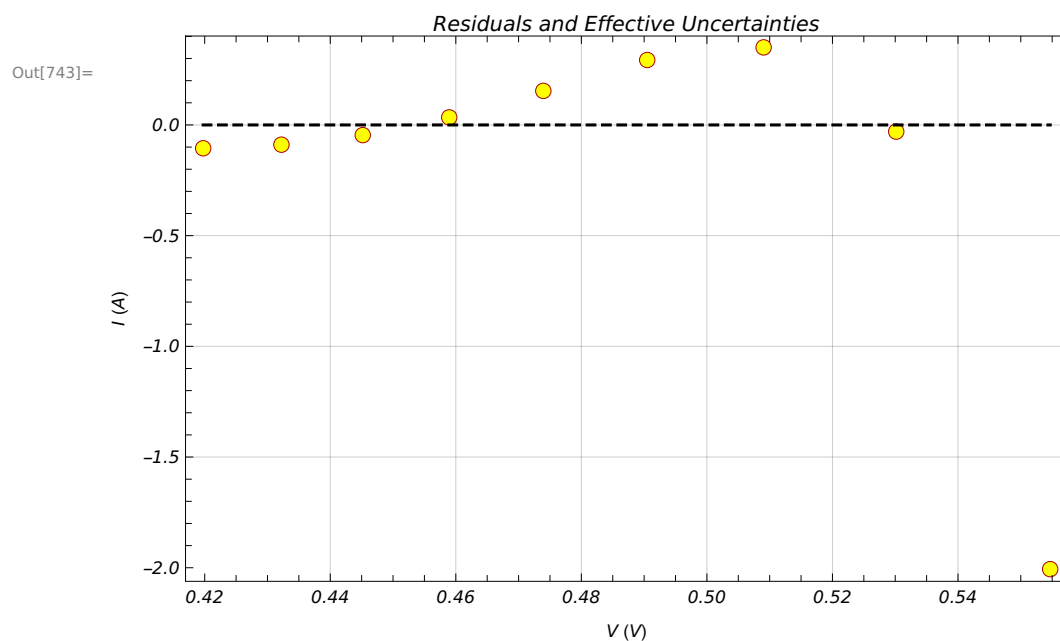
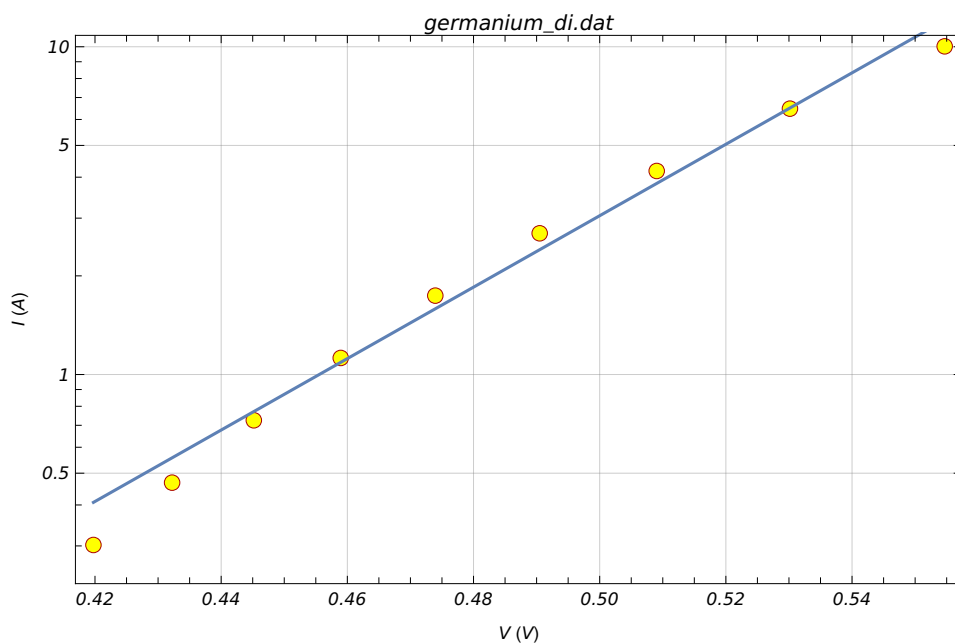
27 points removed.

In[742]:= DiodeFit[]

```



```
In[743]:= LogDifferencePlot[FrameLabel → {"V (V)", "I (A)"}]
```



$$y(x) = a \left(\exp[b x] - 1 \right)$$

$a =$	$b =$	
0.0000108504	25.0939	
$\sigma_a =$	$\sigma_b =$	$\chi^2 / (n-2) =$
3.02275×10^{-8}	0.00560288	45693.8

```
In[747]:= commitFit[{0.4148`, 0.5649458958333333`}, 45693.79129063999`];
```

```
In[*]:= (* We store the collected data in a separate dataset for silicon
         diode at room temp and re-initialize fitParam for further use. *)
         germaniumDI = fitParam;
```

```
In[750]:= fitParam = {};
```

Transistor - Room Temperature

Whole dataset (bad points removed)

```
In[287]:= With[ {name = SystemDialogInput["FileOpen",
      {DataFileName, {"data files" -> {"*.dat", "*.mca"}, "all files" -> {"*"}}}}],
  If[ name != $Canceled,
    LoadFile[name]]
]

In[288]:= NRangeRemove /@ {1, 1, 17, 17};

In[289]:= With[{x = SetXRange[ LinearDataPlot[], Log -> False,
  Label -> "Set the X values for the range you wish to keep." ]},
  Print[x];

  XRangeKeep[Sequence @@ x]
]

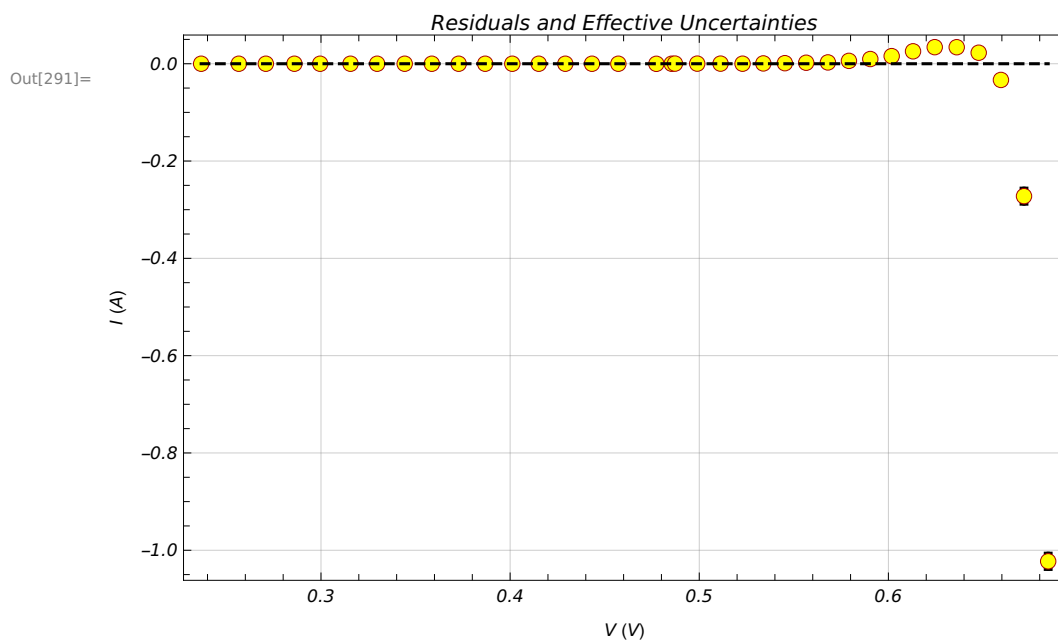
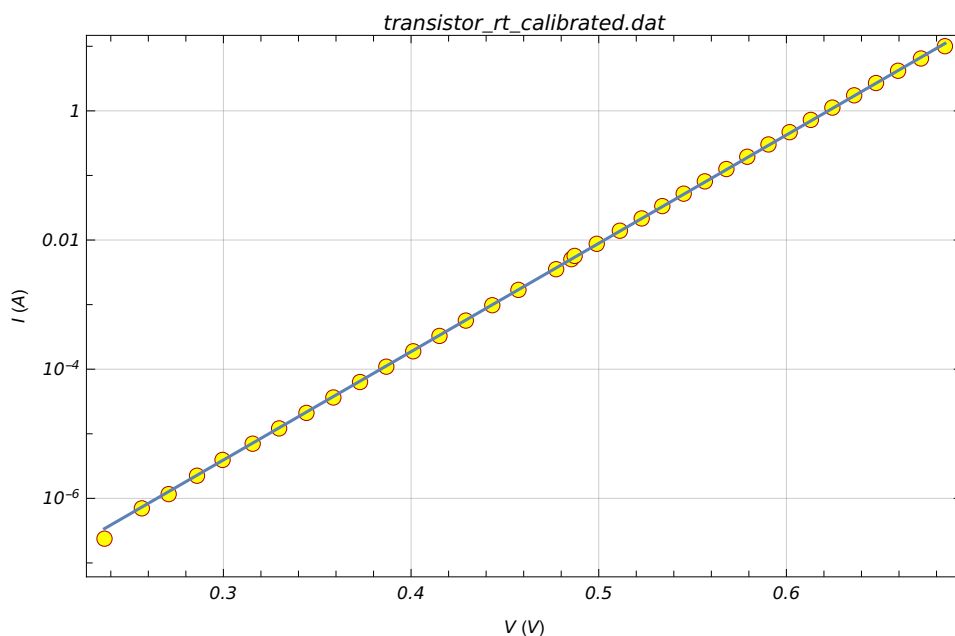
{0.22701, 0.693855}

n= 36

0 points removed.

