Leipzig University Institute of Computer Science Degree Programme Computer Science, B.Sc.

Investigating Core Set-based Active Learning for Text Classification

Bachelor's Thesis

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Declaration

Unless otherwise indicated in the text or references, this thesis is entirely the product of my own scholarly work.

Leipzig, April 26, 2024

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Abstract

Following the exponential growth in the number of readily available documents and texts in recent years, the need for efficient methods of classification has become increasingly important. In many cases, the available data for machine learning is abundant, but the corresponding classes, also known as labels, are expensive to obtain. Active Learning is a subfield of machine learning that attempts to combat this issue by selecting instances from an unlabelled pool such that they are annotated by some information source. This selection is performed using a query strategy, which decides which instances are most conducive to the learning process and should thus be annotated. One such query strategy is the Core-Set approach (Sener and Savarese [2018]), a diversity-based query strategy that operates using the distances between instances and attempts to select sample such that they best cover the rest of the dataset. Although this approach is well-established within the AL field, it has shown mixed results within the field of text classification. In this thesis, I aim to investigate the performance of Core-Set when applied to the task of text classification, as well as propose three approaches (dimensionality reductionbased, uncertainty-based, class balance-based) that iterate upon the original strategy. The experiments conducted within this thesis show that within the domain of text classification, Core-Set has mixed results when compared to well-known baseline approaches. Additionally, this thesis demonstrates minor performance increases when combined with two dimensionality reduction techniques; however, the uncertainty- and class balance-based approaches do not lead to significant improvements.

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Chapter 1

Introduction

Text is one of the most widespread and important sources of information, but extracting data and tangible knowledge from it can be a difficult and expensive task. With the advent of the digital age, enormous amounts of unstructured texts have become available with more being generated by the day. Due to this increasingly large amount of textual data, manually processing information at a larger scale becomes infeasible and thus demands the use of computer-driven approaches.

The classification of text, meaning the assignment of a category or class to a document or piece of text is one of the most common and useful ways to gain information from a piece of text. As the amount of available text content continues to grow, text classification tasks become an increasingly important area of research within the field of natural language processing.

Thanks to machine learning and data science, many methods of extracting information from text have been developed with the purpose of performing text classification at a larger scale. This possibility for automated organization of data can enhance insights and decision-making across industries such as healthcare, finance, and social sciences, among many others. Active Learning (AL) is a subfield of machine learning in which the learning algorithm is able to perform queries on an information source in order to reduce the total amount of annotated data (Settles [2009]). This method can offer significant advantages in improving model performances and especially in reducing labeling costs. Though there is no universally optimal strategy, AL has been proven to be useful in many cases where annotating data is expensive or the total amount of data is very large (Settles [2009]).

Oftentimes, there is a large amount of unlabelled data available for an AL model to learn from. In this case, selecting the most effective data points to be labelled by the information source from this large pool becomes a crucial, but difficult challenge to overcome.

One attempt at improving the effectiveness of AL in this regard is the Core-Set approach (Sener and Savarese [2018]). This method uses core-set selection to counter the issue of AL ineffectiveness on convolutional neural networks (Sener and Savarese [2018]). The proposed approach selects a set of points from the pool such that a model learning over this subset can be consistent when provided with the remaining data points. The method has been shown to have improved results when compared to other approaches in the field of computer vision (Sener and Savarese [2018], Caramalau et al. [2021]), which encompasses tasks that focus on enabling computers to interpret and understand visual information from the real world. This field involves a variety of different methods including image classification, object detection, and semantic segmentation, all of which have significant importance in scientific research, classification tasks, and pattern recognition.

However, the Core-Set approach has been shown to have mixed results in cases of text classification using BERT (Prabhu et al. [2021], Ein-Dor et al. [2020]) and binary text classification using deep neural networks (Liu et al. [2021]). In some cases, Core-Set performs poorly even when compared to the random sampling strategy (Prabhu et al. [2021], Coleman et al. [2022]). Additional research suggests that the approach may even be less effective in computer vision tasks with higher numbers of classes as well as higher-dimensional feature spaces (Sinha et al. [2019]). The theoretical analysis shown in Sener and Savarese [2018] briefly mentions the potential issue of higher class numbers; however, it does not attempt to provide a potential solution to the problem.

The mixed results for Core-Set just mentioned motivated three different research questions for this thesis.

- 1. Can we improve Core-Set's mixed results within the field of text classification using dimensionality reduction techniques?
- 2. Does an uncertainty-based approach improve the performance of Core-Set?
- 3. Can we balance the class distribution within the Core-Set selection, and how will this affect the learning process?

By first explaining Core-Set's functionality and the possible reasons for why it tends to underperform in certain classification tasks, I aim to then examine the performance of Core-Set in comparison to various baseline approaches on large datasets of text content in order to verify this claim. Furthermore, this thesis looks to modify and potentially improve the Core-Set approach for text classification with the previous three research questions in mind and demonstrate the results of these modifications as a part of its experiment.

In the following, Chapter 2 explains the background and related work on the topics of text classification (Section 2.1), active learning in general (Section 2.2), the Core-Set approach (Section 2.3), and dimensionality reduction (Section 2.4) more specifically. In Chapter 3, I describe my approach to modifying Core-Set for text classification using three general categories of approaches. In Chapters 4 and 5, I outline my experiment as well as present and discuss its results. Finally, Chapter 6 concludes the thesis and provides insights on the experiment's limitations as well as potential future developments.

Chapter 2

Background/Related Work

This chapter first provides an overview of the fields of text classification and active learning, which are crucial for understanding Core-Set and its usage scenario within this thesis. I then give a brief review of Core-Set on both a conceptual and functional level. The concepts and notations introduced here will be necessary to understand the reasoning and functionality behind the following approaches employed in the experiment. Finally, this chapter outlines the field of dimensionality reduction, placing emphasis on techniques that will pertain to the subsequent chapters.

2.1 Text Classification

Text classification is one of the most fundamental and important tasks in the field of Natural Language Processing (NLP). As a result, developing efficient automatic text classification methods has become an important research topic.

One of the most common applications of text classification is determining whether the opinion associated with a certain document has a positive or negative sentiment, also known as sentiment analysis. This has a wide range of uses, including the possibility for businesses to better gauge customer opinions on products and services (Liu and Zhang [2012]) in order to adapt accordingly. This application is a binary classification task, meaning the classifier has two classes with which each document can be labelled (positive or negative). Similarly, one might apply this binary classification task to the problem of spam filtering in e-mails, text messages and more.

Beyond that, many applications of text classification require multiple classes, such as news and content categorization. In this case, text classification algorithms can organize documents into specific topics or themes (e.g. Sports, Business, Politics, ...) (Sebastiani [2002]). Other applications include information retrieval, recommender systems, and document summarization (Kowsari et al.

[2019]).

Generally, text classification methods can be divided into the following phases: data collection and preprocessing, feature extraction, classifier selection, and model evaluation (Kowsari et al. [2019], Mironczuk and Protasiewicz [2018], Ikonomakis et al. [2005]). Oftentimes, dimensionality reduction can be applied as an additional optional step within the text classification pipeline, as depicted in Figure 2.1.

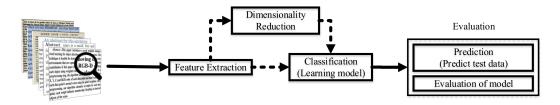


Figure 2.1: Overview of the text classification pipeline adopted from Kowsari et al. [2019].

