WaveSimC

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Chapter 4

Module Documentation

4.1 Np

Namespaces

- namespace np

  Custom implementation of numpy in C++.

Functions

- template<class T , long unsigned int ND>
  boost::multi_array< T, ND > operator* (boost::multi_array< T, ND > const &lhs, boost::multi_array< T, ND > const &rhs)

  Multiplication operator between two multi arrays, element-wise.
- template<class T , long unsigned int ND>
  boost::multi_array< T, ND > operator* (T const &lhs, boost::multi_array< T, ND > const &rhs)

  Multiplication operator between a multi array and a scalar.
- template<class T , long unsigned int ND>
  boost::multi_array< T, ND > operator* (boost::multi_array< T, ND > const &lhs, T const &rhs)

  Multiplication operator between a multi array and a scalar.
- template<class T , long unsigned int ND>
  boost::multi_array< T, ND > operator+ (boost::multi_array< T, ND > const &lhs, boost::multi_array< T, ND > const &rhs)

  Addition operator between two multi arrays, element wise.
- template<class T , long unsigned int ND>
  boost::multi_array< T, ND > operator+ (T const &lhs, boost::multi_array< T, ND > const &rhs)

  Addition operator between a multi array and a scalar.
- template<class T , long unsigned int ND>
  boost::multi_array< T, ND > operator+ (boost::multi_array< T, ND > const &lhs, T const &rhs)

  Addition operator between a scalar and a multi array.
- template<class T , long unsigned int ND>
  boost::multi_array< T, ND > operator- (boost::multi_array< T, ND > const &lhs, boost::multi_array< T, ND > const &rhs)

  Minus operator between two multi arrays, element-wise.
- template<class T , long unsigned int ND>
  boost::multi_array< T, ND > operator- (T const &lhs, boost::multi_array< T, ND > const &rhs)

Minus operator between a scalar and a multi array, element-wise.

- template<class T , long unsigned int ND>
  boost::multi_array< T, ND > operator- (boost::multi_array< T, ND > const &lhs, T const &rhs)

  Minus operator between a multi array and a scalar, element-wise.
- template<class T , long unsigned int ND>
  boost::multi_array< T, ND > operator/ (boost::multi_array< T, ND > const &lhs, boost::multi_array< T, ND > const &rhs)

  Division between two multi arrays, element wise.
- template<class T , long unsigned int ND>
  boost::multi_array< T, ND > operator/ (T const &lhs, boost::multi_array< T, ND > const &rhs)

  Division between a scalar and a multi array, element wise.
- template<class T , long unsigned int ND>
  boost::multi_array< T, ND > operator/ (boost::multi_array< T, ND > const &lhs, T const &rhs)

  Division between a multi array and a scalar, element wise.

4.1.1 Detailed Description

4.1.2 Function Documentation

4.1.2.1 operator∗() [1/3]

```
template<class T , long unsigned int ND>
boost::multi_array< T, ND > operator* (
            boost::multi_array< T, ND > const & lhs,
            boost::multi_array< T, ND > const & rhs )  [inline]
```

Multiplication operator between two multi arrays, element-wise.

Definition at line 447 of file np.hpp.

```
00448 {
00449     std::function<T(T, T)> func = std::multiplies<T>();
00450     return np::element_wise_duo_apply(lhs, rhs, func);
00451 }
```

4.1.2.2 operator∗() [2/3]

```
template<class T , long unsigned int ND>
boost::multi_array< T, ND > operator* (
            boost::multi_array< T, ND > const & lhs,
            T const & rhs )  [inline]
```

Multiplication operator between a multi array and a scalar.

Definition at line 463 of file np.hpp.

```
00464 {
00465     return rhs * lhs;
00466 }
```

4.1.2.3 operator∗() [3/3]

```
template<class T , long unsigned int ND>
boost::multi_array< T, ND > operator* (
            T const & lhs,
            boost::multi_array< T, ND > const & rhs )  [inline]
```

Multiplication operator between a multi array and a scalar.