In[290]:= DiodeFit[]
```

In[291]:= **LogDifferencePlot**[FrameLabel → {"V (V)", "I (A)"}]



$$y(x) = a \left(\text{Exp}[b x] - 1 \right)$$

$$a = 3.64202 \times 10^{-11} \quad b = 38.6257$$

$$\sigma_a = 1.15854 \times 10^{-13} \quad \sigma_b = 0.00530517 \quad \chi^2 / (n-2) = 204.849$$

In[292]:= **commitFit**[{0.22701010416666667`, 0.6938548958333333`}, 204.84853397967123`];

Low voltage

```

In[293]:= With[ {name = SystemDialogInput["FileOpen",
      {DataFileName, {"data files" -> {"*.dat", "*.mca"}, "all files" -> {"*"}}}}],
      If[ name != $Canceled,
        LoadFile[name]]
    ]

In[294]:= NRangeRemove /@ {1, 1, 17, 17};

In[295]:= With[{x = SetXRange[ LinearDataPlot[], Log -> False,
      Label -> "Set the X values for the range you wish to keep." ]},
      Print[x];

      XRangeKeep[Sequence @@ x]
    ]

{0.22701, 0.3649}

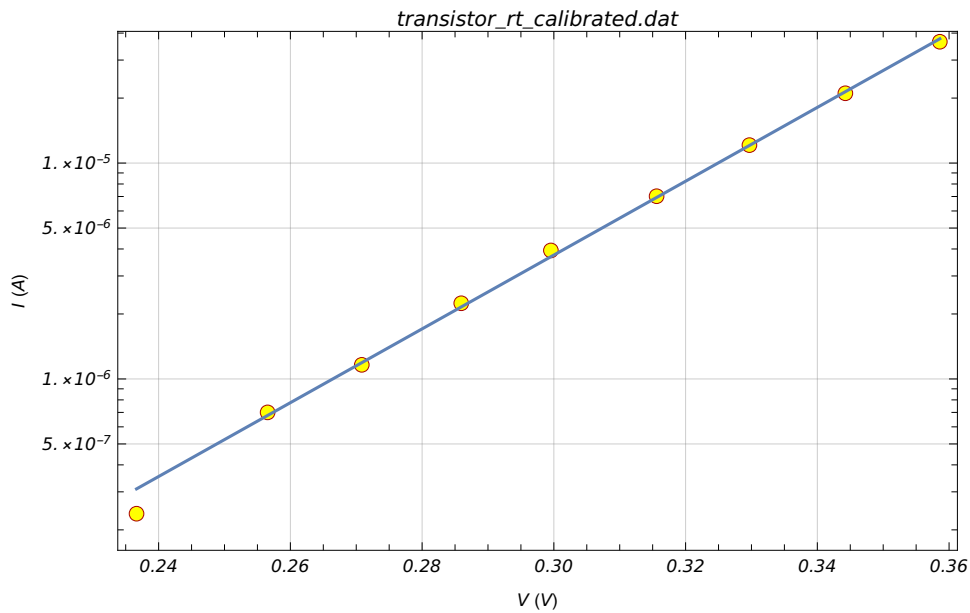
n= 9

27 points removed.

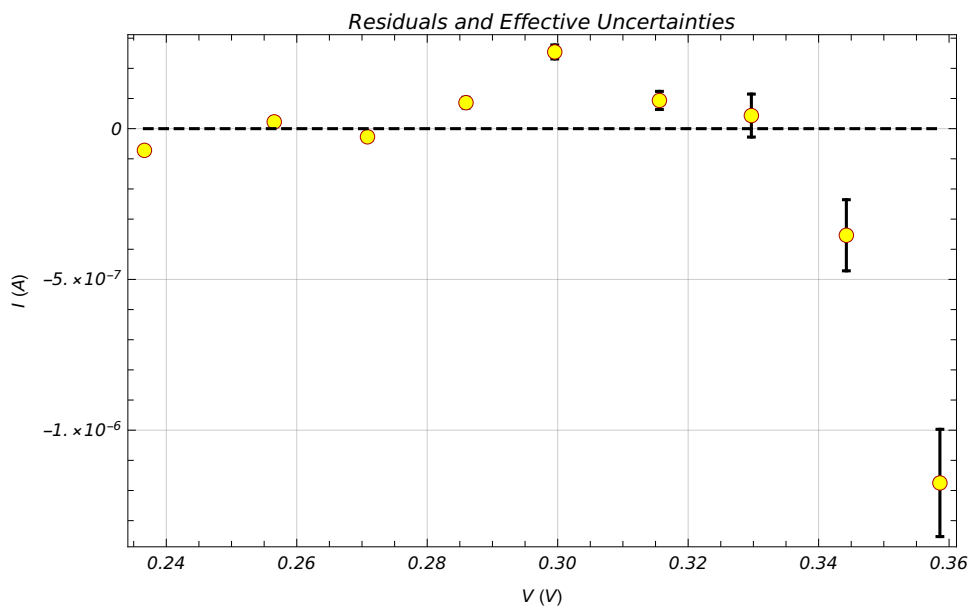
In[296]:= DiodeFit[]

```

In[297]:= `LogDifferencePlot[FrameLabel → {"V (V)", "I (A)"}]`



Out[297]=



$$y(x) = a \left(\exp[b x] - 1 \right)$$

$$a = 2.78634 \times 10^{-11} \quad b = 39.3656$$

$$\sigma_a = 6.63776 \times 10^{-13} \quad \sigma_b = 0.0734669 \quad \chi^2 / (n-2) = 86.5428$$

In[298]:= `commitFit[{0.22701010416666667, 0.3649}, 86.54277146677468];`

Medium voltage

```

In[304]:= With[ {name = SystemDialogInput["FileOpen",
      {DataFileName, {"data files" -> {"*.dat", "*.mca"}, "all files" -> {"*"}}}}],
      If[ name != $Canceled,
        LoadFile[name]]
    ]

In[305]:= NRangeRemove /@ {1, 1, 17, 17};

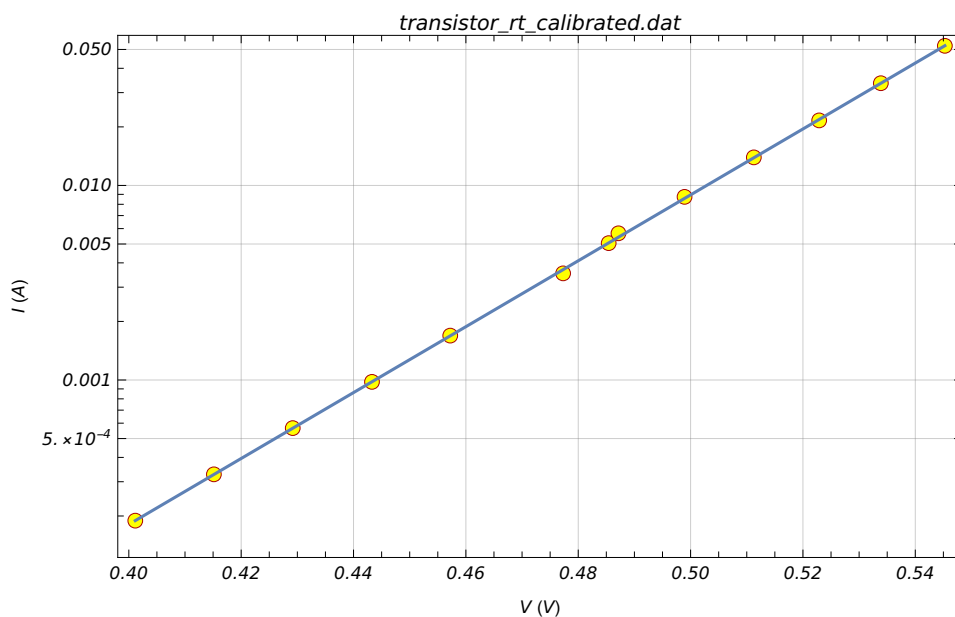
In[306]:= With[{x = SetXRange[ LinearDataPlot[], Log -> False,
      Label -> "Set the X values for the range you wish to keep." ]},
      Print[x];

      XRangeKeep[Sequence @@ x]
    ]
{0.3976, 0.5514}
n= 13
23 points removed.