In the first stage, some form of text data necessary to complete some classification objective is acquired, ideally of a sufficient amount. Several open data sets are publicly available to this end (Pang and Lee [2005], Zhang et al. [2015], Li and Roth [2006]). The preprocessing phase includes steps such as lemmatization, removal of stop words, tokenization and stemming.

The preprocessed text data must them be converted into numerical feature vectors. There are a number of techniques for accomplishing this such as Bag-of-Words, TF-IDF (Term Frequency-Inverse Document Frequency), and word embedding methods such as Word2Vec or GloVe. Word embeddings are representations of words, typically in the form of real-valued, fixed-length vectors (Almeida and Xexéo [2019]). In addition to the word embedding methods just mentioned which are known as static word embeddings, there exist context-sensitive methods as of the late-2010s such as ELMo and BERT (Peters et al. [2018], Devlin et al. [2019]), which can better represent the varied senses encompassed by words depending on their contexts.

The next phase, classifier selection, is one of the most crucial steps in the text classification pipeline. Without a comprehensive grasp of the underlying concepts of each algorithm, we cannot effectively determine an appropriate model for the task. Commonly known algorithms include Logistic Regression, Naïve Bayes and Support Vector Machines. More recently deep learning models such as Convolutional Neural Networks (CNNs), Recurrent Neural Networks (RNNs) and Transformer Models have become established as state-of-the-art approaches, especially when considering large text classification tasks (Chen [2015], Liu et al. [2016], Lai et al. [2015], Devlin et al. [2019], Sun et al.

[2019]). One of the most well-established baseline transformer models is BERT (Devlin et al. [2019]), which stands for Bidirectional Encoder Representations from Transformers. This paper originally introduced BERT with two different model sizes known as BERT_{BASE} and BERT_{LARGE}, both of which were pre-trained on the BooksCorpus dataset (Zhu et al. [2015]) with 800M words and English Wikipedia with 2,500M words. Its bidirectional nature allows the model to learn a text's information from both the left and right context (Devlin et al. [2019]). Generally, this pre-trained model can then be fine-tuned, i.e. trained on additional data, for various more specific tasks. Looking to further improve upon this model, several variations of BERT have been presented since its creation, such as RoBERTa (Liu et al. [2019]) and SBERT (Reimers and Gurevych [2019]). The latter, also known as Sentence-BERT, uses siamese and triplet network structures in order to produce sentence embeddings such that semantically similar sentences are close within the vector space, an aspect in which BERT was also shown to deliver unsuitable results for many common similarity measures (Reimers and Gurevych [2019]). This approach has been further iterated upon by Tunstall et al. [2022], who proposed SetFit (Sentence Transformer Fine-tuning) as a framework for fine-tuning sentence transformers. The general idea of SetFit is to fine-tune a pre-trained SBERT model in a contrastive manner, then use this fine-tuned model to generate text embeddings for training (Tunstall et al. [2022]).

The various different deep learning methods just mentioned are increasingly popular due to their ability to model more complex and non-linear relationships within data (LeCun et al. [2015]). The Core-Set approach was also originally developed for the deep learning domain, more specifically CNNs. As a result, this thesis focuses on the use of deep learning models, more specifically transformers.

Model evaluation is usually the "final" phase of the text classification process. This encompasses the assessment of the classifier's performance, for which a myriad of metrics such as accuracy, F1-score and AUC can be employed. Based on the evaluation, one can select a suitable model/strategy as well as attempt to optimize it, e.g. by tuning hyperparameters.

The process of text classification clearly includes many steps which can be optimized and examined. For this reason, going over the entire process in detail would exceed the scope of this thesis. With this in mind, this thesis' experiment does not focus on the initial steps such as data collection, preprocessing and feature extraction, but rather the model training and evaluation steps.

2.2 Active Learning

Active Learning has become an increasingly important field when considering the need for efficient model construction as well as the labelling bottleneck in various machine learning tasks. Many fields, such as speech recognition, information extraction and classification suffer from this bottleneck as a result of their instance labels being expensive or time-consuming to obtain (Settles [2009]).

Generally, active learning takes place in one of three main scenarios, namely membership query synthesis, stream-based selective sampling and pool-based active learning.

In the case of membership query synthesis, a membership query is created in the form of some unlabelled instance from the original dataset (Angluin [1987], Wang et al. [2015]). In other words, this approach synthesizes a query de novo, rather than selecting some query from the instance space. One challenge of this approach is ensuring that the synthesized query is consistent with meeting the constraints imposed by the real data. In the case of a human oracle, this can result in unrecognizable queries, for example in the case of computer vision tasks. Similarly, this issue could also apply to text classification, where the query synthesis produces unintelligible texts (Lang and Baum [1992], Settles [2009]).

Stream-based selective sampling, in contrast, typically examines each unlabelled instance one at a time and decides whether to query the oracle or to assign a label (Settles [2009]).

Finally, we consider the pool-based approach as one of the commonly known applications of AL. This scenario assumes a large set of unlabelled instances and a small set of labelled instances, from which queries can be selectively drawn using a *query strategy*. Generally, most approaches begin with some random selection of points to initialize the classifier. With each AL iteration, the query strategy selects new instances on which to train the classifier. This process is then repeated until some stopping criterion is met.

The key difference to the stream-based approach is that pool-based learning considers the entire collection and attempts to select the most informative instances, as opposed to making individual query decisions. This can be useful in many real-world problems where plenty of unlabelled data is available and the pool is assumed to be closed (though this is not necessarily always the case) (Settles [2009]).

This thesis considers the case of the pool-based scenario, as does the original Core-Set paper. It is worth mentioning however, that Core-Set has also been applied in the stream-based context (Saran et al. [2023]).

2.3 Core-Set

The Core-Set approach as proposed by Sener and Savarese [2018] was originally designed for CNNs to tackle the problem of AL algorithms on large datasets. The empirical studies conducted in this paper show that Core-Set outperforms other established query strategies when applied in the field of computer vision.

Sener and Savarese [2018] define the task of AL as a *core-set selection* problem in which the algorithm selects a smaller subset of points with increased diversity to learn from such that the model can be competitive over a larger dataset. This problem ends up being equivalent to the *k-Center* problem (Sener and Savarese [2018]), which is also referred to as the minimax facility location problem.

In mathematical terms, given a set of points N and a budget $k \leq |N|$, k-Center finds a subset $\mathbf{s} \subseteq N$ of k points such that the maximum distance of any point in $N \setminus \mathbf{s}$ to its closest center in \mathbf{s} is minimal (Har-Peled [2008]). Core-Set applies this concept to the field of AL in that the k centers selected from N will be the instances selected to be labelled by the oracle (also referred to by Sener and Savarese [2018] as the budget, or b).

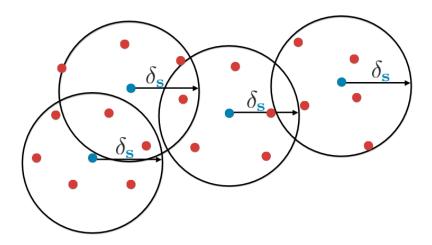


Figure 2.2: Visualization of the k-Center approach from Sener and Savarese [2018]. s denotes the set of k selected points, $\delta_{\mathbf{s}}$ denotes the maximum distance of any point in N to its nearest center in s.

Another way of viewing this problem is by placing circles around the points in our set of centers. If we denote the maximum distance of any point in N to its nearest center in \mathbf{s} with $\delta_{\mathbf{s}}$ and we place circles with a $\delta_{\mathbf{s}}$ -radius around each center in \mathbf{s} , we can "cover" the entire set of points N. In other words, k-Center attempts to find the minimum $\delta_{\mathbf{s}}$ such that all points lie within the union of the

 $\delta_{\rm s}$ -circles when placed upon each center (depicted in Figure 2.2). Due to the nature of k-Center, the selected points tend to be spread out throughout the dataset in order to "cover" all the unselected points, making this a diversity-based approach.

