$$S_1 = W_3[x] W_1[x] pa_1 a_1$$
 $S_2 = W_1[y] r_2[y] pc_1 a_1$
 $S_3 = r_2[z] W_3[z] pc_2$