Definition at line 455 of file np.hpp.

```
00456 {
00457     std::function<T(T)> func = [lhs](T item)
00458     { return lhs * item; };
00459     return np::element_wise_apply(rhs, func);
00460 }
```

4.1.2.4 operator+() [1/3]

```
template<class T , long unsigned int ND>
boost::multi_array< T, ND > operator+ (
            boost::multi_array< T, ND > const & lhs,
            boost::multi_array< T, ND > const & rhs )
```

Addition operator between two multi arrays, element wise.

Definition at line 471 of file np.hpp.

```
00472 {
00473     std::function<T(T, T)> func = std::plus<T>();
00474     return np::element_wise_duo_apply(lhs, rhs, func);
00475 }
```

4.1.2.5 operator+() [2/3]

```
template<class T , long unsigned int ND>
boost::multi_array< T, ND > operator+ (
            boost::multi_array< T, ND > const & lhs,
            T const & rhs )  [inline]
```

Addition operator between a scalar and a multi array.

Definition at line 488 of file np.hpp.

```
00489 {
00490     return rhs + lhs;
00491 }
```

4.1.2.6 operator+() [3/3]

```
template<class T , long unsigned int ND>
boost::multi_array< T, ND > operator+ (
            T const & lhs,
            boost::multi_array< T, ND > const & rhs )  [inline]
```

Addition operator between a multi array and a scalar.

Definition at line 479 of file np.hpp.

```
00480 {
00481     std::function<T(T)> func = [lhs](T item)
00482     { return lhs + item; };
00483     return np::element_wise_apply(rhs, func);
00484 }
```

4.1.2.7 operator-() [1/3]

```
template<class T , long unsigned int ND>
boost::multi_array< T, ND > operator- (
            boost::multi_array< T, ND > const & lhs,
            boost::multi_array< T, ND > const & rhs )
```

Minus operator between two multi arrays, element-wise.

Definition at line 496 of file np.hpp.

```
00497 {
00498     std::function<T(T, T)> func = std::minus<T>();
00499     return np::element_wise_duo_apply(lhs, rhs, func);
00500 }
```

4.1.2.8 operator-() [2/3]

```
template<class T , long unsigned int ND>
boost::multi_array< T, ND > operator- (
            boost::multi_array< T, ND > const & lhs,
            T const & rhs )  [inline]
```

Minus operator between a multi array and a scalar, element-wise.

Definition at line 513 of file np.hpp.

```
00514 {
00515     return rhs - lhs;
00516 }
```

4.1.2.9 operator-() [3/3]

```
template<class T , long unsigned int ND>
boost::multi_array< T, ND > operator- (
            T const & lhs,
            boost::multi_array< T, ND > const & rhs )  [inline]
```

Minus operator between a scalar and a multi array, element-wise.

Definition at line 504 of file np.hpp.

```
00505 {
00506     std::function<T(T)> func = [lhs](T item)
00507     { return lhs - item; };
00508     return np::element_wise_apply(rhs, func);
00509 }
```

4.1.2.10 operator/() [1/3]

```
template<class T , long unsigned int ND>
boost::multi_array< T, ND > operator/ (
            boost::multi_array< T, ND > const & lhs,
            boost::multi_array< T, ND > const & rhs )
```

Division between two multi arrays, element wise.

Definition at line 521 of file np.hpp.

```
00522 {
00523     std::function<T(T, T)> func = std::divides<T>();
00524     return np::element_wise_duo_apply(lhs, rhs, func);
00525 }
```

4.1.2.11 operator/() [2/3]

```
template<class T , long unsigned int ND>
boost::multi_array< T, ND > operator/ (
            boost::multi_array< T, ND > const & lhs,
            T const & rhs )  [inline]
```

Division between a multi array and a scalar, element wise.

Definition at line 538 of file np.hpp.

```
00539 {
00540     return rhs / lhs;
00541 }
```

4.1.2.12 operator/() [3/3]

```
template<class T , long unsigned int ND>
boost::multi_array< T, ND > operator/ (
            T const & lhs,
            boost::multi_array< T, ND > const & rhs )  [inline]
```

Division between a scalar and a multi array, element wise.

