GAMs for Foraging Whales

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Load libraries

```
library(tidyverse)
library(mgcv)
library(corrplot)
library(geoR)
library(here)
```

Research question:

What environmental variables characterize sperm whale habitat?

Hypothesis: Sperm whales are found in deep, productive offshore waters.

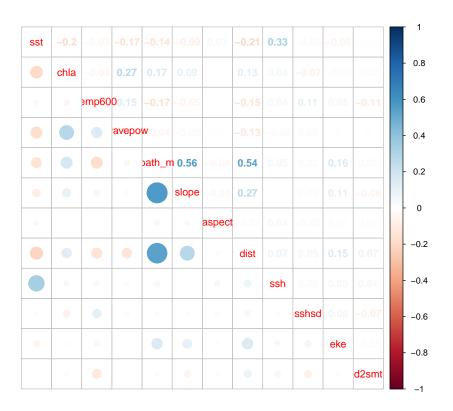
Load universal variables

```
# Values used for file and directory names
survey = "AllSurveys"
gridsize = 25
loctype = "Combined"
loctype2 = "Comb"
```

Load data from 'models/data' folder

Check correlation of covariates

```
require(corrplot)
corrplot.mixed(cor(PmScaled[, 18:29]), upper = "number", lower = "circle")
```



Are all correlation coefficients < |0.6|?
abs(cor(PmScaled[, 18:29])) <= 0.6</pre>

	sst	chla	temp600	wavenow	bath m	slope	aspect	dist	ssh	sshsd	eke
sst	FALSE	TRUE	TRUE	TRUE	TRUE	TRUE	TRUE	TRUE	TRUE	TRUE	TRUE
chla		FALSE	TRUE	TRUE	TRUE	TRUE	TRUE	TRUE	TRUE	TRUE	TRUE
temp600	TRUE	TRUE	FALSE	TRUE	TRUE	TRUE	TRUE	TRUE	TRUE	TRUE	TRUE
wavepow	TRUE	TRUE	TRUE	FALSE	TRUE	TRUE	TRUE	TRUE	TRUE	TRUE	TRUE
bath m	TRUE	TRUE	TRUE	TRUE	FALSE	TRUE	TRUE	TRUE	TRUE	TRUE	TRUE
slope	TRUE	TRUE	TRUE	TRUE	TRUE	FALSE	TRUE	TRUE	TRUE	TRUE	TRUE
aspect	TRUE	TRUE	TRUE	TRUE	TRUE	TRUE	FALSE	TRUE	TRUE	TRUE	TRUE
dist	TRUE	TRUE	TRUE	TRUE	TRUE	TRUE	TRUE	FALSE	TRUE	TRUE	TRUE
ssh	TRUE	TRUE	TRUE	TRUE	TRUE	TRUE	TRUE	TRUE	FALSE	TRUE	TRUE
sshsd	TRUE	TRUE	TRUE	TRUE	TRUE	TRUE	TRUE	TRUE	TRUE	FALSE	TRUE
eke	TRUE	TRUE	TRUE	TRUE	TRUE	TRUE	TRUE	TRUE	TRUE	TRUE	FALSE
d2smt	TRUE	TRUE	TRUE	TRUE	TRUE	TRUE	TRUE	TRUE	TRUE	TRUE	TRUE
	${\tt d2smt}$										
sst	TRUE										
chla	TRUE										
temp600	TRUE										
wavepow	TRUE										
$bath_m$	TRUE										
slope	TRUE										
aspect	TRUE										
dist	TRUE										
ssh	TRUE										
sshsd	TRUE										
eke	TRUE										
d2smt	FALSE										

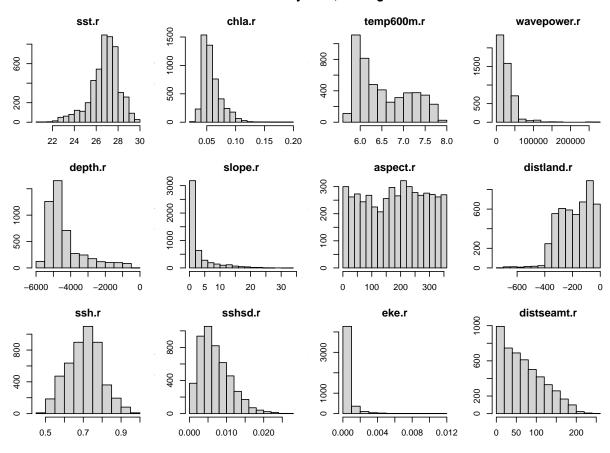
KS tests

I compared the distributions of environmental data between the whales and the absences. Plots are attached in separate powerpoint. In summary, temperature at 600 m, SSH, and chlorophyll were the only variables with significantly different distributions (p-value < 0.05). However, the D statistics were close to zero (D \sim 0.1) for each, indicating that although the distributions were different, they were not that far apart. The plots also show how similar the general shape of the distributions are between where the whales were observed and where they were absent.