This problem has been shown to be NP-hard (Hsu and Nemhauser [1979], Hochbaum [1984]). As a result, Core-Set uses a greedy approach to solve the k-Center problem. However, it is worth noting that any approximation of k-Center is bound by twice the optimal solution (Hsu and Nemhauser [1979]). Let OPT denote the maximum distance of a center to a point in the optimal solution to k-Center, meaning the solution where $\delta_{\mathbf{s}}$ is minimal. Then the greedy approximation's resulting maximum distance $\delta_{\mathbf{s}}$ to any center in \mathbf{s} is at the worst $2 \cdot OPT$ (Mount [2017]). The pseudocode used by Sener and Savarese [2018] for k-Center greedy within the active learning context can be seen in Algorithm 1.

Algorithm 1 k-Center-Greedy (adopted from Sener and Savarese [2018])

```
Input: data \mathbf{x}_i, existing pool \mathbf{s}^0, budget b
Initialize \mathbf{s} = \mathbf{s}^0
repeat
u = \operatorname{argmax}_{i \in [n] \setminus \mathbf{s}} \min_{j \in \mathbf{s}} \Delta(\mathbf{x}_i, \mathbf{x}_j)
\mathbf{s} = \mathbf{s} \cup \{u\}
until |\mathbf{s}| = b + |\mathbf{s}^0|
return \mathbf{s} \setminus \mathbf{s}^0
```

The original paper by Sener and Savarese [2018] attempts to further improve the robustness of this approximation by placing an upper limit on the number of outliers that can be selected. This thesis focuses on and uses the regular k-Center greedy algorithm, which is generally better established due to ease of implementation and interpretability.

2.4 Dimensionality Reduction

As pointed out earlier, one of the major challenges of the Core-Set approach is handling data points with a higher dimensionality (Sinha et al. [2019]). Broadly speaking, this is a phenomenon coined by Richard E. Bellman known as the *curse of dimensionality* (Freimer and Bellman [1961]). As a result, many algorithms have been developed to transform data from a high-dimensional space into a low-dimensional space. Moreover, reducing dimensionality is often an important aspect when considering the task of data visualization. This task

directly poses another challenge: managing to reduce the dimensionality of the data while still being able to retain the highest possible amount of information.

One such method is the Principal Components Analysis (PCA), which is one of the most popular linear techniques for dimensionality reduction (Van Der Maaten et al. [2009]). In essence, PCA linearly transforms the data into a representation that attempts to closely describe the variance of the initial data (Jolliffe and Cadima [2016]). Other commonly used linear techniques include Linear Discriminant Analysis (LDA), Multidimensional Scaling (MDS), and Non-negative Matrix Factorization (NMF).

These techniques can be powerful; however, they often miss important non-linear structures in high-dimensional data. Therefore, non-linear techniques have been developed such as Isometric Mapping (Isomap), t-distributed Stochastic Neighbor Embedding (t-SNE) and Uniform Manifold Approximation and Projection (UMAP).

t-distributed Stochastic Neighbor Embedding

t-SNE is a relatively modern probablistic approach that has improved upon many other non-linear techniques in creating a single map that reveals structure on many different scales. In addition, it manages to reduce the tendency of Stochastic Neighbour Embedding (SNE) to crowd data points together at the center by using a different cost function (Van der Maaten and Hinton [2008]).

First, it converts the high-dimensional Euclidean distances into conditional probabilities, such that similar data points are assigned higher probabilities and dissimilar data points are assigned very low probabilities. It then creates a similar probability distribution over the lower-dimensional map such that the *Kullback–Leibler divergence* (a measure of how one probability distribution differs from another) is minimized.

The caveat of this technique is that its efficiency on large datasets relies on a variant of the Barnes–Hut algorithm, which results in reductions only being possible to the two- or three-dimensional space (van der Maaten [2013]). Because of this drawback, the method is generally used for the visualization of high-dimensional data, for which a reduction to two- or three-dimensional spaces is ideal.

Uniform Manifold Approximation and Projection

UMAP exists within a similar vein to t-SNE, but offers important improvements in some areas. This technique models the data with a fuzzy topological representation using simplices, then attempts to find some low-dimensional projection with the closest possible equivalent fuzzy topological structure (McInnes

and Healy [2018]). Another key difference is that UMAP accomplishes this projection by attempting to minimize the cross-entropy between the topological representations, whereas t-SNE uses the Kullback-Leibler divergence.

This paper also elaborates that the resulting reductions are competitive with t-SNE in the field of visualization and offer superior runtime performances. In addition, there exists no computational restriction on the embedding dimension, as opposed to t-SNE. As a result, McInnes and Healy [2018] also mentions it as a useful tool not only for visualization, but for machine learning tasks in general.

Chapter 3

Approach

The following chapter describes my approach to the subsequent experiment. The attempt to improve upon and modify Core-Set resulted in multiple different iterations of the original k-Center greedy algorithm, which I have grouped into three different categories. Each of these different categories is designed to address one of the three research questions central to this thesis.

First, I outline the dimensionality reduction-based approach, considering the two different nonlinear techniques discussed previously. After that, I present two uncertainty-based approaches which take pointwise probabilities into account. The final approach for the experiment attempts to use class balancing in combination with Core-Set.

3.1 Dimensionality Reduction-Based

As mentioned, distance-based methods such as Core-Set can be ineffective in higher dimensions. To overcome this challenge, I propose the application of a non-linear dimensionality reduction technique on the training data before selecting new points using Core-Set. My aim with this is attempting to preserve any non-linear structures within the datasets. In essence, this would modify the original k-Center greedy approach in that the distances computed between the points in \mathbf{s} and the unselected points would be different, since the algorithm would take in reduced embeddings (this modification is noted in Algorithm 2).

This resulted in two dimensionality-reduction based approaches. The first strategy, which I refer to as CS-tSNE, use t-SNE in order to reduce the embeddings down to two dimensions. Additionally, I propose the use of UMAP as an alternative, which I use to reduce the data to a 256-dimensional space. This strategy will be referred to as CS-UMAP.

¹Both of these approaches will operate on 768-dimensional embeddings.

Algorithm 2 Dimensionality-Reduced k-Center-Greedy

```
Input: data \mathbf{x}_i, existing pool \mathbf{s}^0, budget b
Initialize \mathbf{s} = \mathbf{s}^0
repeat
u = \operatorname{argmax}_{i \in [n] \setminus \mathbf{s}} \min_{j \in \mathbf{s}} \Delta_{Reduced}(\mathbf{x}_i, \mathbf{x}_j) \qquad \triangleright \text{ Computing distances on } \mathbf{s} = \mathbf{s} \cup \{u\} \qquad \triangleright \text{ reduced embeddings } 
until |\mathbf{s}| = b + |\mathbf{s}^0|
return \mathbf{s} \setminus \mathbf{s}^0
```

3.2 Uncertainty-Based

Next, I examine the effect of pointwise probabilities on the Core-Set algorithm. Core-Set currently operates using the distances between its points – in this experiment, I propose an approach where Core-Set considers the probability distributions in addition to the distances.