Definition at line 529 of file np.hpp.

```
00530 {
00531     std::function<T(T)> func = [lhs](T item)
00532     { return lhs / item; };
00533     return np::element_wise_apply(rhs, func);
00534 }
```

Chapter 5

Namespace Documentation

5.1 np Namespace Reference

Custom implementation of numpy in C++.

Typedefs

- typedef double ndArrayValue

Enumerations

- enum **indexing** { **xy** , **ij** }

Functions

- template<std::size_t ND>
  boost::multi_array< ndArrayValue, ND >::index getIndex (const boost::multi_array< ndArrayValue, ND > &m, const ndArrayValue *requestedElement, const unsigned short int direction)

  Gets the index of one element in a multi_array in one axis.
- template<std::size_t ND>
  boost::array< typename boost::multi_array< ndArrayValue, ND >::index, ND > getIndexArray (const boost::multi_array< ndArrayValue, ND > &m, const ndArrayValue *requestedElement)

  Gets the index of one element in a multi_array.
- template<typename Array , typename Element , typename Functor >
  void for_each (const boost::type< Element > &type_dispatch, Array A, Functor &xform)
- template<typename Element , typename Functor >
  void for_each (const boost::type< Element > &, Element &Val, Functor &xform)

  Function to apply a function to all elements of a multi_array.
- template<typename Element , typename Iterator , typename Functor >
  void for_each (const boost::type< Element > &type_dispatch, Iterator begin, Iterator end, Functor &xform)

  Function to apply a function to all elements of a multi_array.
- template<typename Array , typename Functor >
  void for_each (Array &A, Functor xform)

- template<long unsigned int ND>
  constexpr std::vector< boost::multi_array< double, ND > > gradient (boost::multi_array< double, ND > inArray, std::initializer_list< double > args)
- boost::multi_array< double, 1 > linspace (double start, double stop, long unsigned int num)

  Implements the numpy linspace function.
- template<long unsigned int ND>
  std::vector< boost::multi_array< double, ND > > meshgrid (const boost::multi_array< double, 1 >(&cinput)[ND], bool sparsing=false, indexing indexing_type=xy)
- template<class T , long unsigned int ND>
  boost::multi_array< T, ND > element_wise_apply (const boost::multi_array< T, ND > &input_array, std::function< T(T)> func)

  Cretes a new array and fills it with the values of the result of the function called on the input array element-wise.
- template<class T , long unsigned int ND>
  boost::multi_array< T, ND > sqrt (const boost::multi_array< T, ND > &input_array)
- template<class T >
  T sqrt (const T input)
- template<class T , long unsigned int ND>
  boost::multi_array< T, ND > exp (const boost::multi_array< T, ND > &input_array)
- template<class T >
  T exp (const T input)
- template<class T , long unsigned int ND>
  boost::multi_array< T, ND > log (const boost::multi_array< T, ND > &input_array)
- template<class T >
  T log (const T input)
- template<class T , long unsigned int ND>
  boost::multi_array< T, ND > pow (const boost::multi_array< T, ND > &input_array, const T exponent)
- template<class T >
  T pow (const T input, const T exponent)
- template<class T , long unsigned int ND>
  boost::multi_array< T, ND > element_wise_duo_apply (boost::multi_array< T, ND > const &lhs, boost::multi_array< T, ND > const &rhs, std::function< T(T, T)> func)

5.1.1 Detailed Description

Custom implementation of numpy in C++.

5.1.2 Typedef Documentation

5.1.2.1 ndArrayValue

```
typedef double np::ndArrayValue
```

Definition at line 22 of file np.hpp.

5.1.3 Enumeration Type Documentation

5.1.3.1 indexing

```
enum np::indexing
```

Definition at line 172 of file np.hpp.

```
00173     {
00174         xy,
00175         ij
00176     };
```

5.1.4 Function Documentation

5.1.4.1 element_wise_apply()

```
template<class T , long unsigned int ND>
boost::multi_array< T, ND > np::element_wise_apply (
            const boost::multi_array< T, ND > & input_array,
            std::function< T(T)> func )  [inline]
```

Cretes a new array and fills it with the values of the result of the function called on the input array element-wise.