Data Visualization

Histograms showing the general distribution of each environmental predictor for the entire dataset.

Acoustics Only Data, 25km grid



dev.off()

Data Splitting

Split the data into train and test sets

```
require(dplyr)
splitdf <- function(dataframe, seed = NULL) {
    if (!is.null(seed))
        set.seed(seed)
    index <- 1:nrow(dataframe)
    trainindex <- sample(index, trunc(length(index) * 0.7))
    trainset <- dataframe[trainindex, ]
    testset <- dataframe[-trainindex, ]
    list(trainset = trainset, testset = testset)
}
trainForg = NULL
testForg = NULL
# preschk = NULL
seed = 3</pre>
```

```
for (s in c(1641, 1303, 1604, 1705, 1706)) {
    trSub <- filter(PmForage, survey == s)</pre>
    # subset for presences and split 70/30
    pres1 <- filter(trSub, pa > 0 & forage == 1) # & loc == 1) #include all presence data/acoustic enc
    listPres <- splitdf(pres1, seed) #output is list for train and test
    # preschk = rbind(preschk, pres1) subset for absences and
    # split 70/30
    abs0 <- filter(trSub, pa == 0)
    listAbs <- splitdf(abs0, seed)</pre>
                                    #output is list for train and test
    # combine train data for presence and absence
    trainAll <- rbind(listPres$trainset, listAbs$trainset)</pre>
    # combine test data for presence and absence
    testAll <- rbind(listPres$testset, listAbs$testset)</pre>
    trainForg = rbind(trainForg, trainAll)
    testForg = rbind(testForg, testAll)
    # trainAcOnly$log.effort <- log(trainAcOnly$EffArea)</pre>
    # testAcOnly$log.effort <- log(testAcOnly$EffArea)</pre>
}
saveRDS(trainForg, here::here(paste0("output/models/", loctype,
    "/data/Train_", gridsize, "km_", loctype2, "_Hunt.rda")))
saveRDS(testForg, here::here(paste0("output/models/", loctype,
    "/data/Test_", gridsize, "km_", loctype2, "_Hunt.rda")))
# nrow(dplyr::filter(trainAcOnly, trainAcOnly$pa >0))
# nrow(dplyr::filter(testAcOnly, testAcOnly$pa >0))
```

Generalized Additive Models

The data are treated as count data, number of sperm whale encounters per cell, and we used the negative binomial distribution to model the response variable for comparison with the Tweedie distribution. We used thin-plate regression splines (the default basis) for the smoothers of the environmental predictors. Each smoother was limited to 3 degrees of freedom (k=3) to reduce overfitting parameters per recommendations from other studies building similar types of cetaceans distribution models. The log of the effort was included as an offset to account for the variation in effort per cell.

25 km spatial scale

- NEGATIVE BINOMIAL DISTRIBUTION
- Knots contrained to k=3 according to literature on cetacean distribution models.
- Automatic term selection is uses an additional penalty term when determining the smoothness of the function ('select' argument = TRUE)..
- We excluded all non-significant variables (alpha=0.05) and refit the models until all variables were significant.
- REML is restricted maximum likelihood used to optimize the parameter estimates.

Load training and test data

Model Selection

SET 1

Full Models

```
+ does not include spatial smoother
+ does not include slope or aspect due to the variation between left and rightes not include slope or a
```

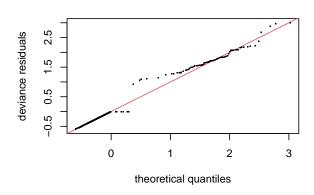
```
Family: Negative Binomial(0.215)
Link function: log
Formula:
pa \sim s(bath_m, k = 3) + s(dist, k = 3) + s(d2smt, k = 3) + s(sst, k = 3) + s
            k = 3) + s(chla, k = 3) + s(temp600, k = 3) + s(ssh, k = 3) +
            s(shsd, k = 3) + s(eke, k = 3) + s(wavepow, k = 3) + offset(log.effort)
Parametric coefficients:
                                     Estimate Std. Error z value Pr(>|z|)
                                                                    0.1387 -165.8 <2e-16 ***
(Intercept) -22.9993
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
Approximate significance of smooth terms:
                                                     edf Ref.df Chi.sq p-value
s(bath_m) 1.890e-04
                                                                                 2 0.000 0.506523
                                  7.229e-06
                                                                                 2 0.000 0.608563
s(dist)
s(d2smt)
                                  4.459e-02
                                                                              2 0.044 0.317263
s(sst)
                                  1.577e+00
                                                                                 2 10.560 0.001159 **
                                  9.139e-01
                                                                              2 9.931 0.000813 ***
s(chla)
s(temp600) 1.634e+00
                                                                             2 11.480 0.000884 ***
                                  1.245e-01
                                                                            2 0.139 0.286352
s(ssh)
                                                                          2 3.304 0.037689 *
2 1.383 0.138333
s(sshsd) 7.662e-01
                                  6.343e-01
s(eke)
s(wavepow) 6.744e-06
                                                                             2 0.000 1.000000
```

```
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
```

