

Hedge Fund Quantitative Analyst Interview Report

Nbody Labs, Company

May 1, 2023

1 Interview Transcript

Below is the complete transcript of the interview. The topics covered in the interview are: Topic 1, ..., Topic n.

2 Technical Interview

Below are the questions and solutions generated by NBodyLabs.

2.1 Question #0:

Problem: Consider a function $f(x, y) = x^2 + y^2$. Find the critical points and determine their nature (maximum, minimum, or saddle point) using the second partial derivative test.

Difficulty: Medium

Topic: Calculus and Differential Equations

Reference Solution: To find the critical points of the function $f(x, y) = x^2 + y^2$ and determine their nature, we will follow these steps:
1. Find the first partial derivatives of f with respect to x and y .
2. Set the first partial derivatives equal to zero and solve for x and y to find the critical points.
3. Use the second partial derivative test to determine the nature of the critical points.
Step 1: Calculate the first partial derivatives.
 $f_x = \frac{\partial f}{\partial x} = 2x$
 $f_y = \frac{\partial f}{\partial y} = 2y$
Step 2: Find the critical points by setting f_x and f_y equal to 0.
 $2x = 0 \Rightarrow x = 0$
 $2y = 0 \Rightarrow y = 0$
The critical point is $(0, 0)$.
Step 3: Apply the second partial derivative test.
Calculate the second partial derivatives:
 $f_{xx} = \frac{\partial^2 f}{\partial x^2} = 2$
 $f_{yy} = \frac{\partial^2 f}{\partial y^2} = 2$
 $f_{xy} = \frac{\partial^2 f}{\partial x \partial y} = 0$
Compute the determinant of the Hessian matrix $D = f_{xx} * f_{yy} - f_{xy}^2$:
 $D = 2 * 2 - 0^2 = 4$
Since $D > 0$ and $f_{xx} > 0$, the critical point $(0, 0)$ is a local minimum.

conclusion, the function $f(x, y) = x^2 + y^2$ has a single critical point at $(0, 0)$, which is a local minimum.

Grading Rubric: {'rubric': [{'Question': 'Question Number 0', 'Rubric': [{'Part': 'Step 1: Calculate the first partial derivatives', 'Description': 'Correctly calculates the first partial derivatives of f with respect to x and y ', 'Points': {'0': 'No attempt or incorrect calculation', '1': 'Partial correct calculation (only one correct partial derivative)', '2': 'Correctly calculates both f_x and f_y '}}}, {'Part': 'Step 2: Find the critical points', 'Description': 'Sets the first partial derivatives equal to zero and solves for x and y to find the critical points', 'Points': {'0': 'No attempt or incorrect critical point', '1': 'Correctly identifies the critical point $(0, 0)$ '}}}, {'Part': 'Step 3: Apply the second partial derivative test', 'Description': 'Calculates the second partial derivatives and computes the determinant of the Hessian matrix', 'Points': {'0': 'No attempt or incorrect calculation', '1': 'Partial correct calculation (one or two correct second partial derivatives)', '2': 'Correctly calculates all second partial derivatives and computes the determinant'}}}, {'Part': 'Step 3: Determine the nature of the critical points', 'Description': 'Uses the second partial derivative test to determine the nature of the critical points', 'Points': {'0': 'No attempt or incorrect determination', '1': 'Correctly determines the nature of the critical point $(0, 0)$ as a local minimum'}}}, {'Part': 'Overall structure and thought process', 'Description': 'Presents a clear and structured thought process throughout the solution', 'Points': {'0': 'Unclear or disorganized thought process', '1': 'Some structure and clarity, but with room for improvement', '2': 'Clear and structured thought process'}}}]}

Feedback on Candidate Solution: The candidate provided a correct conclusion, stating that the critical point $(0, 0)$ is a local minimum. However, they did not show the steps for calculating the first and second partial derivatives, finding the critical points, and applying the second partial derivative test. As a result, they did not achieve points in Steps 1, 2, and 3, but achieved 1 point in Step 4 for correctly determining the nature of the critical point and 1 point in Step 5 for overall structure and thought process.

Candidate Score: 2 / 9