Definition at line 243 of file np.hpp.

```
00244     {
00245 
00246         // Create output array copying extents
00247         using arrayIndex = boost::multi_array<double, ND>::index;
00248         using ndIndexArray = boost::array<arrayIndex, ND>;
00249         boost::detail::multi_array::extent_gen<ND> output_extents;
00250         std::vector<size_t> shape_list;
00251         for (std::size_t i = 0; i < ND; i++)
00252         {
00253             shape_list.push_back(input_array.shape()[i]);
00254         }
00255         std::copy(shape_list.begin(), shape_list.end(), output_extents.ranges_.begin());
00256         boost::multi_array<T, ND> output_array(output_extents);
00257 
00258         // Looping through the elements of the output array
00259         const T *p = input_array.data();
00260         ndIndexArray index;
00261         for (std::size_t i = 0; i < input_array.num_elements(); i++)
00262         {
00263             index = getIndexArray(input_array, p);
00264             output_array(index) = func(input_array(index));
00265             ++p;
00266         }
00267         return output_array;
00268     }
```

5.1.4.2 element_wise_duo_apply()

```
template<class T , long unsigned int ND>
boost::multi_array< T, ND > np::element_wise_duo_apply (
            boost::multi_array< T, ND > const & lhs,
            boost::multi_array< T, ND > const & rhs,
            std::function< T(T, T)> func )
```

Creates a new array in which the value at each index is the the result of the input function applied to an element of the left hand side array and one on the righ hand side array in the same index Outputs a copy of the result

Definition at line 324 of file np.hpp.

```
00325     {
00326         // Create output array copying extents
00327         using arrayIndex = boost::multi_array<double, ND>::index;
00328         using ndIndexArray = boost::array<arrayIndex, ND>;
00329         boost::detail::multi_array::extent_gen<ND> output_extents;
00330         std::vector<size_t> shape_list;
00331         for (std::size_t i = 0; i < ND; i++)
00332         {
00333             shape_list.push_back(lhs.shape()[i]);
00334         }
00335         std::copy(shape_list.begin(), shape_list.end(), output_extents.ranges_.begin());
00336         boost::multi_array<T, ND> output_array(output_extents);
00337 
00338         // Looping through the elements of the output array
00339         const T *p = lhs.data();
00340         ndIndexArray index;
00341         for (std::size_t i = 0; i < lhs.num_elements(); i++)
00342         {
00343             index = getIndexArray(lhs, p);
00344             output_array(index) = func(lhs(index), rhs(index));
00345             ++p;
00346         }
00347         return output_array;
00348     }
```

5.1.4.3 exp() [1/2]

```
template<class T , long unsigned int ND>
boost::multi_array< T, ND > np::exp (
             const boost::multi_array< T, ND > & input_array )  [inline]
```

Definition at line 285 of file np.hpp.

```
00286     {
00287         std::function<T(T)> func = (T(*)(T))std::exp;
00288         return element_wise_apply(input_array, func);
00289     }
```

5.1.4.4 exp() [2/2]

```
template<class T >
T np::exp (
             const T input )  [inline]
```

Definition at line 291 of file np.hpp.

```
00292     {
00293         return std::exp(input);
00294     }
```

5.1.4.5 for_each() [1/4]

```
template<typename Array , typename Functor >
void np::for_each (
             Array & A,
             Functor xform )  [inline]
```

Function to apply a function to all elements of a multi_array Simple overload

Definition at line 80 of file np.hpp.

```
00081     {
00082         // Dispatch to the proper function
00083         for_each(boost::type<typename Array::element>(), A.begin(), A.end(), xform);
00084     }
```

5.1.4.6 for_each() [2/4]

```
template<typename Element , typename Functor >
void np::for_each (
             const boost::type< Element > & ,
             Element & Val,
             Functor & xform )  [inline]
```

Function to apply a function to all elements of a multi_array.