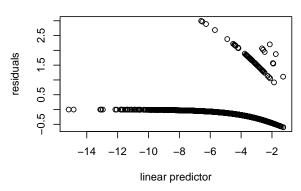
R-sq.(adj) = 0.0335 Deviance explained = 9.91% -REML = 349.66 Scale est. = 1 n = 3325

AIC(nbHunt)

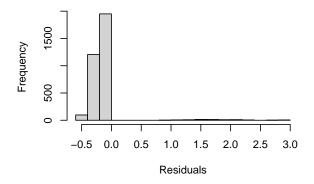
[1] 696.7931



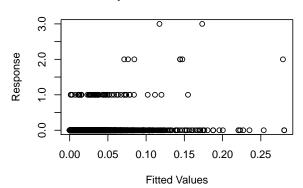
Resids vs. linear pred.



Histogram of residuals



Response vs. Fitted Values



Method: REML Optimizer: outer newton full convergence after 15 iterations.

Gradient range [-4.138678e-05,2.13395e-05]
(score 349.6551 & scale 1).

Hessian positive definite, eigenvalue range [8.288702e-07,5.446699].

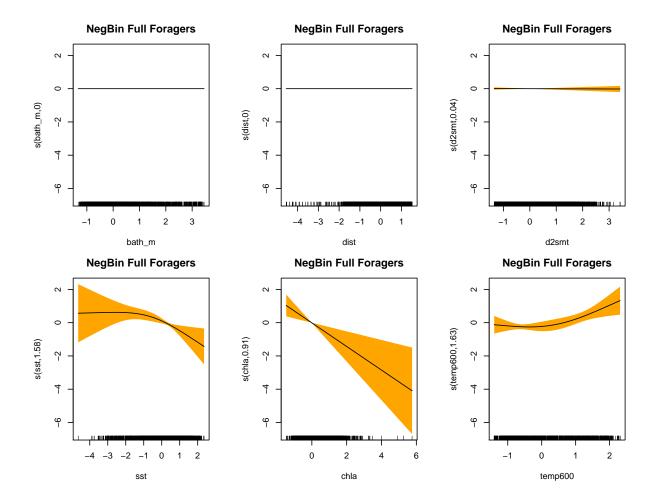
Model rank = 21 / 21

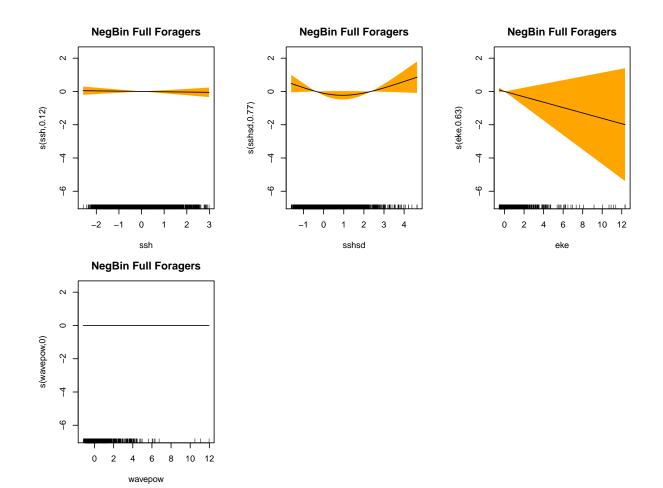
Basis dimension (k) checking results. Low p-value (k-index<1) may indicate that k is too low, especially if edf is close to k'.

k' edf k-index p-value $s(bath_m)$ 2.00e+00 1.89e-04 0.78 <2e-16 ***

```
s(dist)
           2.00e+00 7.23e-06
                                 0.84
                                        0.530
s(d2smt)
           2.00e+00 4.46e-02
                                 0.82
                                        0.270
s(sst)
           2.00e+00 1.58e+00
                                 0.82
                                        0.205
s(chla)
           2.00e+00 9.14e-01
                                 0.84
                                        0.520
s(temp600) 2.00e+00 1.63e+00
                                 0.77
                                       <2e-16 ***
s(ssh)
           2.00e+00 1.24e-01
                                 0.82
                                        0.105
s(sshsd)
           2.00e+00 7.66e-01
                                 0.81
                                        0.055 .
s(eke)
           2.00e+00 6.34e-01
                                 0.84
                                        0.440
s(wavepow) 2.00e+00 6.74e-06
                                 0.78
                                       <2e-16 ***
```

Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' '1





Trying the Tweedie for comparison

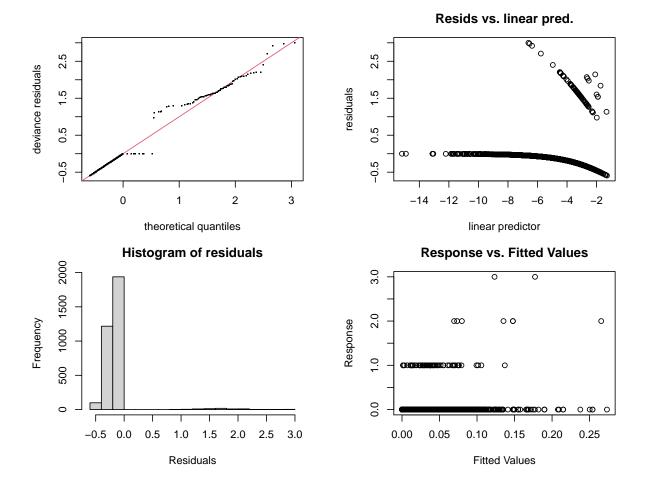
```
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Approximate significance of smooth terms:
                 edf Ref.df
                                F p-value
s(bath m) 3.558e-05 2 0.000 0.648125
s(dist)
           4.388e-05
                         2 0.000 0.455767
s(d2smt) 4.935e-01
                        2 0.473 0.164867
                        2 6.836 0.000232 ***
2 6.012 0.000265 ***
s(sst)
           1.677e+00
s(chla)
           9.264e-01
s(temp600) 1.720e+00
                         2 8.554 4.67e-05 ***
                         2 0.351 0.193042
           4.187e-01
s(ssh)
           8.708e-01 2 3.407 0.005133 **
6.688e-01 2 0.833 0.113263
s(sshsd)
           6.688e-01
s(eke)
                          2 0.833 0.113263
s(wavepow) 1.863e-05 2 0.000 1.000000
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
R-sq.(adj) = 0.04 Deviance explained = 9.12%
-REML = 265.07 Scale est. = 1.0427
AIC(twHunt)
[1] 3297.434
Reduced Models
  • Negative Binomial -> higher explained deviance
  • Removed non-significant variables:
       - depth
       - distance to land
       - distance to seamount
       - SSH
       - eke
       - wave power
# * Does NOT include sighted acoustic encounters
nbHuntb \leftarrow gam(pa \sim s(sst, k = 3) + s(chla, k = 3) + s(temp600,
    k = 3) + s(sshsd, k = 3) + offset(log.effort), data = trainHunt,
    family = nb, link = "log", select = TRUE, method = "REML")
summary(nbHuntb)
Family: Negative Binomial(0.209)
Link function: log
Formula:
pa \sim s(sst, k = 3) + s(chla, k = 3) + s(temp600, k = 3) + s(sshsd,
    k = 3) + offset(log.effort)
```

Parametric coefficients:

```
Estimate Std. Error z value Pr(>|z|)
                        0.1382 -166.4
(Intercept) -22.9910
                                        <2e-16 ***
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
Approximate significance of smooth terms:
             edf Ref.df Chi.sq p-value
                      2 10.741 0.001321 **
s(sst)
          1.6254
s(chla)
          0.9161
                      2 10.236 0.000697 ***
                      2 11.394 0.000923 ***
s(temp600) 1.6274
s(sshsd)
          0.7813
                      2 3.599 0.031790 *
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
R-sq.(adj) = 0.032
                     Deviance explained = 9.4%
-REML = 349.93 Scale est. = 1
                                      n = 3325
```

AIC(nbHuntb) #slightly lower AIC

[1] 696.6479



Method: REML Optimizer: outer newton full convergence after 13 iterations.

Gradient range [-6.508201e-06,3.240972e-06]
(score 349.9333 & scale 1).

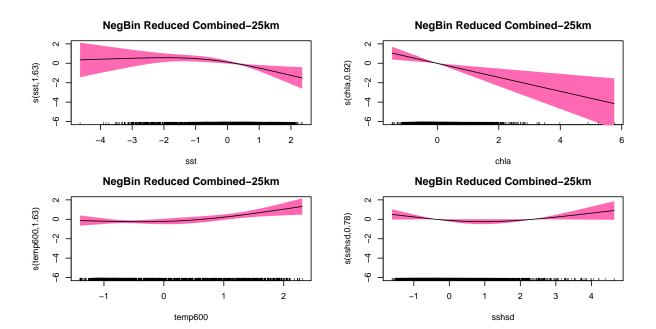
Hessian positive definite, eigenvalue range [5.12901e-06,5.535083].