To accomplish this, I use an uncertainty-based approach. Uncertainty sampling, which was introduced by Lewis and Gale [1994], essentially attempts to select the unlabelled examples with the lowest classification certainty. In this case, I specifically opted for an approach similar to that of Breaking-Ties (Luo et al. [2005]), where the instances with the smallest margin between their top two most likely classification probabilities are selected, essentially "breaking the tie" between the two most likely classes. In other words, if $\mathbf{p}_{j,k}^*$ denotes the probability of the k-th most likely class label for the j-th instance, then Breaking-Ties seeks to select instances where $\mathbf{p}_{j,1}^* - \mathbf{p}_{j,2}^*$ is minimal.

Algorithm 3 Weighted k-Center-Greedy

```
Input: \mathbf{x}_i, \mathbf{s}^0, b, breaking-ties probabilities \mathbf{p}_{bt}
Initialize \mathbf{s} = \mathbf{s}^0

repeat
d = \min_{j \in \mathbf{s}} \Delta(\mathbf{x}_i, \mathbf{x}_j)
u = \operatorname{argmax}_{i \in [n] \setminus \mathbf{s}} 0.8 \cdot d + 0.2 \cdot \mathbf{p}_{bt}
\mathbf{s} = \mathbf{s} \cup \{u\}
\mathbf{until} \ |\mathbf{s}| = b + |\mathbf{s}^0|
\mathbf{return} \ \mathbf{s} \setminus \mathbf{s}^0
\triangleright Weigh results using linear \mathbf{s}
```

This approach resulted in two different implementation ideas: the first, which I will refer to as "Weighted Core-Set" (WCS), calculates the uncertainties prior to executing the standard Core-Set algorithm, then multiplies the resulting Core-Set distances and probabilities using weights during selection (in this case, I used an 80–20 weighting in favour of the Core-Set distances).

This approach is depicted in Algorithm 3.

Algorithm 4 Re-ranked k-Center-Greedy

```
Input: \mathbf{x}_i, \mathbf{s}^0, b, class probabilities \mathbf{p}_i
Initialize \mathbf{s} = \mathbf{s}^0, r = \emptyset

repeat

u = \operatorname{argmax}_{i \in [n] \setminus \mathbf{s}} \min_{j \in \mathbf{s}} \Delta(\mathbf{x}_i, \mathbf{x}_j)
\mathbf{s} = \mathbf{s} \cup \{u\}

until |\mathbf{s}| = 2b + |\mathbf{s}^0|

repeat

u = \operatorname{argmin}_{j \in \mathbf{s} \setminus r} \mathbf{p}_{j,1}^* - \mathbf{p}_{j,2}^*
r = r \cup \{u\}

until |r| = b

repeat

Compute Core-Set of size 2b

repeat

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```

The second, which I will call "Re-ranked Core-Set" (RGC), opts to first compute a Core-Set twice the size of the original sample size b, then "re-ranks" the resulting distances according to Breaking-Ties uncertainties and finally selects the points with the b highest uncertainties. The pseudocode for this approach can be seen in Algorithm 4.

In theory, these two approaches aim to use uncertainties to improve Core-Set's selections such that the newly selected set of points should ideally contain instances which also have high uncertainties.

3.3 Class Balance-Based

Finally, I take into account the class distributions within each Core-Set and select points based on the representation of each class. This approach will be called "Class-Balanced Core-Set" (CB-CS).

The basic idea with this approach is that the class distribution within out pool of labelled instances should, in theory, have an even class distribution such that the models learns from similar amounts of instances from each class. In other words, the query strategy (in this case Core-Set) should attempt to select more or less instances of a certain class depending on the discrepancy between the class distribution of the labelled pool and some balanced distribution of that class.

One way of determining the degree to which our pool of instances is "class-balanced" is by using the normalized entropy metric. This metric is based on the Shannon entropy H (Shannon [1948]), which is defined in Equation 3.1 over some discrete random variable X, which is in this case the class distribution.

$$H(X) = -\sum_{x \in X} p(x) \log p(x)$$
(3.1)

Dividing by the logarithm of the number of classes n for the class distribution, we get the normalized entropy H_{norm} (Equation 3.2), also referred to as to as H_{REL} (Wilcox [1967]).

$$H_{norm}(X) = \frac{-\sum_{x \in X} p(x) \log p(x)}{\log n}$$
(3.2)

This metric scales the output to lie between 0 and 1, such that 1 indicates a uniform distribution. This can be applied to the measurement of class imbalances, where a normalized entropy value closer to 1 indicates a more balanced class distribution and is thus a desirable result. Thus, the aim of this approach is to increase this metric with each iteration such that the classes are balanced within the labelled pool.

Algorithm 5 Class-Balanced k-Center Greedy