Definition at line 59 of file np.hpp.

```
00060     {
00061         Val = xform(Val);
00062     }
```

5.1.4.7 for_each() [3/4]

```
template<typename Array , typename Element , typename Functor >
void np::for_each (
             const boost::type< Element > & type_dispatch,
             Array A,
             Functor & xform )  [inline]
```

Function to apply a function to all elements of a multi_array Simple overload

Definition at line 51 of file np.hpp.

```
00053     {
00054         for_each(type_dispatch, A.begin(), A.end(), xform);
00055     }
```

5.1.4.8 for_each() [4/4]

```
template<typename Element , typename Iterator , typename Functor >
void np::for_each (
             const boost::type< Element > & type_dispatch,
             Iterator begin,
             Iterator end,
             Functor & xform )  [inline]
```

Function to apply a function to all elements of a multi_array.

Definition at line 66 of file np.hpp.

```
00069     {
00070         while (begin != end)
00071         {
00072             for_each(type_dispatch, *begin, xform);
00073             ++begin;
00074         }
00075     }
```

5.1.4.9 getIndex()

```
template<std::size_t ND>
boost::multi_array< ndArrayValue, ND >::index np::getIndex (
            const boost::multi_array< ndArrayValue, ND > & m,
            const ndArrayValue * requestedElement,
            const unsigned short int direction )  [inline]
```

Gets the index of one element in a multi_array in one axis.

Definition at line 27 of file np.hpp.

```
00028     {
00029         int offset = requestedElement - m.origin();
00030         return (offset / m.strides()[direction] % m.shape()[direction] + m.index_bases()[direction]);
00031     }
```

5.1.4.10 getIndexArray()

```
template<std::size_t ND>
boost::array< typename boost::multi_array< ndArrayValue, ND >::index, ND > np::getIndexArray
(
            const boost::multi_array< ndArrayValue, ND > & m,
            const ndArrayValue * requestedElement )  [inline]
```

Gets the index of one element in a multi_array.

Definition at line 36 of file np.hpp.

```
00037     {
00038         using indexType = boost::multi_array<ndArrayValue, ND>::index;
00039         boost::array<indexType, ND> _index;
00040         for (unsigned int dir = 0; dir < ND; dir++)
00041         {
00042             _index[dir] = getIndex(m, requestedElement, dir);
00043         }
00044
00045         return _index;
00046     }
```

5.1.4.11 gradient()

```
template<long unsigned int ND>
constexpr std::vector< boost::multi_array< double, ND > > np::gradient (
            boost::multi_array< double, ND > inArray,
            std::initializer_list< double > args )  [inline], [constexpr]
```

Takes the gradient of a n-dimensional multi_array Todo: Actually implement the gradient calculation template <long unsigned int ND, typename... Args>