Model rank = 9 / 9

Basis dimension (k) checking results. Low p-value (k-index<1) may indicate that k is too low, especially if edf is close to k'.

edf k-index p-value s(sst) 2.000 1.625 0.82 0.24 s(chla) 2.000 0.916 0.84 0.54 s(temp600) 2.000 1.627 0.77 <2e-16 *** s(sshsd) 2.000 0.781 0.81 0.06 .

Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1



SET 2

Full Models: Includes s(Longitude, Latitude)

Includes 2D Lat-Lon smoother to account for spatial structure in the data and fit the spatial variation not explained by the other predictors

```
nbHuntLL <- gam(pa ~ s(Longitude, Latitude) + s(bath_m, k = 3) +</pre>
    s(dist, k = 3) + s(d2smt, k = 3) + s(sst, k = 3) + s(chla,
    k = 3) + s(temp600, k = 3) + s(ssh, k = 3) + s(sshsd, k = 3) +
    s(eke, k = 3) + s(wavepow, k = 3) + offset(log.effort), data = trainHunt,
    family = nb, link = "log", select = TRUE, method = "REML")
summary(nbHuntLL)
Family: Negative Binomial(0.336)
Link function: log
Formula:
pa ~ s(Longitude, Latitude) + s(bath_m, k = 3) + s(dist, k = 3) +
    s(d2smt, k = 3) + s(sst, k = 3) + s(chla, k = 3) + s(temp600,
    k = 3) + s(ssh, k = 3) + s(sshsd, k = 3) + s(eke, k = 3) +
    s(wavepow, k = 3) + offset(log.effort)
Parametric coefficients:
            Estimate Std. Error z value Pr(>|z|)
                          0.1538 -150.7 <2e-16 ***
(Intercept) -23.1897
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
Approximate significance of smooth terms:
                              edf Ref.df Chi.sq p-value
s(Longitude, Latitude) 9.227e+00
                                      29 40.180 9.67e-08 ***
s(bath_m)
                      6.055e-05
                                       2 0.000 0.56098
s(dist)
                                       2 0.000 0.30197
                       1.069e-04
                     9.713e-05 2 0.000 0.46633

9.454e-01 2 3.375 0.03437 *

8.916e-01 2 7.476 0.00279 *

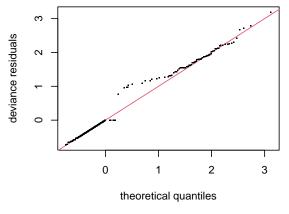
7.735e-01 2 3.325 0.02338 *

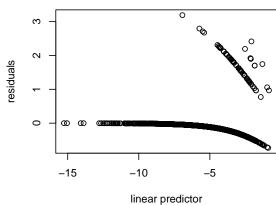
6.952e-05 2 0.000 0.51109

8.420e-01 2 5.241 0.01207 *
s(d2smt)
s(sst)
s(chla)
                                      2 7.476 0.00279 **
s(temp600)
                    7.735e-01
s(ssh)
                     8.420e-01
                                      2 5.241 0.01207 *
s(sshsd)
s(eke)
                       4.675e-01
                                      2 0.700 0.21651
                                      2 0.000 0.80305
s(wavepow)
                       3.730e-05
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
R-sq.(adj) = 0.0624 Deviance explained = 18.3%
-REML = 341.55 Scale est. = 1
                                         n = 3325
AIC(nbHuntLL)
```

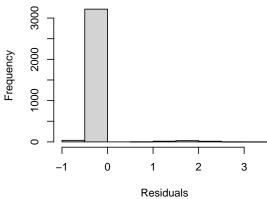
[1] 680.0982

Resids vs. linear pred.

