

Homework 1

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a) After running the linear regression model on python to predict the dependent variable Temp, using CO₂, CH₄, N₂O, CFC-11, CFC-12, Aerosols, TSI and MEI as features, we found the following in-sample and out-of-sample R², MSE, and MAE.

in-sample R²: 0.6920595959984741

in-sample MSE: 0.008731426409911177

in-sample MAE: 0.07260918612938931

out-of-sample R²: -0.541325583402297

out-of-sample MSE: 0.012206974835137179

out-of-sample MAE: 0.09312747891276273

(b) After running the linear regression model on python to predict the dependent variable Temp, using N₂O, Aerosols, TSI, and MEI as features, we found the following in-sample and out-of-sample R², MSE, and MAE.

in-sample R²: 0.6490120806760372

in-sample MSE: 0.009952007429105784

in-sample MAE: 0.07666650280233205

out-of-sample R²: 0.20031861104556226

out-of-sample MSE: 0.006333308611894036

out-of-sample MAE: 0.06154027269393422

(c) Between the two models built in parts (a) and (b), the model built in part (a) performs better in-sample, as its R-squared is higher and error metrics are smaller. However, the model in part (a) has a negative R-squared for out-of-sample, indicating poor performance compared to using averages as predicted values. In contrast, the model in part (b) explains roughly 20% of the out-of-sample variability in predicted values. Therefore, the model in part (b) performs better out-of-sample.

(d) Model 1 has N₂O coefficient = -3.48478075e-02

Interpretation: If we keep all the parameters and features constant and increase the N₂O content by 1 unit, the temperature will decrease by -3.48478075e-02 units.

Model 2 has N₂O coefficient = 0.02427612

Interpretation: If we keep all the parameters and features constant and increase the N₂O content by 1 unit, the temperature will increase by 0.02427612 units.

(e) We feel that we should prefer the Model 2, ie. use only N₂O, Aerosols, TSI, and MEI as features to predict the temperature. The first model suggests that as the quantity of N₂O increases, the temperature drops which is against the scientific opinion, given N₂O is a greenhouse gas that increases temperature and not decreases.

Additionally, out-of-sample R² of the first model is negative, making the model unreliable to understand the true impact of independent variables, including N₂O, on the dependent variable.

The second model still includes N2O's impact on temperature and has a better out-of-sample R^2 , meaning it is more effective in making accurate predictions on new data.