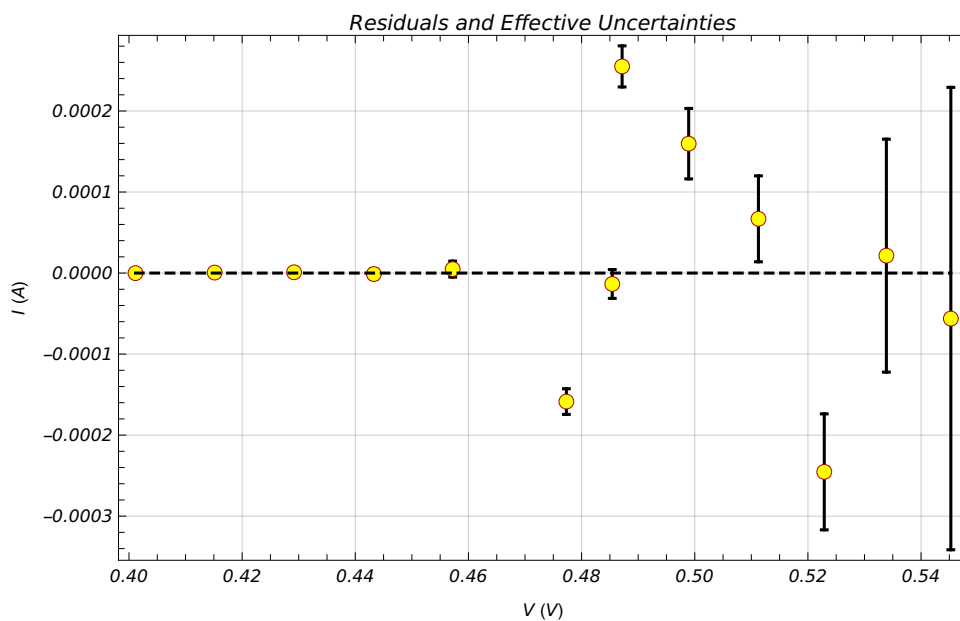
In[307]:= DiodeFit[]

```

In[308]:= `LogDifferencePlot[FrameLabel → {"V (V)", "I (A)"}]`



Out[308]=



$$y(x) = a \left(\exp[b x] - 1 \right)$$

$$a = 3.04044 \times 10^{-11} \quad b = 38.9992$$

$$\sigma_a = 4.3288 \times 10^{-13} \quad \sigma_b = 0.0291436 \quad \chi^2 / (n-2) = 20.852$$

In[309]:= `commitFit[{0.39760000000000006`, 0.5514000000000001`}, 20.85201748541172`];`

High voltage

```

In[310]:= With[ {name = SystemDialogInput["FileOpen",
      {DataFileName, {"data files" -> {"*.dat", "*.mca"}, "all files" -> {"*"}}}}],
      If[ name != $Canceled,
        LoadFile[name]]
    ]

In[311]:= NRangeRemove /@ {1, 1, 17, 17};

In[312]:= With[{x = SetXRange[ LinearDataPlot[], Log -> False,
      Label -> "Set the X values for the range you wish to keep." ]},
      Print[x];

      XRangeKeep[Sequence @@ x]
    ]

{0.5629, 0.693855}

n= 11

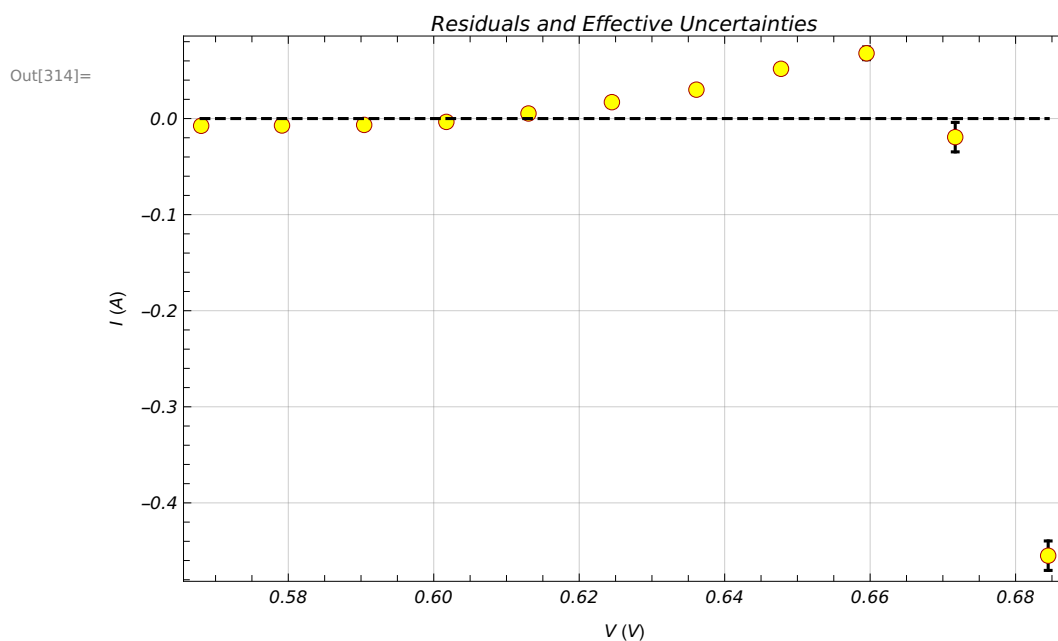
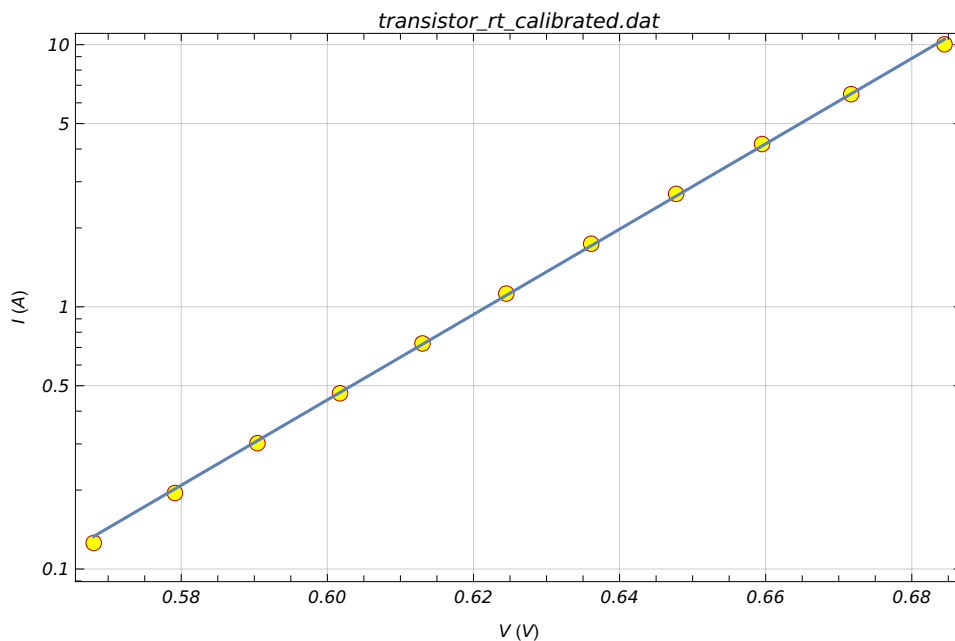
25 points removed.