Definition at line 90 of file np.hpp.

```
00091     {
00092         // static_assert(args.size() == ND, "Number of arguments must match the number of dimensions
      of the array");
00093         using arrayIndex = boost::multi_array<double, ND>::index;
00094
00095         using ndIndexArray = boost::array<arrayIndex, ND>;
00096
00097         // constexpr std::size_t n = sizeof...(Args);
00098         std::size_t n = args.size();
00099         // std::tuple<Args...> store(args...);
```

```
00100         std::vector<double> arg_vector = args;
00101         boost::multi_array<double, ND> my_array;
00102         std::vector<boost::multi_array<double, ND» output_arrays;
00103         for (std::size_t i = 0; i < n; i++)
00104         {
00105             boost::multi_array<double, ND> dfdh = inArray;
00106             output_arrays.push_back(dfdh);
00107         }
00108 
00109         ndArrayValue *p = inArray.data();
00110         ndIndexArray index;
00111         for (std::size_t i = 0; i < inArray.num_elements(); i++)
00112         {
00113             index = getIndexArray(inArray, p);
00114             /*
00115             std::cout « "Index: ";
00116             for (std::size_t j = 0; j < n; j++)
00117             {
00118                 std::cout « index[j] « " ";
00119             }
00120             std::cout « "\n";
00121             */
00122             // Calculating the gradient now
00123             // j is the axis/dimension
00124             for (std::size_t j = 0; j < n; j++)
00125             {
00126                 ndIndexArray index_high = index;
00127                 double dh_high;
00128                 if ((long unsigned int)index_high[j] < inArray.shape()[j] - 1)
00129                 {
00130                     index_high[j] += 1;
00131                     dh_high = arg_vector[j];
00132                 }
00133                 else
00134                 {
00135                     dh_high = 0;
00136                 }
00137                 ndIndexArray index_low = index;
00138                 double dh_low;
00139                 if (index_low[j] > 0)
00140                 {
00141                     index_low[j] -= 1;
00142                     dh_low = arg_vector[j];
00143                 }
00144                 else
00145                 {
00146                     dh_low = 0;
00147                 }
00148 
00149                 double dh = dh_high + dh_low;
00150                 double gradient = (inArray(index_high) - inArray(index_low)) / dh;
00151                 // std::cout « gradient « "\n";
00152                 output_arrays[j](index) = gradient;
00153             }
00154             // std::cout « " value = " « inArray(index) « "  check = " « *p « std::endl;
00155             ++p;
00156         }
00157         return output_arrays;
00158     }
```

5.1.4.12 linspace()

```
boost::multi_array< double, 1 > np::linspace (
            double start,
            double stop,
            long unsigned int num )  [inline]
```

Implements the numpy linspace function.

Definition at line 161 of file np.hpp.

```
00162     {
00163         double step = (stop - start) / (num - 1);
00164         boost::multi_array<double, 1> output(boost::extents[num]);
00165         for (std::size_t i = 0; i < num; i++)
00166         {
00167             output[i] = start + i * step;
00168         }
00169         return output;
00170     }
```

5.1.4.13 log() [1/2]

```
template<class T , long unsigned int ND>
boost::multi_array< T, ND > np::log (
            const boost::multi_array< T, ND > & input_array )  [inline]
```

Definition at line 297 of file np.hpp.

```
00298     {
00299         std::function<T(T)> func = std::log<T>();
00300         return element_wise_apply(input_array, func);
00301     }
```

5.1.4.14 log() [2/2]

```
template<class T >
T np::log (
            const T input )  [inline]
```

Definition at line 303 of file np.hpp.

```
00304     {
00305         return std::log(input);
00306     }
```

5.1.4.15 meshgrid()

```
template<long unsigned int ND>
std::vector< boost::multi_array< double, ND > > np::meshgrid (
            const boost::multi_array< double, 1 >(&) cinput[ND],
            bool sparsing = false,
            indexing indexing_type = xy )  [inline]
```

Implementation of meshgrid TODO: Implement sparsing=true If the indexing type is xx, then reverse the order of the first two elements of ci if the number of dimensions is 2 or 3 In accordance with the numpy implementation