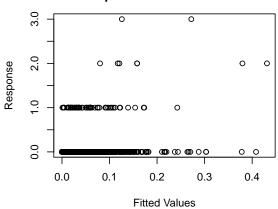




Histogram of residuals



Response vs. Fitted Values



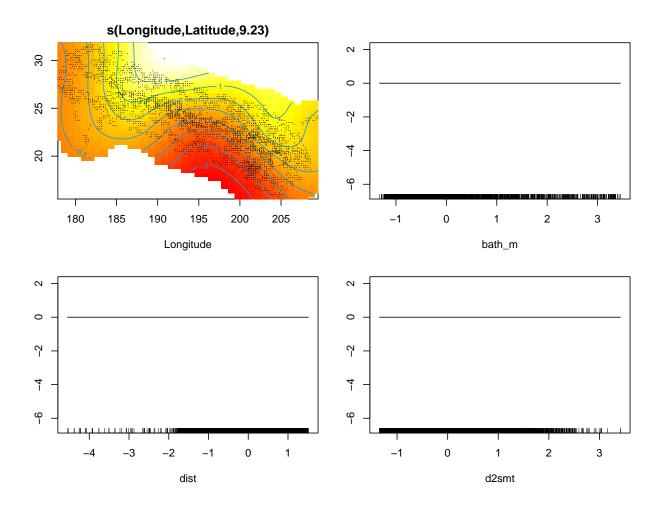
Method: REML Optimizer: outer newton full convergence after 12 iterations. Gradient range [-0.0006049324,0.0001165966] (score 341.5505 & scale 1).

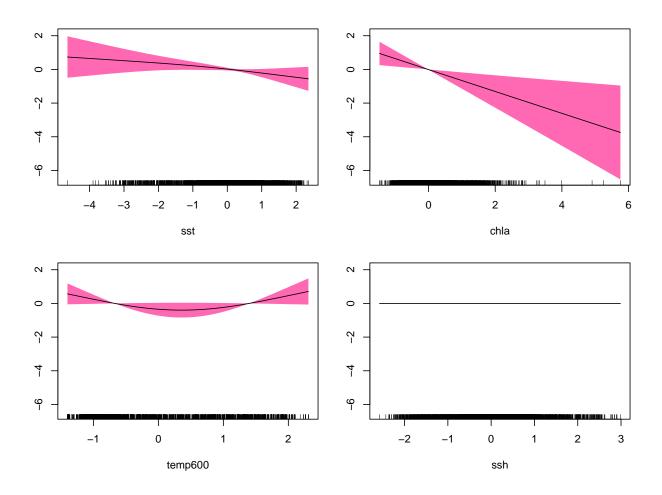
Hessian positive definite, eigenvalue range [5.439635e-06,4.223997]. Model rank = 50 / 50

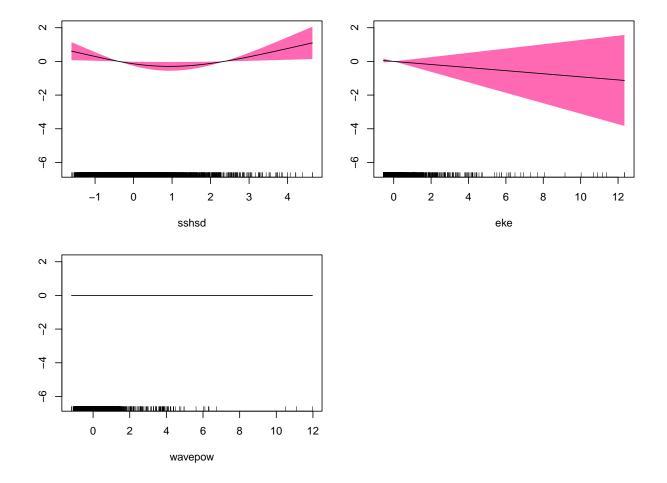
Basis dimension (k) checking results. Low p-value (k-index<1) may indicate that k is too low, especially if edf is close to k'.

	k'	edf	k-index	p-value	
s(Longitude, Latitude)	2.90e+01	9.23e+00	0.82	0.065	
s(bath_m)	2.00e+00	6.06e-05	0.80	0.010	**
s(dist)	2.00e+00	1.07e-04	0.86	0.650	
s(d2smt)	2.00e+00	9.71e-05	0.85	0.300	
s(sst)	2.00e+00	9.45e-01	0.84	0.190	
s(chla)	2.00e+00	8.92e-01	0.85	0.390	
s(temp600)	2.00e+00	7.74e-01	0.80	<2e-16	***
s(ssh)	2.00e+00	6.95e-05	0.84	0.170	
s(sshsd)	2.00e+00	8.42e-01	0.83	0.105	
s(eke)	2.00e+00	4.68e-01	0.85	0.315	
s(wavepow)	2.00e+00	3.73e-05	0.80	<2e-16	***

Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1







Checking Tweedie for comparison

```
twHuntLL <- gam(pa ~ s(Longitude, Latitude) + s(bath_m, k = 3) +
    s(dist, k = 3) + s(d2smt, k = 3) + s(sst, k = 3) + s(chla,
    k = 3) + s(temp600, k = 3) + s(ssh, k = 3) + s(sshsd, k = 3) +
    s(eke, k = 3) + s(wavepow, k = 3) + offset(log.effort), data = trainHunt,
    family = tw, link = "log", select = TRUE, method = "REML")
summary(twHuntLL)</pre>
```

```
Family: Tweedie(p=1.01)
Link function: log

Formula:
pa ~ s(Longitude, Latitude) + s(bath_m, k = 3) + s(dist, k = 3) +
    s(d2smt, k = 3) + s(sst, k = 3) + s(chla, k = 3) + s(temp600, k = 3) + s(ssh, k = 3) + s(sshsd, k = 3) + s(eke, k = 3) +
    s(wavepow, k = 3) + offset(log.effort)
Parametric coefficients:
```

Estimate Std. Error t value Pr(>|t|)

2D Spatial Smoother

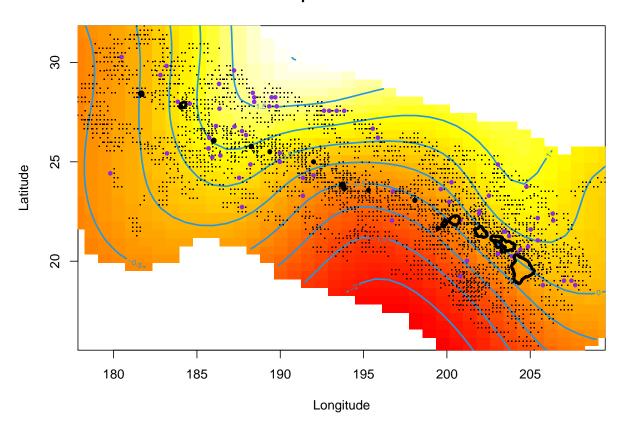


Figure 1: Purple dots represent acoustically detected encounters. Black dots are all data points (grid centroids)

```
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
Approximate significance of smooth terms:
                                     edf Ref.df
                                                         F p-value
s(Longitude, Latitude) 1.022e+01
                                           29 1.807 3.29e-10 ***
s(bath m)
                                               2 0.000 0.55626
                             9.254e-05
                            6.713e-05
s(dist)
                                                2 0.000 0.31244
s(d2smt)
                          3.431e-01
                                               2 0.262 0.19691
s(sst)
                            1.157e+00
                                               2 2.074 0.02535 *

      9.037e-01
      2 4.457
      0.00112 **

      8.432e-01
      2 2.661
      0.00581 **

      1.632e-04
      2 0.000
      0.54736

      9.013e-01
      2 4.633
      0.00123 **

      5.644e-01
      2 0.535
      0.16338

      8.450e-05
      2 0.000
      0.51516

                                               2 4.457 0.00112 **
s(chla)
                             9.037e-01
s(temp600)
s(ssh)
s(sshsd)
s(eke)
s(wavepow)
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
R-sq.(adj) = 0.0737 Deviance explained =
-REML = 253.84 Scale est. = 1.0402
AIC(twHuntLL)
```

[1] 3456.021

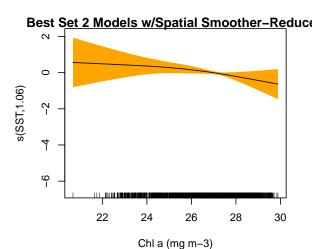
REDUCE MODEL PARAMETERS

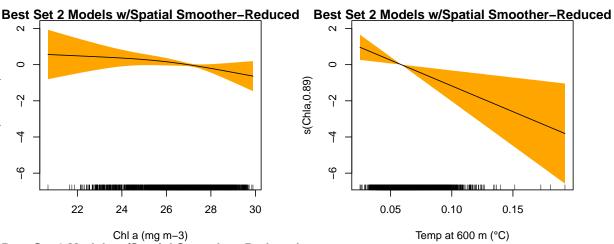
- Negative Binomial: higher explained deviance, lower AIC than Tweedie
- Keep:
 - Lon, Lat
 - SST
 - chlorophyll
 - temp at 600 m
 - SSHsd

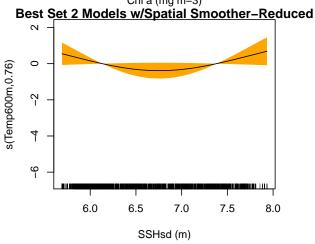
Family: Negative Binomial(0.332) Link function: log

Formula:

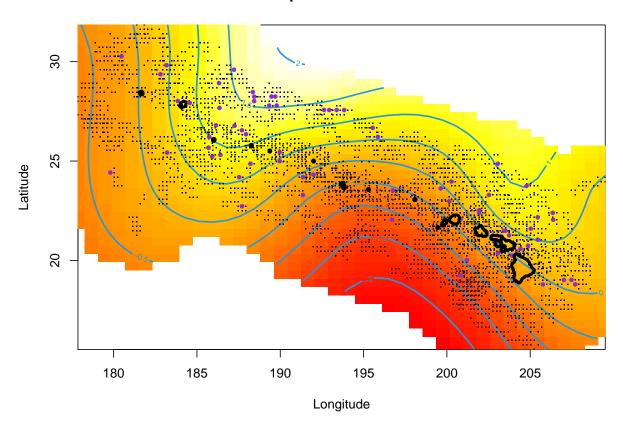
```
pa ~ s(Longitude, Latitude) + <math>s(SST, k = 3) + s(Chla, k = 3) +
    s(Temp600m, k = 3) + s(SSHsd, k = 3) + offset(log.effort)
Parametric coefficients:
            Estimate Std. Error z value Pr(>|z|)
(Intercept)
           -23.188
                         0.154 -150.6
                                         <2e-16 ***
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
Approximate significance of smooth terms:
                        edf Ref.df Chi.sq p-value
s(Longitude, Latitude) 9.1825
                                 29 40.493 7.57e-08 ***
s(SST)
                      1.0574
                                 2 3.322 0.04214 *
s(Chla)
                      0.8921
                                    7.613 0.00247 **
                                 2
s(Temp600m)
                      0.7631
                                 2 3.143 0.02616 *
s(SSHsd)
                      0.8467
                                 2
                                    5.444 0.01076 *
               0 '*** 0.001 '** 0.01 '* 0.05 '. ' 0.1 ' 1
R-sq.(adj) = 0.0614
                      Deviance explained = 18.1%
-REML = 341.61 Scale est. = 1
                                      n = 3325
```







Spatial Smoother



Conclusions

Predict Test Data

```
# absolute error Calculate MSE AFTER transforming the
# predictions back to the same scale as the observed data
colnames(testHunt)[30] <- "SST"</pre>
colnames(testHunt)[31] <- "Chla"</pre>
colnames(testHunt)[32] <- "Temp600m"</pre>
colnames(testHunt)[39] <- "SSHsd"</pre>
nbPred <- predict.gam(nbHuntb, newdata = testHunt, type = "response",</pre>
    se.fit = TRUE)
nbTestFinal <- data.frame(testHunt, fit = nbPred$fit, se.fit = nbPred$se.fit)</pre>
nbMSEtest <- mean((nbTestFinal$pa - nbTestFinal$fit)^2) #MSE
# mean(abs((testFinal$pa - testFinal$fit))) #Mean absolute
# error
#### For nbCombcLL, with spatial smoother #### pulling the
#### prediction and residual data from the model
nbTrainLL <- trainHunt %>% mutate(resid = resid(nbHuntLLb2),
    predict = predict(nbHuntLLb2))
predTrainLL <- predict.gam(nbHuntLLb2, type = "response") #calculate MSE for these to compare with tes
nbTrainLL$fit <- predTrainLL</pre>
# using scale of 0,1,2 makes this hard to interpret
nbMSEtrainLL <- mean((nbTrainLL$pa - nbTrainLL$fit)^2) #MSE</pre>
# mean(abs((nbTrainFinal$pa - nbTrainFinal$fit))) #Mean
# absolute error Calculate MSE AFTER transforming the
# predictions back to the same scale as the observed data
nbPredLL <- predict.gam(nbHuntLLb2, newdata = testHunt, type = "response",</pre>
    se.fit = TRUE)
nbTestLL <- data.frame(testHunt, fit = nbPredLL$fit, se.fit = nbPredLL$se.fit)</pre>
nbMSEtestLL <- mean((nbTestLL$pa - nbTestLL$fit)^2) #MSE</pre>
# mean(abs((testFinal$pa - testFinal$fit))) #Mean absolute
# error
# AIC
nbAIC <- AIC(nbHuntb)</pre>
nbAICLL <- AIC(nbHuntLLb2)</pre>
# Explained Deviance
nbExpDev = round(((nbHuntb$null.deviance - nbHuntb$deviance)/nbHuntb$null.deviance) *
nbExpDevLL = round(((nbHuntLLb2$null.deviance - nbHuntLLb2$deviance)/nbHuntLLb2$null.deviance) *
 100, 2)
# make summary table of metrics
table = matrix(NA, nrow = 2, ncol = 5)
colnames(table) = c("Best Models", "ExpDev", "AIC", "MSEtrain",
    "MSEtest")
# enter info by row
```

Table 1: Negative Binomial Model Summary Metrics

Best Models	ExpDev	AIC	MSEtrain	MSEtest
nbCombb	9.4%	696.65	0.00-	0.029
nbCombLLb2 (w/ s(Lon,Lat))	18.14%	679.84		0.029