In[313]:= DiodeFit[]

```



```
In[314]:= LogDifferencePlot[FrameLabel → {"V (V)", "I (A)"}]
```



$$y(x) = a \left(\exp[b x] - 1 \right)$$

$$a = 7.5261 \times 10^{-11} \quad b = 37.4882$$

$$\sigma_a = 8.96097 \times 10^{-13} \quad \sigma_b = 0.0185673 \quad \chi^2 / (n-2) = 222.001$$

```
In[315]:= commitFit[{0.5629000000000001`, 0.6938548958333333`}, 222.0012998180222`];
```

```
(* We store the collected data in a separate dataset for silicon
   diode at room temp and re-initialize fitParam for further use. *)
transistorRT = fitParam;
```

```
fitParam = {};
```

Transistor - Dry Ice Temperature

Whole dataset (bad points removed)

```
In[319]:= With[ {name = SystemDialogInput["FileOpen",
      {DataFileName, {"data files" -> {"*.dat", "*.mca"}, "all files" -> {"*"}}}]},
  If[ name != $Canceled,
    LoadFile[name]]
]

In[320]:= NRangeRemove /@ {1, 1, 17, 17};

In[321]:= With[{x = SetXRange[ LinearDataPlot[], Log -> False,
  Label -> "Set the X values for the range you wish to keep." ]},
  Print[x];

  XRangeKeep[Sequence @@ x]
]

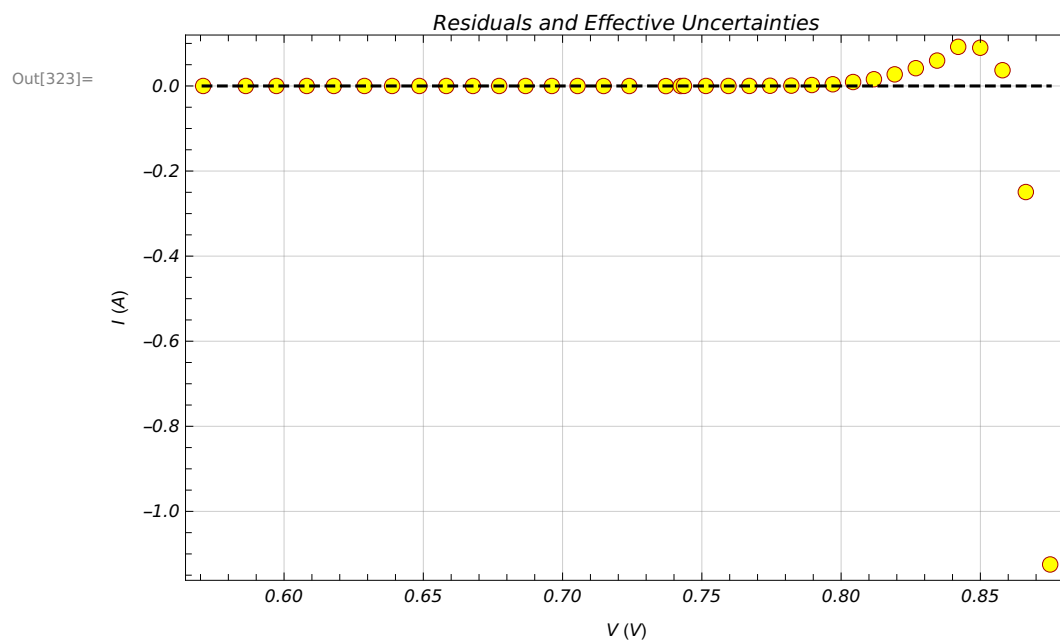
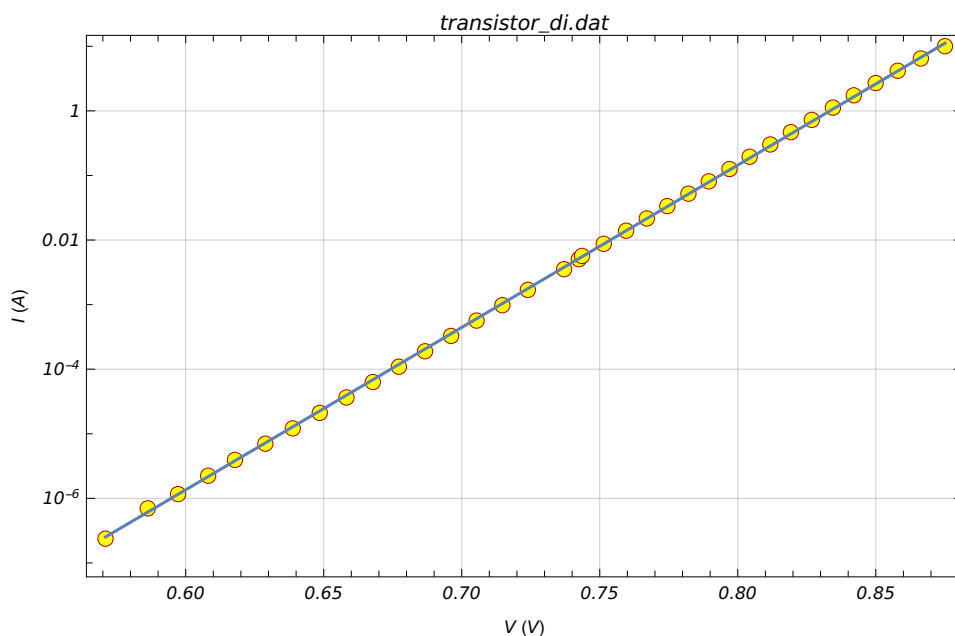
{0.564039, 0.881428}

n= 36

0 points removed.

In[322]:= DiodeFit[]
```

In[323]:= `LogDifferencePlot[FrameLabel → {"V (V)", "I (A)"}]`



$$y(x) = a \left(\exp[b x] - 1 \right)$$

$$a = 1.11695 \times 10^{-21} \quad b = 57.8879$$

$$\sigma_a = 7.44262 \times 10^{-24} \quad \sigma_b = 0.00787585 \quad \chi^2 / (n-2) = 578.877$$

In[324]:= `commitFit[{0.5640392291666667`, 0.8814277708333333`}, 578.877313412121`];`

Low voltage

```

In[330]:= With[ {name = SystemDialogInput["FileOpen",
      {DataFileName, {"data files" -> {"*.dat", "*.mca"}, "all files" -> {"*"}}}}],
      If[ name != $Canceled,
        LoadFile[name]]
    ]

In[331]:= NRangeRemove /@ {1, 1, 17, 17};

In[332]:= With[{x = SetXRange[ LinearDataPlot[], Log -> False,
      Label -> "Set the X values for the range you wish to keep." ]},
      Print[x];

      XRangeKeep[Sequence @@ x]
    ]

{0.5809, 0.6621}

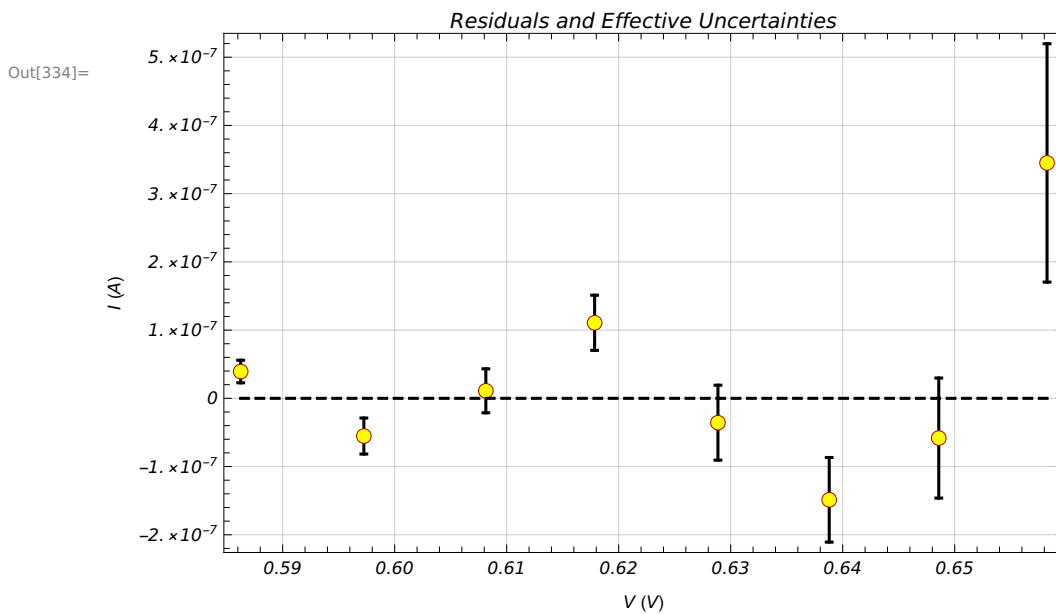
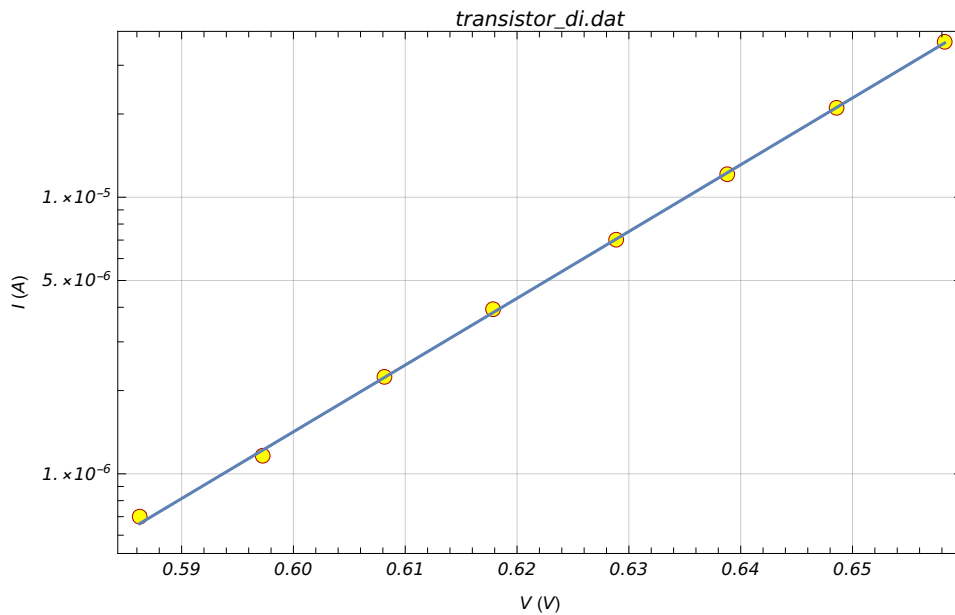
n= 8