```
Input: \mathbf{x}_i, \mathbf{s}^0, b, true class labels y_i, predicted class labels y_i^{pred} classes C d = \operatorname{target\_dist}_{i \in [n] \setminus \mathbf{s}}(b, C, y_i, y_i^{pred}) Initialize \mathbf{s} = \mathbf{s}^0 for c \in C do \mathbf{s}^c = \emptyset class_pool = \{[n] \setminus \mathbf{s}\}_{i \in \{i \mid y_i^{pred} = c\}} repeat u = \operatorname{argmax}_{i \in \operatorname{class\_pool}\min_{j \in \mathbf{s}} \Delta(\mathbf{x}_i, \mathbf{x}_j) \mathbf{s}^c = \mathbf{s}^c \cup \{u\} until |\mathbf{s}^c| = d^c \mathbf{s} = \mathbf{s} \cup \mathbf{s}^c end for return \mathbf{s} \setminus \mathbf{s}^0
```

To this end, I divide a single query into multiple Core-Set computations, essentially constructing disjoint Core-Set selections for each class. For each class' Core-Set selection, the budget b (e.g., the amount of selected instances from this class) depends on the desired class distribution. First, the class distributions of the model's predictions and of the true labels are used to determine how many instances should ideally be queried for each class in order to achieve a "balance" in the labelled pool. In the corresponding pseudocode (Algorithm 5), this calculation has been denoted by the use of $target_dist$, which uses an existing implementation from the Python library Small-Text

(Schröder et al. [2023]). The resulting distribution d then contains the desired number of instances for some class $c \in C$, denoted by d^c . After this, k-Center greedy is used to select the desired number of points of each class, such that if d^c denotes the number of newly selected instances for the class c, then $\sum_{c \in C} d^c = b$.

Chapter 4

Experiment

With these approaches in mind, this chapter outlines the experiment; first describing the data and setup of the experiment, and finally delving into its results.

This experiment takes place within a simulated AL environment, meaning the oracle is not a human expert or annotator, but rather an already labelled pool of data. To this end, I select three established pre-labelled text classification datasets of different varieties. The AL takes place on these datasets using two different classifier models, each of which I then combine with one of eight different query strategies. The query strategies to be compared contain two baseline approaches, Core-Set itself, and the implementations of the previously discussed Core-Set variations.

The following two sections explain in greater detail the data and setup used as a basis for the conducted experiment. The performances are then measured using two metrics, accuracy and AUC, throughout five runs for each combination of dataset, classifier and query strategy. In the final section, I present and evaluate the experiment results.

4.1 Data

This experiment was conducted across three datasets commonly used in the field of text classification. These datasets are of three different types: sentiment analysis, questions, and news.

For binary classification, I used **Movie Review** (Pang and Lee [2005]), a sentiment analysis dataset containing 5,331 positive and 5,331 negative online movie reviews. For multi-class text classification, I performed the AL on **AG's News** (Zhang et al. [2015]), a news dataset comprised of 120,000 training samples and 7,600 test samples, and **TREC** (Li and Roth [2006]), a question dataset containing 5,500 training samples and 500 test samples. The test set

was provided in the case of AG's News and TREC, in the case of Movie Review I employed a split of the 10,662 samples myself, which can be seen alongside additional information in Table 4.1. Example instances from each dataset as well as their corresponding classes can also be seen in Table 4.2.

Dataset Name (ID)	Classes	Train	Test	MNC (*)
Movie Review (MR)	2	9,596	1,066	114.16
AG News (AGN)	4	120,000	7,600	236.41
TREC (TREC)	6	$5,\!452$	500	49.39

Table 4.1: Information on the different datasets. (*) Mean number of characters in a single instance.

Dataset Name (ID)	Class	Example Instance
Movie Review (MR)	1 (positive)	if you sometimes like to go to the movies to have fun , wasabi is a good place to start .
AG News (AGN)	2 (Business)	Wall St. Bears Claw Back Into the Black (Reuters) Reuters - Short-sellers, Wall Street's dwindling\band of ultra-cynics, are seeing green again.
TREC (TREC)	2 ('DESC')	How did serfdom develop in and then leave Russia ?

Table 4.2: Examples of instances and their corresponding labels from each dataset. The example label 'DESC' signifies a description or abstract concept.

4.2 Experiment Setup

I selected two state-of-the-art transformers, BERT (Devlin et al. [2019]) and SetFit (Tunstall et al. [2022]) to fine-tune as models for this experiment. BERT is an established language model pre-trained on 3,300M English words and may thus serve as a good baseline model for this experiment. It uses bidirectional self-attention in order to incorporate context from both directions of a given token, unlike many previous context-sensitive approaches which only considered a single direction. For this experiment, I use BERT_{BASE}, which consists of 12 layers, hidden units of size 768 with 110M parameters in total. SetFit, on the other hand, is based on sentence transformers which are then fine-tuned in a contrastive manner. This model also has 12 layers, 110M parameters and generates 768-dimensional embeddings. Due to the nature of sentence transformers explained previously in Section 2.1, this model may be able to aid Core-Set's selection as a consequence of the improved vector space representations when considering similarity measures (Reimers and Gurevych [2019]). The model implementations used in this experiment are HuggingFace's bertbase-uncased and paraphrase-mpnet-base-v2.

The experiment is conducted by performing 20 queries on 25 instances, with a validation set size of 10%. The results are averaged over five runs of queries per combination of dataset, model and query strategy. The training and evaluation of these models is run using an AL experiment setup based on the Python library Small-Text (Schröder et al. [2023]). This also includes the implementation of k-Center greedy as well as various methods concerning class redistributions.

Alongside the original Core-Set (CS), I compare my different approaches with Random Sampling (RS) and Breaking-Ties (BT). RS offers a good view of a baseline performance and is especially of interest when compared to Core-Set. BT, on the other hand, may serve as a good upper bound when looking at improving Core-Set's performance.

4.3 Experiment Results

Based on the experimental setup outlined in Section 4.2, this chapter presents the outcomes for each experiment run. I first present the learning curves for the each training run, then report on the corresponding result tables.

The following figures show the learning curves for each combination of dataset, model and query strategy.

Overall, the SetFit learning curves generally outperform the BERT model and seem to show much less variation between the different query strategies. This is reflected not only in the mean curve progressions of each model, but

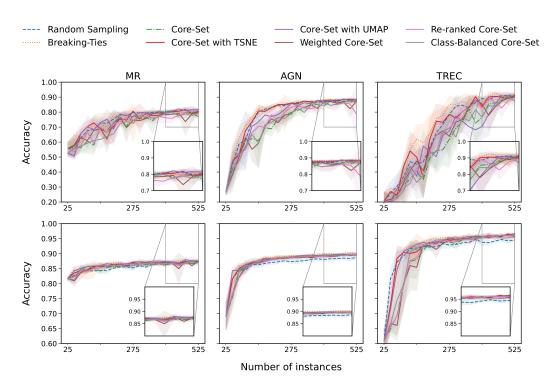


Figure 4.1: Active Learning curves of BERT (top row) and SetFit (bottom row) on each dataset when combined with eight query strategies: Random Sampling, Breaking-Ties, Core-Set, Core-Set with t-SNE, Core-Set with UMAP, Weighted Core-Set, Re-ranked Core-Set and Class-Balanced Core-Set. The lines represent the mean accuracy and the surrounding tubes represent the standard deviation over five runs.

also in the smaller standard deviations of each individual line. Even in the case of BERT's resulting AL curves, the most noticeable accuracy differences seem to mainly occur in early iterations. Generally, the mean accuracy scores of the different strategies tend to lie in a similar range by the final iteration.

I first compare and contrast the different results for the training of the BERT model (Figure 4.1). We can clearly see general upwards trends to varying degrees depending on the dataset. The highest final accuracies are achieved on the TREC dataset, whereas the learning curves for AGN have the fastest increase in early iterations. Both seem to resemble a saturation curve, with TREC's mean accuracy values starting to slowly level out around 90%, whereas AGN's stop around 85% near the second half of the learning process. From this point on, the curves of both datasets gradually rise by around 5% towards the end of training. On the other hand, the learning curves on MR show a more gradual, steady rise throughout the entire process and finish with slightly lower overall accuracies, with all results coming out to just under or around 80%.

When comparing the curves of the different query strategies, we can see that specifically in the case of BERT, CS does indeed seem to underperform when compared to the baseline approaches. This is mainly noticeable when looking at the earlier iterations (between queries 1 to 10). The underperformance of CS becomes even more apparent when considering the fact that the learning curves of RS are consistently above those of CS. This further reinforces the sentiment that Core-Set may have weaknesses within the domain of text classification.

