

## Question 2

For Network 1:

$$\vec{a}^{(1)} = W^{(1)}\vec{a}^{(0)} + \vec{b}^{(1)} \quad (1)$$

$$\vec{a}^{(2)} = W^{(2)}\vec{a}^{(1)} + \vec{b}^{(2)} \quad (2)$$

$$\vec{a}^{(3)} = W^{(3)}\vec{a}^{(2)} + \vec{b}^{(3)} \quad (3)$$

Bring equation (1), (2) into equation (3)

$$\vec{a}^{(3)} = W^{(1)}W^{(2)}W^{(3)}\vec{a}^{(0)} + W^{(2)}W^{(3)}\vec{b}^{(1)} + W^{(3)}\vec{b}^{(2)} + \vec{b}^{(3)}$$

For Network 2:

$$\vec{a}^{(3)} = W \vec{a}^{(0)} + B$$

$$\text{When } W = W^{(1)}W^{(2)}W^{(3)} \quad B = W^{(2)}W^{(3)}\vec{b}^{(1)} + W^{(3)}\vec{b}^{(2)} + \vec{b}^{(3)}$$

The two networks are equivalent.