28 points removed.

In[333]:= DiodeFit[]

```

In[334]:= `LogDifferencePlot[FrameLabel → {"V (V)", "I (A)"}]`



$y(x) = a \left(\text{Exp}[b x] - 1 \right)$
 $a = 4.67296 \times 10^{-21}$ $b = 55.578$
 $\sigma_a = 5.1192 \times 10^{-22}$ $\sigma_b = 0.163026$ $\chi^2 / (n-2) = 4.69663$

In[335]:= `commitFit[{0.5809000000000001, 0.6621}, 4.696633498979921];`

Medium voltage

```

In[340]:= With[ {name = SystemDialogInput["FileOpen",
      {DataFileName, {"data files" -> {"*.dat", "*.mca"}, "all files" -> {"*"}}}}],
      If[ name != $Canceled,
        LoadFile[name]]
    ]

In[341]:= NRangeRemove /@ {1, 1, 17, 17};

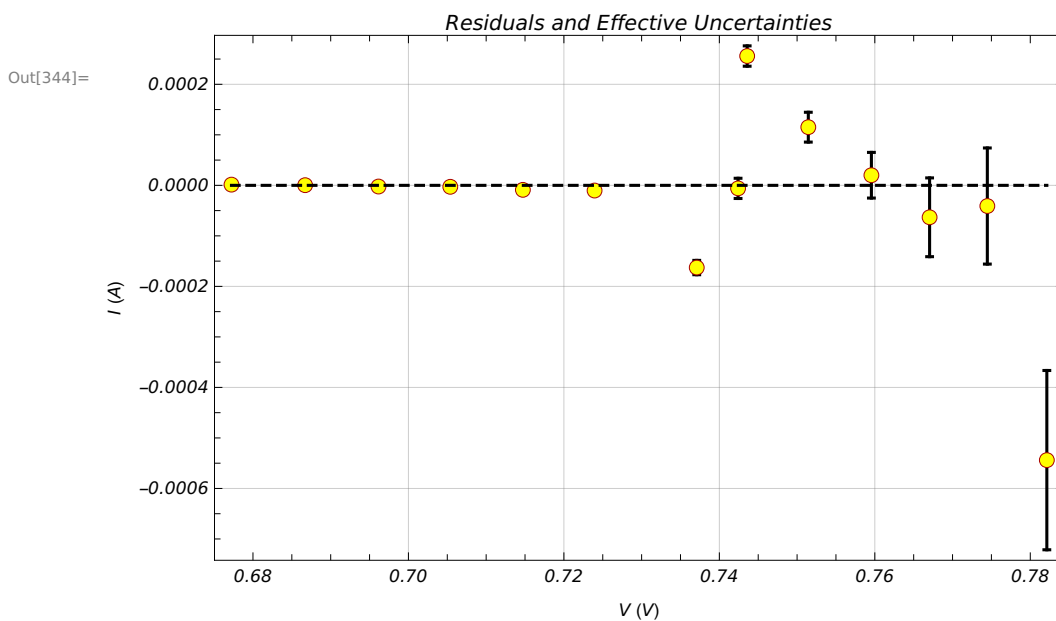
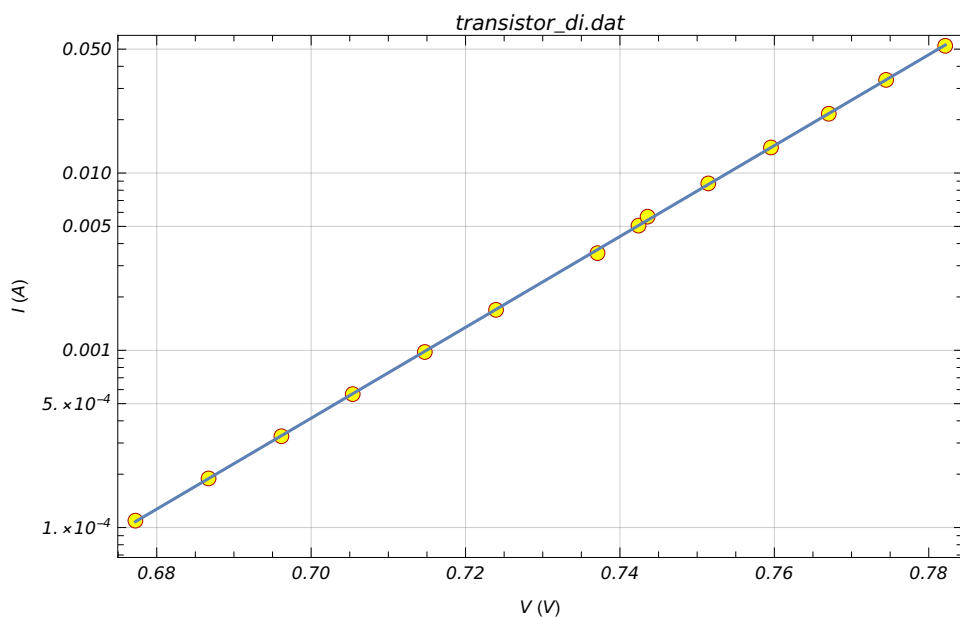
In[342]:= With[{x = SetXRange[ LinearDataPlot[], Log -> False,
      Label -> "Set the X values for the range you wish to keep." ]},
      Print[x];

      XRangeKeep[Sequence @@ x]
    ]
    {0.6731, 0.786}
    n= 14
    22 points removed.

In[343]:= DiodeFit[]

```

In[344]:= `LogDifferencePlot[FrameLabel -> {"V (V)", "I (A)"}]`



$$y(x) = a \left(\exp[b x] - 1 \right)$$

$$a = 4.71352 \times 10^{-22} \quad b = 59.0236$$

$$\sigma_a = 1.28114 \times 10^{-23} \quad \sigma_b = 0.0360829 \quad \chi^2 / (n-2) = 27.7266$$

In[345]:= `commitFit[{0.6731`, 0.786`}, 27.72657449600054`];`

High voltage

```

In[346]:= With[ {name = SystemDialogInput["FileOpen",
      {DataFileName, {"data files" -> {"*.dat", "*.mca"}, "all files" -> {"*"}}}}],
      If[ name != $Canceled,
        LoadFile[name]]
    ]

In[347]:= NRangeRemove /@ {1, 1, 17, 17};

In[348]:= With[{x = SetXRange[ LinearDataPlot[], Log -> False,
      Label -> "Set the X values for the range you wish to keep." ]},
      Print[x];

      XRangeKeep[Sequence @@ x]
    ]