In the case of AGN and TREC, we can clearly see the curve of BT achieve high performances throughout, although CS-tSNE is able to compete very closely on AGN. Interestingly enough, RS has managed to achieve similar scores to the strategies mentioned previously in these cases.

We also observe that in most cases, the different variations of Core-Set seem to be on par with or more performant than the original Core-Set. Both dimensionality reduction-based approaches, especially CS-tSNE, look to be a strong contenders in most cases and manages to perform similarly to or better than Core-Set and the remaining variants.

CS-UMAP performs favorably especially in the case of MR, where it remains on the upper end of accuracy scores throughout and manages to outperform all other strategies by the final iteration. In the case of AGN and TREC, we still find improvements to Core-Set during training, although these datasets seem to generally favour the t-SNE approach. Interestingly, the learning curve takes a dip in the latter half of training on the TREC dataset and rises rapidly again in the final iterations. Notably, a comparable sharp decrease is apparent in the first half of training on the same dataset for CS-tSNE's curve.

The class-balanced approach, on the other hand, does not seem to show

significant accuracy improvements during training in comparison to the regular Core-Set approach. One discernible difference with the learning curve of CB-CS is noticeable on the MR dataset, where its curve seems to have much less fluctuations than CS and its other variations. Generally, however, CS and its class-balanced version show very similar learning curve trends across all three datasets.

Weighted Core-Set and Re-ranked Core-Set are in a similar vein to, albeit oftentimes slightly above, the Class-Balanced approach. Both curves fluctuate around the same level or slightly higher than CS, but do not manage to surpass the baseline approaches in early iterations. We can see that in the case of AGN, the re-ranked strategy's learning curve even takes a dip in mean accuracy towards the end, resulting in a mean final accuracy below that of all other strategies by the final iteration despite being relatively competitive in prior iterations.

The SetFit learning curves (Figure 4.1) show much less fluctuation throughout the individual learning curves, as well as smaller discrepancies between the different query strategies during training.

In the case of MR, all strategies have very similar accuracy curves and bundle tightly around the final iterations, with all final values somewhere around 87,5%. For this dataset, the increase throughout the entire process is very minimal, amounting to only around 5% from the first query to the end of training. As for AGN and TREC, more learning progress is visible from beginning to end. Moreover, the margins between the curves are slightly wider, and some differences can be noted when comparing the different strategies. For these two datasets, the curves again show large early increases around the first five iterations, with the values starting to level out somewhere between instance 150 and 275. For these datasets, the values by the last iteration are also higher than for MR, with final results around the 90% mark on AGN and around 95% on TREC.

Again, BT stands out as one of the best strategies, with CS-tSNE generally following a similar trend. In contrast to BERT, CS itself does not seem to underperform throughout in any significant way. Only in the first half of the learning process on TREC can we see some kind of noticeable difference between CS and the other curves. In these earlier instances, CS is outperformed by the baseline strategies as well as the dimensionality reduction-based strategies.

In this diagram we can also observe the different strategies fall into two "groups" of curve progressions in the beginning iterations. Similarly to BERT's learning curves, we can see WCS, RCS and CB-CS following a very close trend to that of CS. The other query strategies (RS, BT, CS-tSNE, CS-UMAP) seem to follow a slightly higher, but similarly bundled, trend. This bundling of query

strategies is only noticeable on the TREC dataset curves, whereas the other graphs seem to show all or most strategies bundled closer together overall.

One slight outlier in these graphs is RS, of which the accuracy values stay visibly below the other query strategies in the second half of each run, specifically when considering AGN and TREC. For these two datasets, RS seems to be competitive in early iterations, outperforming CS and many of the other strategies, but progress rapidly slows, resulting in lower final scores than the other strategies.

The following page shows two tables containing the mean accuracy (Table 4.3) and mean AUC values (Table 4.4) corresponding to the learning curves.

Dataset	Model				Query Strategy	;y			
		RS	BT	CS	CS-tSNE	CS-UMAP	WCS	RCS	CS-CB
AGN	BERT SetFit	$0.884 \pm 0.004 \\ 0.886 \pm 0.006$	$\begin{array}{c} \textbf{0.889} \pm \textbf{0.010} \\ \textbf{0.902} \pm \textbf{0.004} \end{array}$	0.874 ± 0.012 0.895 ± 0.003	$\begin{array}{c} 0.881 \pm 0.010 \\ 0.895 \pm 0.003 \end{array}$	0.884 ± 0.010 0.899 ± 0.001	0.873 ± 0.011 0.895 ± 0.005	0.785 ± 0.221 0.866 ± 0.016 0.895 ± 0.004 0.898 ± 0.006	0.866 ± 0.016 0.898 ± 0.006
MR	BERT SetFit	BERT 0.806 ± 0.011 SetFit 0.869 ± 0.006	0.815 ± 0.009 $\mathbf{0.880 \pm 0.005}$	0.770 ± 0.015 0.871 ± 0.005	$0.796 \pm 0.020 \\ 0.874 \pm 0.005$	0.819 ± 0.011 0.876 ± 0.008	0.806 ± 0.014 0.874 ± 0.007	0.811 ± 0.013 0.793 ± 0.021 0.870 ± 0.004 0.870 ± 0.006	$0.793 \pm 0.021 \\ 0.870 \pm 0.006$
TREC	$egin{aligned} ext{BERT} \ ext{SetFit} \end{aligned}$	$\begin{array}{c} 0.904 \pm 0.018 \\ 0.945 \pm 0.004 \end{array}$	0.920 ± 0.014 0.954 ± 0.006	$\begin{array}{c} 0.902 \pm 0.021 \\ 0.962 \pm 0.004 \end{array}$	$\begin{array}{c} 0.912 \pm 0.009 \\ 0.957 \pm 0.007 \end{array}$	0.898 ± 0.033 0.962 ± 0.010	0.897 ± 0.027 0.966 \pm 0.004	0.897 ± 0.036 0.962 ± 0.003	$0.872 \pm 0.048 \\ 0.956 \pm 0.007$

Table 4.3: Final accuracy per dataset, model, and query strategy. We report the mean and standard deviation over five runs. The best result per dataset is printed in bold.

Dataset Model	Model				Query Strategy				
		RS	BT	CS	CS-tSNE	CS-UMAP	WCS	RCS	CS-CB
AGN	BERT SetFit	$\begin{array}{c} 0.790 \pm 0.015 \\ 0.865 \pm 0.007 \end{array}$	$\begin{array}{c} \textbf{0.800} \pm \textbf{0.009} \\ \textbf{0.881} \pm \textbf{0.004} \end{array}$	0.735 ± 0.020 0.871 ± 0.005	0.792 ± 0.007 0.875 ± 0.004	0.772 ± 0.019 0.879 ± 0.004	0.731 ± 0.014 0.870 ± 0.003	$0.741 \pm 0.015 \\ 0.870 \pm 0.002$	$0.733 \pm 0.017 \\ 0.873 \pm 0.003$
MR	BERT SetFit	0.750 ± 0.007 0.854 ± 0.002	$\begin{array}{c} 0.746 \pm 0.011 \\ 0.864 \pm 0.005 \end{array}$		$ 0.718 \pm 0.009 \qquad 0.741 \pm 0.017 $ $ 0.856 \pm 0.003 \qquad 0.862 \pm 0.003 $	0.748 ± 0.005 0.866 \pm 0.005	0.720 ± 0.004 0.858 ± 0.007	$0.718 \pm 0.005 \\ 0.857 \pm 0.003$	$\begin{array}{c} 0.706 \pm 0.015 \\ 0.859 \pm 0.002 \end{array}$
TREC	BERT SetFit	$\begin{array}{c} 0.674 \pm 0.029 \\ 0.914 \pm 0.011 \end{array}$	$\begin{array}{c} 0.709 \pm 0.008 \\ 0.923 \pm 0.007 \end{array}$	$0.594 \pm 0.022 \\ 0.896 \pm 0.015$	0.676 ± 0.037 0.919 ± 0.005	0.609 ± 0.029 0.921 ± 0.008	0.629 ± 0.024 0.893 ± 0.012	$0.624 \pm 0.012 \\ 0.897 \pm 0.012$	$\begin{array}{c} 0.598 \pm 0.025 \\ 0.905 \pm 0.010 \end{array}$

Table 4.4: Final AUC per dataset, model, and query strategy. We report the mean and standard deviation over five runs. The best result per dataset is printed in bold.

In Table 4.3, BT dominates for almost every dataset on both models. Only in two cases does another strategy achieve the highest overall final mean accuracy. Even though the differences are predominantly characterized by very small margins throughout, there are still noteworthy observations to be made.

First, we can again see that RS outperforms CS when used with BERT throughout all datasets. CS seems to encounter minor difficulties specifically on the MR dataset with BERT, where it marks the lowest result of all the strategies. Despite this, CS' training with the SetFit model yields improved results, particularly when contrasted with those achieved by RS with SetFit.

The results of the CS variations show small improvements in accuracy at various points. CS-tSNE and CS-UMAP most notably show slightly higher scores than CS in almost all cases. For CS-tSNE, the only exception is on TREC with SetFit. This row of results has some other noteworthy differences between query strategies. We can see that is the only combination of model and dataset for which CS, along with all of its variations, scores a higher result than BT. In the case of CS-UMAP, the only instance where we find no improvement to CS is on the TREC dataset. However, we observe quite consistent accuracy scores above 80% for this strategy across the board. Additionally, this approach manages to improve upon Core-Sets relatively low accuracy score on the MR dataset with BERT, increasing from 77% to nearly 82%.

