ETH Zurich Institut für Theoretische Informatik

Prof. Dr. Angelika Steger Prof. Dr. Emo Welzl

Prof. Dr. Peter Widmayer

Algorithms Lab

Exercise – Poker Chips

You regularly meet with your friends on Thursdays for poker night. Three hours into the evening, and slightly drunk already, you get bored of the game and start stacking up the chips in various ways. This gets you thinking. What if you played a solitaire game with the chips?

The rules are as follows. First distribute the chips randomly into several stacks. Then repeat until no chips are left:

- For any subset (of your choosing) of stacks remove the topmost chip from each of its stacks, provided these chips all have the same color.
- If you removed k > 1 chips, award yourself 2^{k-2} points. If you only removed one chip, 0 points.

Your score is the sum of points gained in each step. The goal, of course, is to score the maximum possible number of points.

On the next morning, sober again, you decide to solve the problem once and for all with a program.

Input The first line of the input contains the number of test cases $1 \le t \le 60$. Each of the following t test cases describes a starting arrangement of the game as follows.

- It starts with a line that contains one integer $1 \le n \le 5$, the number of stacks you formed.
- The next line contains n positive integers m_1, \ldots, m_n ($1 \le m_i \le 2000$) separated by spaces, such that $\prod_i (m_i + 1) \le 2^{16}$. Here m_i is the number of chips in the i-th stack.
- The following n lines list the chips in the stacks. The i-th such line contains integers c_{i1}, \ldots, c_{im_i} separated by spaces. Each c_{ij} ($1 \le c_{ij} \le 2^{10}$) represents the color of one chip. c_{im_i} is the chip at the top of the stack (removed first) and c_{i1} is the chip at the bottom (removed last).

Output For every test case the corresponding output appears on a separate line. Each output consists of one integer p: the maximum number of points you can score in the game according to the rules above.

Points There are four test sets, worth 100 points in total.

- 1. For the first test set, worth 30 points, you may assume $n \le 2$.
- 2. For the second test set, worth 30 points, you may assume $m_i \le 12$ for all $i \in \{1, ..., n\}$.
- 3. For the third test set, worth 20 points, there are no additional assumptions.
- 4. For the fourth (hidden) test set, worth 20 points, there are no additional assumptions.

Sample Input

Sample Output

2