{0.7782, 0.881428}

n= 13

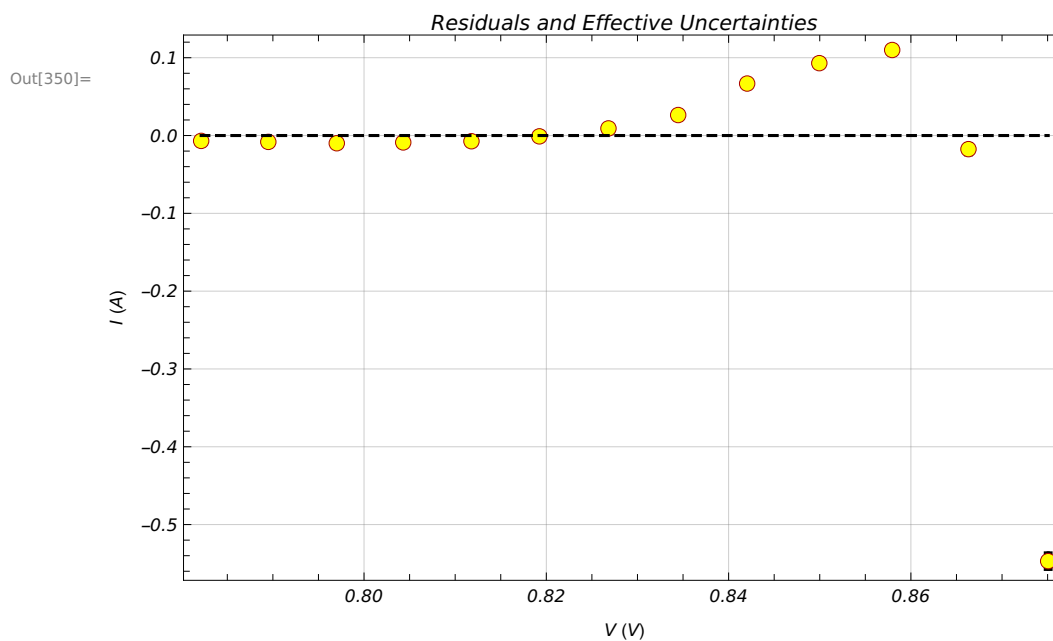
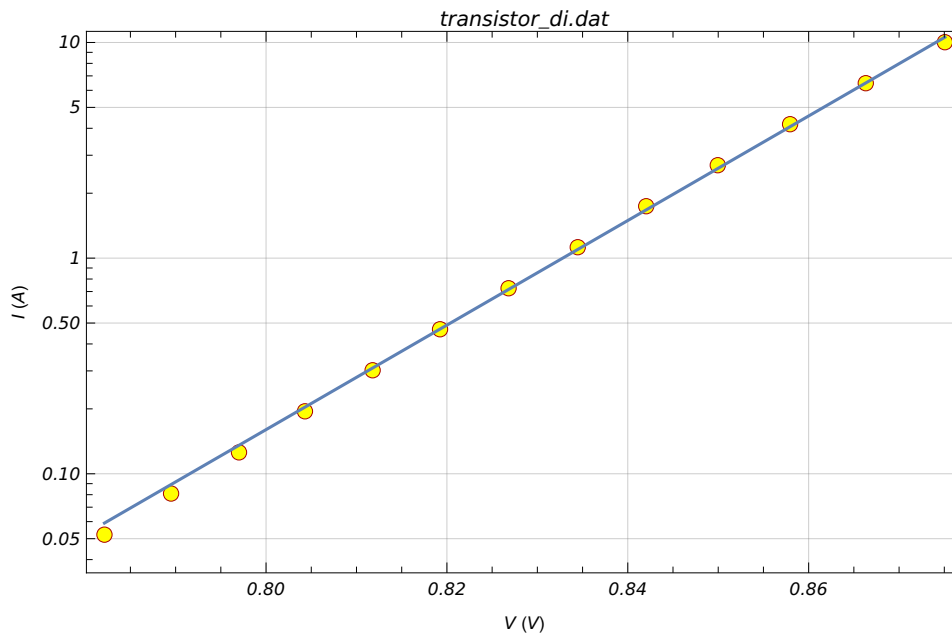
23 points removed.

In[349]:= DiodeFit[]

```



```
In[350]:= LogDifferencePlot[FrameLabel → {"V (V)", "I (A)"}]
```



$$y(x) = a \left(\exp[b x] - 1 \right)$$

$a = 6.48147 \times 10^{-21}$	$b = 55.8177$
$\sigma_a = 4.3966 \times 10^{-23}$	$\sigma_b = 0.15547$ $\chi^2 / (n-2) = 702.496$

```
In[351]:= commitFit[{0.7782`, 0.8814277708333333`}, 702.4964280713867`];
```

```
In[352]:= (* We store the collected data in a separate dataset for silicon
diode at room temp and re-initialize fitParam for further use. *)
transistorDI = fitParam;
```

```
In[353]:= fitParam = {};
```

Exporting fit data for safekeeping

```
In[752]:= paramList = {"siliconRT", "siliconDI",
  "germaniumRT", "germaniumDI", "transistorRT", "transistorDI"};
```

```
In[753]:= Export[StringJoin[#, ".m"], ToExpression[#]] & /@ paramList;
```

Processing fit parameter data

```
In[846]:= (* We construct a list of diode parameters ( $\eta$  and  $I_R$ )
  from the fit parameter list for each diode configuration. This
  list has structure {region,  $I_R$ ,  $\sigma I_R$ ,  $\eta$ ,  $\sigma \eta$ ,  $\tilde{\chi}^2$ }. *)
qe = 1.6021766 * 10-19 (* C *);
kb = 1.3806485 * 10-23 (* J K-1 *);
t = 298 (* K *);
processed[dataset_] := Table[{dataset[[i]][[1]],
  10-3 dataset[[i]][[2]], 10-3 dataset[[i]][[3]],  $\frac{qe}{kb t \text{ dataset}[[i]][[4]]}$ ,
   $\frac{qe \text{ dataset}[[i]][[5]]}{kb t (\text{dataset}[[i]][[4]])^2}$ , dataset[[i]][[6]]}, {i, 1, Length[dataset]}];
present[dataset_, x_] := Table[{NumberForm[dataset[[i]][[1]], 4],
  NumberForm[10x dataset[[i]][[2]],
    {8, -RealDigits[10x dataset[[i]][[3]]][[2]] + 2}], NumberForm[
    10x dataset[[i]][[3]], {8, -RealDigits[10x dataset[[i]][[3]]][[2]] + 2}],
  NumberForm[dataset[[i]][[4]], {8, -RealDigits[dataset[[i]][[5]]][[2]] + 2}],
  NumberForm[dataset[[i]][[5]], {8, -RealDigits[dataset[[i]][[5]]][[2]] + 2}],
  Round[dataset[[i]][[6]]}], {i, 1, Length[dataset]}];

In[851]:= ClearAll["siliconRT2", "siliconDI2", "germaniumRT2",
  "germaniumDI2", "transistorRT2", "transistorDI2"];

In[852]:= For[i = 1, i ≤ Length[paramList], i++,
  Evaluate[Symbol[StringJoin[paramList[[i]], "2"]]] =
  processed[ToExpression[paramList[[i]]]];

In[866]:= siliconRTpresent =
  Join[{{"Voltage Range (V)", "IR (μA)", "σIR (nA)", "η", "ση", "χ2"}}},
  present[siliconRT2, 9]];

In[867]:= siliconDIpresent =
  Join[{{"Voltage Range (V)", "IR (pA)", "σIR (fA)", "η", "ση", "χ2"}}},
  present[siliconDI2, 15]];
```

```
In[868]:= germaniumRTpresent =
  Join[{{"Voltage Range (V)", "IR (mA)", "σIR (μA)", "η", "ση", "χ̃2"}}],
  present[germaniumRT2, 6]];
```

```
In[869]:= germaniumDIpresent =
  Join[{{"Voltage Range (V)", "IR (nA)", "σIR (pA)", "η", "ση", "χ̃2"}}],
  present[germaniumDI2, 12]];
```

```
In[870]:= transistorRTpresent =
  Join[{{"Voltage Range (V)", "IR (pA)", "σIR (fA)", "η", "ση", "χ̃2"}}],
  present[transistorRT2, 15]];
```

```
In[871]:= transistorDIpresent =
  Join[{{"Voltage Range (V)", "IR (yA)", "σIR (zA)", "η", "ση", "χ̃2"}}],
  present[transistorDI2, 24]];
```

Processed parameter data

```
In[543]:= grid[data_] := Grid[data, Alignment → Left, Spacings → {2, 1}, Frame → All,
  ItemStyle → "Text", Background → {{Gray, None}, {LightGray, None}}];
```

Silicon Diode - Room temperature