Definition at line 184 of file np.hpp.

```
00185     {
00186         using arrayIndex = boost::multi_array<double, ND>::index;
00187         using ndIndexArray = boost::array<arrayIndex, ND>;
00188         std::vector<boost::multi_array<double, ND» output_arrays;
00189         boost::multi_array<double, 1> ci[ND];
00190         // Copy elements of cinput to ci, do the proper inversions
00191         for (std::size_t i = 0; i < ND; i++)
00192         {
00193             std::size_t source = i;
00194             if (indexing_type == xy && (ND == 3 || ND == 2))
00195             {
00196                 switch (i)
00197                 {
00198                 case 0:
00199                     source = 1;
00200                     break;
00201                 case 1:
00202                     source = 0;
00203                     break;
00204                 default:
00205                     break;
00206                 }
00207             }
00208             ci[i] = boost::multi_array<double, 1>();
00209             ci[i].resize(boost::extents[cinput[source].num_elements()]);
00210             ci[i] = cinput[source];
00211         }
```

```
00212         // Deducing the extents of the N-Dimensional output
00213         boost::detail::multi_array::extent_gen<ND> output_extents;
00214         std::vector<size_t> shape_list;
00215         for (std::size_t i = 0; i < ND; i++)
00216         {
00217             shape_list.push_back(ci[i].shape()[0]);
00218         }
00219         std::copy(shape_list.begin(), shape_list.end(), output_extents.ranges_.begin());
00220 
00221         // Creating the output arrays
00222         for (std::size_t i = 0; i < ND; i++)
00223         {
00224             boost::multi_array<double, ND> output_array(output_extents);
00225             ndArrayValue *p = output_array.data();
00226             ndIndexArray index;
00227             // Looping through the elements of the output array
00228             for (std::size_t j = 0; j < output_array.num_elements(); j++)
00229             {
00230                 index = getIndexArray(output_array, p);
00231                 boost::multi_array<double, 1>::index index_1d;
00232                 index_1d = index[i];
00233                 output_array(index) = ci[i][index_1d];
00234                 ++p;
00235             }
00236             output_arrays.push_back(output_array);
00237         }
00238         return output_arrays;
00239     }
```

5.1.4.16 pow() [1/2]

```
template<class T , long unsigned int ND>
boost::multi_array< T, ND > np::pow (
             const boost::multi_array< T, ND > & input_array,
             const T exponent )  [inline]
```

Definition at line 308 of file np.hpp.

```
00309     {
00310         std::function<T(T)> pow_func = [exponent](T input)
00311         { return std::pow(input, exponent); };
00312         return element_wise_apply(input_array, pow_func);
00313     }
```

5.1.4.17 pow() [2/2]

```
template<class T >
T np::pow (
             const T input,
             const T exponent )  [inline]
```

Definition at line 315 of file np.hpp.

```
00316     {
00317         return std::pow(input, exponent);
00318     }
```

5.1.4.18 sqrt() [1/2]

```
template<class T , long unsigned int ND>
boost::multi_array< T, ND > np::sqrt (
            const boost::multi_array< T, ND > & input_array )  [inline]
```

Definition at line 273 of file np.hpp.

```
00274     {
00275         std::function<T(T)> func = (T(*)(T))std::sqrt;
00276         return element_wise_apply(input_array, func);
00277     }
```

5.1.4.19 sqrt() [2/2]

```
template<class T >
T np::sqrt (
            const T input )  [inline]
```

Definition at line 279 of file np.hpp.

```
00280     {
00281         return std::sqrt(input);
00282     }
```