Although WCS does have the best result in the case of the TREC dataset with SetFit, the remaining results in its column do not show consistent improvements when compared to CS. A similar sentiment applies to RCS and CS-CB, which show varied results in comparison to CS. The former method demonstrates a noticeable decrease to CS of around 9% for SetFit and AGN.

Even so, all of the CS variations also show some kind of improvement in the case of MR with BERT, in which CS has the lowest accuracy overall. Notably, AGN is the only dataset where CS-tSNE, WCS and RCS do not have any impact on the mean accuracy score in the case of SetFit. Even in cases where results are not exactly the same, they often remain within a one-standard-deviation range of each other. One row where this is most evident is the combination of SetFit and MR across all query strategies. Generally, the SetFit results in all rows exhibit the smallest discrepancies, as is reflected in the learning curves presented previously.

Table 4.4 contains the reported mean AUC (area under curve) and the corresponding standard deviation for each combination of dataset, model and query strategy. Again, SetFit exhibits higher values than BERT overall, with considerably high results on the TREC dataset around the 90% mark. The discrepancy between the two models is also most apparent for this dataset, with margins of 30% or more in some instances. Regarding the other datasets,

we again see MR with most of the lowest values overall, however AGN's results generally seem to fall within a similar range.

The top performing AUC results, similarly to the accuracy table, show BT as having the best results in almost all cases. Unexpectedly, RS manages to reach the highest AUC among all query strategies in the case of MR with BERT. For BERT, we observe even more noticeable discrepancies to CS across the board than in the accuracy tables. Additionally, the UMAP approach ranks highest in the case of MR with the SetFit model. However, both of these ranks are by relatively small margins to the rest of the results, especially the latter scenario.

Again, the CS variations offer some minor improvements in multiple cases. Here, the similarities between the learning curves of CS, WCS, RCS and CB-CS become even more apparent, as the values of these strategies are almost equal in most instances. Nonetheless, the two dimensionality reduction approaches show higher AUC values than CS throughout. The largest improvement for CS-tSNE was achieved with BERT, namely on TREC (8.2%), with the second largest being on AGN (5.7%). The improvements with CS-UMAP are even more minor, mainly noticeable with BERT on AGN (3.7%) and MR (3%).

Chapter 5

Discussion

Although none of the proposed Core-Set variations manage to get scores consistently as high as the Breaking-Ties approach, we can still gather interesting insights from the conducted experiment.

One presumption prior to the conducting of the experiment was that Core-Set may have mixed results in cases of text classification. Not only that, but according to Prabhu et al. [2021], Core-Set's results with BERT sometimes lie even below the performances of Random Sampling. This experiment's results further support this statement, with Core-Set being outperformed by Random Sampling with BERT, both in mean accuracy and mean AUC.

In order to discuss the research questions posed in Chapter 1, I have structured the rest of this chapter according to the results of each approach presented in Chapter 3. Pertaining to the third research question, I have also conducted further analysis of the experiment results in order to determine whether the approach did indeed result in a more balanced distribution of classes in the labelled pool.

5.1 Dimensionality Reduction-Based Approach

The previously presented experiment has offered further insights with regard to the first research question. The first modification to Core-Set, which used t-SNE to reduce word embeddings prior to the selection with k-Center greedy, generally managed to improve Core-Set over the three given datasets. Though the differences in the case of SetFit were very minor, we can observe more noticeable improvements in efficiency (i.e. mean AUC results) with BERT, where Core-Set seemed to have its weaknesses originally. The second technique used for this approach resulted in similar improvements to the Core-Set approach, which were most noticeable on the MR dataset with BERT. Again, the overall accuracy and AUC differences were minor in most instances, but

overall positive nonetheless.

Between the two dimensionality-based approaches, the differences observed were even more minor. Based on the experiment results, it is not yet clear which dimension is optimal for the reduced space, as the reduction to both two and 256 dimensions led to similarly positive outcomes. Due to this, it is also unclear which of the two techniques is superior for this particular task; to determine this, the techniques should be compared on the same reduction dimensions.

The demonstrated improvements of Core-Set when applied to dimensionality-reduced embeddings may further support the sentiment that Core-Set encounters difficulties when faced with the task of higher-dimensional feature spaces (Sinha et al. [2019]), as was also mentioned in Chapter 1. However, the exact impact of the degree to which the dimension is reduced (i.e., what dimensions Core-Set operates most optimally on) still remains unclear. Additionally, these techniques inevitably lead to longer runtimes, especially in the case of the lesser-optimized t-SNE. In the context of this thesis' experiment, this factor did not lead to any major issues or difficulties; however, in the case of larger datasets or larger feature spaces, this approach may cause considerable runtime increases. In these cases, understanding the tradeoff between performance boosts and longer runtimes becomes increasingly important.

5.2 Uncertainty-Based Approach

With respect to the second research question, I presented and implemented two uncertainty-based approaches. Both attempts to combine an uncertainty-based approach with Core-Set have shown minor, but generally insignificant improvements, with certain cases even showing slight drops in performance.

Though WCS and RCS had generally similar results overall, they still lean slightly in favour of WCS due to the improvements on TREC with SetFit and AGN with BERT, in which RCS fell short. Another aspect outside of performance that may favour WCS over RCS is the ease of implementation and interpretability, which is more straightforward for the weighted approach. In addition, WCS does not perform what are essentially two instance selection runs per query, which is the case in the re-ranked approach and might lead to slightly longer runtimes.

It may be that the combination of Core-Set with the uncertainty-based approach that I attempted was simply too minor to have a noticeable impact on the resulting accuracy scores. In the case of WCS, the linear combination may place an overwhelming emphasis on Core-Set, leading to results that do not differ much from the original k-Center algorithm. In the case of RCS, it

may also be that re-ranking only 2b instances is not sufficient for changes in performance, which might explain why this approach also does not manage to outperform either of the approaches it is based on.

With these mixed results in mind, my conclusion regarding this research question is negative.

5.3 Class Balance-Based Approach

Finally, with regard to the third research question, it becomes clear that the proposed class balance-based approach does not manage to improve upon the Core-Set selection. The accuracy and AUC values are, in most cases, either on par with or slightly below those of Core-Set. This is also reflected in the learning curves, where no clear improvement to Core-Set is visible throughout. In the case of MR, one might initially assume little to no impact for class balancing due to the fact that this dataset only has two classes, and as a consequence, already has relatively balanced class distributions regardless. However, the experiment also considered AGN and TREC, two multi-class datasets, which showed similarly unchanged performances. So, the class balancing employed for this approach did not seem to improve Core-Set, even in the case of multi-class datasets.

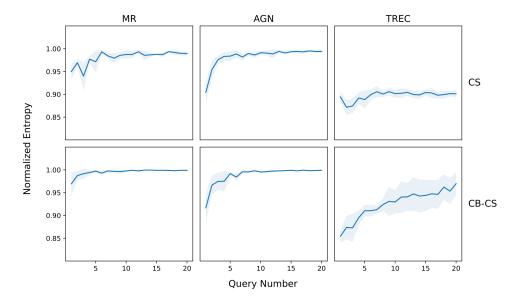


Figure 5.1: Normalized entropy curves for instances selected during AL with BERT using Core-Set and Class-Balanced Core-Set. The lines represent the mean accuracy and the surrounding tubes represent the standard deviation over five runs.

In order to investigate the functionality of the class-balanced approach, I

tracked the class distributions after each query of the previously conducted experiment. As a result, I was able to observe an overall positive impact of the balancing on the class distribution within the labelled pool. This impact was measured using the normalized entropy within the labelled pool after each iteration, as explained in Chapter 3. Similar to the learning curves in Chapter 4, I have plotted the mean over five runs in Figure 5.1.