```
In[872]:= grid[siliconRTpresent]
```

```
Out[872]=
```

Voltage Range (V)	I _R (μA)	σ _{I_R} (nA)	η	σ _η	χ̃ ²
{-0.01543, 0.756}	4.3550	0.0047	1.95420	0.00018	513
{-0.01543, 0.1484}	3.560	0.022	1.8069	0.0046	170
{0.206, 0.5024}	3.999	0.015	1.93658	0.00098	41
{0.501, 0.756}	6.564	0.029	2.01676	0.00071	626

Silicon Diode - Dry ice temperature

```
In[873]:= grid[siliconDIpresent]
```

```
Out[873]=
```

Voltage Range (V)	I _R (pA)	σ _{I_R} (fA)	η	σ _η	χ̃ ²
{0.3231, 0.9117}	14.030	0.036	1.27954	0.00014	453
{0.3231, 0.5102}	5.304	0.089	1.1961	0.0014	93
{0.5082, 0.7202}	21.94	0.22	1.30992	0.00070	22
{0.7176, 0.9119}	11.92	0.12	1.27156	0.00051	785

Germanium Diode - Room temperature

In[874]:= `grid[germaniumRTpresent]`

	Voltage Range (V)	I_R (mA)	σ_{I_R} (μ A)	η	σ_η	$\tilde{\chi}^2$
	{-0.008776, 0.4179}	4.0369	0.0058	1.98973	0.00045	10171
Out[874]=	{-0.008776, 0.0908}	0.7776	0.0072	1.2841	0.0053	16
	{0.104, 0.2466}	1.8845	0.0075	1.6624	0.0015	412
	{0.2473, 0.4179}	9.782	0.021	2.28325	0.00080	4169

Germanium Diode - Dry ice temperature

In[875]:= `grid[germaniumDIpresent]`

	Voltage Range (V)	I_R (nA)	σ_{I_R} (pA)	η	σ_η	$\tilde{\chi}^2$
	{0.0528, 0.5649}	475.9	1.2	1.23581	0.00022	43187
Out[875]=	{0.0528, 0.1999}	20.85	0.50	0.9420	0.0032	5
	{0.2008, 0.3901}	66.20	0.36	1.06489	0.00048	140
	{0.4148, 0.5649}	10850.	30.	1.55183	0.00035	45694

Transistor - Room temperature

In[877]:= `grid[transistorRTpresent]`

	Voltage Range (V)	I_R (pA)	σ_{I_R} (fA)	η	σ_η	$\tilde{\chi}^2$
	{0.227, 0.6939}	36.42	0.12	1.00817	0.00014	205
Out[877]=	{0.227, 0.3649}	27.86	0.66	0.9892	0.0018	87
	{0.3976, 0.5514}	30.40	0.43	0.99852	0.00075	21
	{0.5629, 0.6939}	75.26	0.90	1.03876	0.00051	222

Transistor - Dry ice temperature

In[878]:= `grid[transistorDIpresent]`

	Voltage Range (V)	I_R (yA)	σ_{I_R} (zA)	η	σ_η	$\tilde{\chi}^2$
	{0.564, 0.8814}	1.1170	0.0074	0.672703	0.000092	579
Out[878]=	{0.5809, 0.6621}	4.67	0.51	0.7007	0.0021	5
	{0.6731, 0.786}	0.471	0.013	0.65976	0.00040	28
	{0.7782, 0.8814}	6.481	0.044	0.6977	0.0019	702

Analysis of the PN junction theory

Fit residuals

We observe that our fits share the same structure in the fit residuals, indicating that the PN junction theory presented does not completely explain the I-V behavior of PN-junction diodes. This structure is easy to observe in the plots above: residuals start out small, then increase in the positive direction (positive residuals increasing in magnitude), then decrease in magnitude, cross the zero-residual line, and dramatically increase in the negative direction (negative residuals increasing in magnitude). This indicates either that our theory must contain a correction term we have not accounted for, and/or our assumption that the ideality coefficient η is a constant over a given I-V curve in fact does not adequately hold over our measured regions.

Residuals over different regions

Following the observations above, we attempted several fits for each dataset - for each diode at both temperature (room temperature and dry ice temperature), we perform a fit over low-current, medium-current, and high-current regions. From the fit parameters, we can obtain I_R and η , the results of which are shown in the tables above for all diodes, temperatures, and current regions, along with the corresponding $\tilde{\chi}^2$ of the fit.

We observe that the residuals maintain the general structure described above over all fitted regions. Furthermore, we observe a significant variation in goodness-of-fit ($\tilde{\chi}^2$) over different regions of the same IV-curve. This indicates that there must be a correction term to our model, and that this correction term cannot present itself *only* as a variation in η across the IV-curve (if it were only a variation in η , we would expect the goodness-of-fit of our data to the model to always improve when we fit over smaller subsections of our data, and this is not consistently observed in the tables above for the high-current fits, indicating the presence of a correction term not in η that becomes significant at high currents). However, the significant differences in $\tilde{\chi}^2$ and in our best estimates for η using the fits over subsections of each IV-curve indicate that the correction term does include a variation of η over the IV-curve.

Observations from fits

The different diodes differ in their behavior over different current and temperature ranges. The best fits are obtained using the germanium diode and the transistor at dry ice temperatures, over the low current range. The germanium diode at dry ice temperature seems to fit the model relatively well when fit over subsections of the IV-curve, but has a much worse fit over the entire dataset. This indicates that η is not approximately constant as assumed for this configuration, and that the correction term to the model is dominated by the variation of η across the IV-curve for this configuration. The transistor at dry ice temperature has the same issue, but much less severe. It is therefore the dataset that fits the model the most closely. The transistor at room temperature fits the model best over the whole dataset, but it

is not a very good fit ($\tilde{\chi}^2 = 205$).

With the exception of the silicon diode at both temperatures and the transistor at room temperature, we observe that the data fits the model best at low-current, worsening as current increases. This general trend may be caused by series resistance becoming apparent at high-currents.

Series resistance

At large currents, we expect a voltage drop to occur due to the resistance between each of the diode's connecting leads. This causes a current-dependent decrease in the voltage across the diode, such that at high currents the IV-curve for the diode diverges from and lies below the IV-curve predicted by the theory, with divergence from the theory increasing with current. Now, recall that the diode equation predicts current across the diode to vary exponentially with the inverse of temperature, T . Therefore, assuming resistance changes only slowly with temperature, we expect larger currents at lower temperatures for a given voltage to result in series resistance to have a greater effect on the cold data than on the room temperature data.

Below is an interactive plot where we can observe the effects of series resistance on the IV-curves predicted by the theory, for a diode with $I_R = 10^{-9} A$ and $\eta = 1$. We obtain the plot by numerically solving the implicit equation resulting from applying Kirchoff's Voltage Law to a voltage drop across a diode in series with a resistor, whose resistance can be varied to observe the effects on the IV-curves.

```
In[884]:= ClearAll[t, i]

In[885]:= iR = 10^-9;
eta = 1;

In[887]:= i[iR_, η_, v_, t_] := iR (Exp[ $\frac{q e v}{\eta k b t}$ ] - 1);

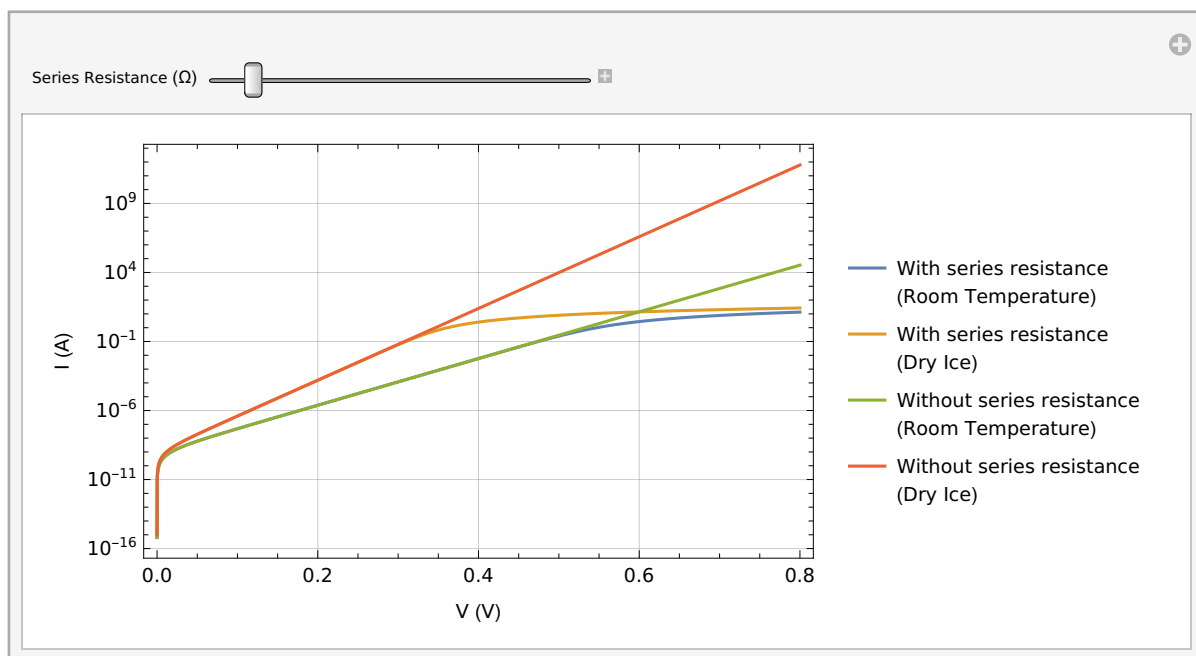
In[888]:= iRes[iR_, η_, v_, t_, r_] := i[iR, η, vDiode, t] /.
FindRoot[v == i[iR, η, vDiode, t] r + vDiode, {vDiode, v}][[1]] // Quiet
```