We can see that for both strategies, the normalized entropy generally increases or stays relatively constant with each query. In the case of MR, we observe only minor changes in the class distribution throughout the learning process. This may be in part attributed to the fact that this dataset only has two classes that are distributed evenly. Nonetheless, we observe the class-balanced approach to have a more stable mean normalized entropy in the first half of the learning process, whereas the regular Core-Set selection has slight fluctuations. Nevertheless, both curves run somewhere within the range of 0.95 and 1, indicating a very close to even distribution in both cases.

For AGN, the difference between Core-Set and the class-balanced approach seem to be even less evident. In both cases, we observe a saturation curve beginning around 0.9 and evening out close to 1 around the fifth query. Although AGN has twice as many classes as MR, it is also a class balanced dataset with equal amounts of instances from each class, which may explain the depicted results.

The dataset in which a change in class distribution within the labelled pool is most distinct is TREC. Here, we note a relatively constant curve around or below a normalized entropy of 0.9 in the case of Core-Set, whereas the class-balanced approach manages to select an increasingly even distribution. In this case, the normalized entropy gradually rises from roughly 0.85 to around 0.97. Still, the standard deviation increases in later iterations, becoming clearly higher than in all other cases.

One reason for these differences in the efficacy of the class-balanced approach are the underlying class distributions of each dataset. In the case of MR and AGN, we have uniform distributions across all classes, whereas TREC is an inherently class-imbalanced dataset.¹ Consequently, the class-balanced approach has very little impact on the distributions of the selected instances, which are nearly uniformally distributed in the first place. TREC, in contrast, has slightly imbalanced classes, resulting in the possibility for improvement using the class-balanced approach.

¹The six classes are distributed as follows: 'ENTY' (22.9%), 'HUM', (22.4%), 'DESC' (21.3%), 'NUM' (16.4%), 'LOC' (15.3%), 'ABBR' (1.6%) (Li and Roth [2006]).

5.4 Limitations

Naturally, there are some limitations to consider with this experiment. On one hand, the training data used only encompassed three different datasets. These datasets do attempt to cover a variety of purposes, class numbers and sizes, but in order to further verify the effectiveness of the proposed approaches, more datasets should be used.

Another aspect that was not considered by my experiment is the effect of each approach on the respective runtime. This may be especially relevant when considering a dimensionality reduction algorithm such as t-SNE, which could have a significant impact when training on larger datasets. Furthermore, this experiment's result evaluation only took into account the respective accuracy and AUC metrics. For the purpose of evaluating the results of each strategy, it may be worth considering other commonly used metrics such as the F1-score.

Finally, it is worth underlining the fact that this thesis examined Core-Set as the basic k-Center greedy approach, whereas Sener and Savarese [2018] propose a slightly optimized, robust k-Center approach that minimizes outliers. This approach was not used for implementation reasons, as the solution for robust k-Center's feasability check depends on Gurobi (Gurobi Optimization, LLC [2023]), a licensed optimization framework. As a result, the results of Core-Set and the corresponding modifications used in this experiment may not be optimal.

5.5 Future Research

As mentioned earlier, this experiment was conducted on three datasets, two of which have uniform class distributions. With regard to the class-balanced approach, it may be worth examining the effect on various datasets with more imbalanced class distributions. Not only may this result in more significant improvements to the normalized entropy, but possibly a more noticeable impact on the learning process itself. Regarding the dimensionality reduction-based approaches, it may be worth examining the effect of reducing to different dimensions, as well as potentially tuning some of the many hyperparameters. In the case of UMAP for instance, it may be worth examining the effect of reducing to 128, 64, 32 dimensions, or even less. For t-SNE, hyperparameters such as perplexity may also have a significant impact on the technique's results. Concerning the two uncertainty-based approaches, it may be worth looking into the effect of a different Core-Set to Breaking-Ties ratio for the weighted linear combination in WCS (80–20), or modifying the amount of instances to re-rank in RCS (2b).

Furthermore, it could be worth investigating the effect of combining two or

more of the approaches presented here. If two strategies such as CS-tSNE and CB-CS only offer minor improvements in some cases, maybe a combination of the two approaches could contribute to more efficient learning.

Of course, some of the aspects mentioned in the previous section could be added to this experiment for further research. Examining other metrics such as the F1-score and runtimes, as well as considering other classifiers and datasets may offer additional insights in determining the usability of the presented approaches.

Chapter 6

Conclusion

In this thesis, I examined the effect of Core-Set as an AL query strategy for text classification tasks and explored possibilities for improving the approach within this domain. To this end, I created an AL experiment in which I compared Core-Set with five variations and two baseline approaches using two models across three different datasets. The motivation for doing this was to see if Core-Set does indeed achieve mixed results within the field of text classification and to attempt to work toward a possible improvement in this regard.

I began by outlining the fields of active learning as well as text classification, as well as giving an overview of the Core-Set approach and various established dimensionality reduction techniques. I then presented three categories of approaches (dimensionality reduction-based, uncertainty-based, class balance-based), which resulted in five different modifications to the original k-Center greedy algorithm. I implemented and tested the various strategies within an AL experiment setup using the datasets and classifiers mentioned previously and discussed their results using various metrics.

The experiment's results show Core-Set producing mixed results in many cases when compared to the baseline strategies. This aligns with what was shown in Prabhu et al. [2021] and briefly mentioned in Coleman et al. [2022]. Moreover, the results conclude that we can observe some slight improvements of Core-Set's performances when used in conjunction with two nonlinear dimensionality reduction techniques, t-SNE and UMAP. These techniques were selected not only for the sake of variation, but also to examine potential differences in results based on the dimensions of the embedding reductions. Furthermore, the uncertainty-based approach and class balance-based approach do not seem to significantly impact Core-Set's results. The uncertainty-based approaches, based on a weighted and a re-ranking scheme, attempted to incorporate uncertainties from breaking-ties, another well-established query strategy, into the "decision making" of Core-Set. However, these approaches did

not manage to achieve consistently higher results than Core-Set. Finally, the class balance-based approach attempted to create Core-Set selections with balanced class distributions with the intention of learning from instances with all kinds of class labels. Although this did not result in any significant performance changes, I was able to observe an overall positive impact on the class distributions of the labelled instance pools in the case where the dataset had imbalanced classes by measuring the respective normalized entropy values.

In general, the modifications to the Core-Set approach presented and discussed within this thesis have yielded similarly mixed experiment results overall. Nonetheless, the insights gained do show some positive aspects and leave room for additional research and examination considering each strategy. With an ever-growing need for efficient text classification, improving state-of-the-art approaches to machine learning will continue to be an important endeavour.

Appendix A

Implementation Details

The experiment setup is based on a pre-existing AL environment created with Schröder et al. [2023]. This also includes the implementation of k-Center greedy as well as various methods concerning class redistributions. In addition, well-known machine learning libraries such as Scikit-Learn, HuggingFace, NumPy, and SciPy were used for the implementation of the query strategies. These libraries were used within a Python 3.8 environment.

The models that were fine-tuned within the experiment are bert-base-uncased and paraphrase-mpnet-base-v2. The datasets were also obtained via huggingface datasets.

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