```

In[955]:= Manipulate[LogPlot[{iRes[iR, eta, v, 298, r],
    iRes[iR, eta, v, 194, r], i[iR, eta, v, 298], i[iR, eta, v, 194]}], {v, 0, 0.8},
    FrameLabel -> {"V (V)", "I (A)"}, PlotLegends -> {"With series resistance
(Room Temperature)", "With series resistance
(Dry Ice)", "Without series resistance
(Room Temperature)", "Without series resistance
(Dry Ice)"}, PlotRange -> All, ImageSize -> 400,
    LabelStyle -> {FontSize -> 10}], {{r, 0, "Series Resistance ( $\Omega$ )", 0, 0.2}}]

```

Out[955]=



Indeed, in the plot above, we can observe a series resistance effect with the characteristics proposed above at high currents, with a greater effect on the cold IV-curve than on the room temperature IV-curve (the onset of significant divergence from the diode equation occurs at lower voltages in the cold IV-curve).

Now, observe that the data from the fits presented above shows significantly worse fits for high-current data, with the high-current fits worsening at dry-ice temperature. From the above, this is exactly what we would expect of data containing evidence of series resistance being fit against the diode equation. This indicates that the correction terms to our diode equation must account for series resistance, and as stated before, variability of η across the IV-curve.

Determining E_g

Solving equation (13.2) from the lab manual for two different temperatures T_1, T_2 , we obtain an expression for E_g in units of eV:

$$E_g = \frac{k_B}{q_e} \frac{(\eta_1 \eta_2)(T_1 T_2)}{(T_2 \eta_2 - T_1 \eta_1)} \text{Log}\left[\frac{I_{R_1}}{I_{R_2}}\right].$$

In[790]:= << SimpleErrorPropagation`

In[791]:= ? PropagateUncertainties

PropagateUncertainties[func, vars] propagates uncertainties in variables listed in vars = {variable1, variable2,...} and returns the propagated uncertainty in func. func must necessarily be differentiable with respect to all variables in vars, and the uncertainties in variables in vars must be independent.

It will return an algebraic expression in terms of the variables

in vars, with uncertainty in some variable denoted by sigmaVariable.

It can be used either by providing an algebraic expression, then substituting values for the variables and uncertainties in a subsequent operation, or simply by assigning values and uncertainties to each variable using the naming conventions mentioned. In the latter case, it will be necessary to localize the variables in vars using Module or Block.

Note: Loading SimpleErrorPropagation` clears any variables named 'variance', 'varianceList' or 'PropagateUncertainties' due to function and subfunction names in the Package.

In[792]:= eg[t1_, t2_, ir1_, ir2_, eta1_, eta2_] := $\frac{k_B}{q_e} \frac{(\eta_1 \eta_2)(t_1 t_2)}{(t_2 \eta_2 - t_1 \eta_1)} \text{Log}\left[\frac{ir_2}{ir_1}\right];$

In[794]:= PropagateUncertainties[
eg[t1, t2, ir1, ir2, eta1, eta2], {eta1, eta2, ir1, ir2}] // Simplify

Out[794]=
$$\sqrt{\left(\frac{1}{ir_1^2 ir_2^2 (\eta_1 t_1 - 1. \eta_2 t_2)^4} t_1^2 t_2^2 \left(\eta_1^2 \eta_2^2 (\eta_1^2 (7.42584 \times 10^{-9} ir_2^2 \sigma_{ir_1^2} + 7.42584 \times 10^{-9} ir_1^2 \sigma_{ir_2^2}) t_1^2 + \right. \right. \right. \\ \left. \eta_1 \eta_2 (-1.48517 \times 10^{-8} ir_2^2 \sigma_{ir_1^2} - 1.48517 \times 10^{-8} ir_1^2 \sigma_{ir_2^2}) t_1 t_2 + \right. \\ \left. \eta_2^2 (7.42584 \times 10^{-9} ir_2^2 \sigma_{ir_1^2} + 7.42584 \times 10^{-9} ir_1^2 \sigma_{ir_2^2}) t_2^2 \right) + \\ \left. ir_1^2 ir_2^2 (7.42584 \times 10^{-9} \eta_1^4 \sigma_{\eta_2^2} t_1^2 + 7.42584 \times 10^{-9} \eta_2^4 \sigma_{\eta_1^2} t_2^2) \right) \text{Log}\left[\frac{ir_2}{ir_1}\right]^2 \right)}$$


```
In[795]:= egUnc[t1_, t2_, ir1_, sigmaIr1_, ir2_,
  sigmaIr2_, eta1_, sigmaEta1_, eta2_, sigmaEta2_] :=
  {eg[t1, t2, ir1, ir2, eta1, eta2],  $\sqrt{\left(\frac{1}{ir1^2 ir2^2 (eta1 t1 - 1. \eta2 t2)^4} \right.}$ 
     $t1^2 t2^2 \left( eta1^2 eta2^2 (eta1^2 (7.425838191741328 \cdot 10^{-9} ir2^2 sigmaIr1^2 + \right.$ 
       $7.425838191741328 \cdot 10^{-9} ir1^2 sigmaIr2^2) t1^2 + eta1 eta2$ 
       $(-1.4851676383482656 \cdot 10^{-8} ir2^2 sigmaIr1^2 - 1.4851676383482656 \cdot 10^{-8}$ 
       $ir1^2 sigmaIr2^2) t1 t2 + eta2^2 (7.425838191741328 \cdot 10^{-9} ir2^2 sigmaIr1^2 +$ 
       $7.425838191741328 \cdot 10^{-9} ir1^2 sigmaIr2^2) t2^2) +$ 
       $ir1^2 ir2^2 (7.425838191741328 \cdot 10^{-9} eta1^4 sigmaEta2^2 t1^2 +$ 
       $7.425838191741328 \cdot 10^{-9} eta2^4 sigmaEta1^2 t2^2) \log\left[\frac{ir2}{ir1}\right]^2 \left. \right)}$ };
```

```
In[798]:= diodeList = {"siliconRT2", "siliconDI2",
  "germaniumRT2", "germaniumDI2", "transistorRT2", "transistorDI2"};
```

```
In[809]:= (* List of best fit estimates of diode parameters,
  ordered as given by diodeList above. *)
```

```
In[879]:= bestFits = Flatten[
  Table[
    Select[
      Evaluate[
        Symbol[
          diodeList[[i]]],
        #[[6]] == Min[
          Evaluate[
            Symbol[
              diodeList[[i]]][[All, 6]]
            &],
        {i, 1, Length[diodeList]}], 1
  ];
```

```
In[921]:= egPresent = {{}, {}, {}};
egPresent[[1]] = Join[{"Silicon Diode"}, egList[[1]]];
egPresent[[2]] = Join[{"Germanium Diode"}, egList[[2]]];
egPresent[[3]] = Join[{"Transistor"}, egList[[3]]];
```

```
In[933]:= grid[egPresent]
```

```
Out[933]=
```

Diode Type	E_g (eV)	σ_{E_g} (eV)
Silicon Diode	0.47692	0.00065
Germanium Diode	0.3194	0.0025
Transistor	0.4904	0.0036

We observe large discrepancies between our estimates above and the known semiconductor gap energies of 1.12 eV for silicon and 0.67 eV for germanium. This could be due to a variety of factors, including the stated variability of η across the IV-curve which we have neglected in our analysis, imperfections in the PN-junctions of our diode, ohmic heating in the diode, undetected systematic errors in the apparatus, or human error during calibration.

Limitations of diode equation

The idealized one-dimensional model of the diode neglects effects such as internal resistance of the diode, capacitance between the two sides of the depletion layer, band gap shift due to doping.