Chapter 6

File Documentation

6.1 coeff.hpp

```
00001 //
00002 // Created by Yan Cheng on 11/28/22.
00003 //
00004
00005 #ifndef WAVESIMC_COEFF_HPP
00006 #define WAVESIMC_COEFF_HPP
00007
00008 #include "CustomLibraries/np.hpp"
00009 #include <math.h>
00010
00011
00012 boost::multi_array<double, 2> get_sigma_1(boost::multi_array<double, 1> x, double dx, int nx, int nz,
00013                                           double c_max, int n=10, double R=1e-3, int m=2)
00014 {
00015     boost::multi_array<double, 2> sigma_1 = np::zeros(nx, nz);
00016     const double PML_width = n * dx;
00017     const double sigma_max = - c_max * log(R) * (m+1) / (PML_width**(m+1));
00018
00019     // TODO: max: find the maximum element in 1D array
00020     const double x_0 = max(x) - PML_width;
00021
00022     // each column of sigma_1 is a 1D array named "polynomial"
00023     boost::multi_array<double, 1> polynomial = np::zeros(nx);
00024     for (int i=0; i<nx; i++)
00025     {
00026         if (x[i] > x_0)
00027         {
00028             // TODO: Does math.h have an absolute value function?
00029             polynomial[i] = sigma_max * abs(x[i] - x_0)**m;
00030             polynomial[nx-i] = polynomial[i];
00031         }
00032         else
00033         {
00034             polynomial[i] = 0;
00035         }
00036     }
00037
00038     // Copy 1D array into each column of 2D array
00039     for (int i=0; i<nx; i++)
00040         for (int j=0; i<nz; j++)
00041             sigma_1[i][j] = polynomial[i];
00042
00043     return sigma_1;
00044 }
00045
00046
00047
00048 boost::multi_array<double, 2> get_sigma_2(boost::multi_array<double, 1> z, double dz, int nx, int nz,
00049                                           double c_max, int n=10, double R=1e-3, int m=2)
00050 {
00051     boost::multi_array<double, 2> sigma_2 = np::zeros(nx, nz);
00052     const double PML_width = n * dz;
00053     const double sigma_max = - c_max * log(R) * (m+1) / (PML_width**(m+1));
00054
00055     // TODO: max: find the maximum element in 1D array
00056     const double z_0 = max(z) - PML_width;
00057
00058     // each column of sigma_1 is a 1D array named "polynomial"
```

```
00059     boost::multi_array<double, 1> polynomial = np::zeros(nz);
00060     for (int j=0; j<nz; j++)
00061     {
00062         if (z[j] > z_0)
00063         {
00064             // TODO: Does math.h have an absolute value function?
00065             polynomial[j] = sigma_max * abs(z[j] - z_0)**m;
00066             polynomial[nz-j] = polynomial[j];
00067         }
00068         else
00069         {
00070             polynomial[j] = 0;
00071         }
00072     }
00073
00074     // Copy 1D array into each column of 2D array
00075     for (int i=0; i<nx; i++)
00076         for (int j=0; i<nz; j++)
00077             sigma_1[i][j] = polynomial[j];
00078
00079     return sigma_2;
00080 }
00081
00082 #endif //WAVESIMC_COEFF_HPP
```

6.2 computational.hpp

```
00001 //
00002 // Created by Yan Cheng on 11/28/22.
00003 //
00004
00005 #ifndef WAVESIMC_COMPUTATIONAL_HPP
00006 #define WAVESIMC_COMPUTATIONAL_HPP
00007
00008 boost::multi_array<double, 2> get_profile()
00009 {
00010
00011 }
00012
00013 #endif //WAVESIMC_COMPUTATIONAL_HPP
```

6.3 helper_func.hpp

```
00001 //
00002 // Created by Yan Cheng on 11/28/22.
00003 //
00004
00005 #ifndef WAVESIMC_HELPER_FUNC_HPP
00006 #define WAVESIMC_HELPER_FUNC_HPP
00007
00008 #include "CustomLibraries/np.hpp"
00009
00010 boost::multi_array<double, 2> dfdx(boost::multi_array<double, 2> f, double dx)
00011 {
00012     std::vector<boost::multi_array<double, 2» grad_f = np::gradient(f, {dx, dx});
00013     return grad_f[0];
00014 }
00015
00016 boost::multi_array<double, 2> dfdz(boost::multi_array<double, 2> f, double dz)
00017 {
00018     std::vector<boost::multi_array<double, 2» grad_f = np::gradient(f, {dz, dz});
00019     return grad_f[1];
00020 }
00021
00022 boost::multi_array<double, 2> d2fdx2(boost::multi_array<double, 2> f, double dx)
00023 {
00024     boost::multi_array<double, 2> f_x = dfdx(f, dx);
00025     boost::multi_array<double, 2> f_xx = dfdx(f_x, dx);
00026     return f_xx;
00027 }
00028
00029 boost::multi_array<double, 2> d2fdz2(boost::multi_array<double, 2> f, double dz)
00030 {
00031     boost::multi_array<double, 2> f_z = dfdz(f, dz);
00032     boost::multi_array<double, 2> f_zz = dfdx(f_z, dz);
00033     return f_zz;
00034 }
00035
```

```
00036 boost::multi_array<double, 2> divergence(boost::multi_array<double, 2> f1, boost::multi_array<double,
       2> f2,
00037                                          double dx, double dz)
00038 {
00039     boost::multi_array<double, 2> f_x = dfdx(f1, dx);
00040     boost::multi_array<double, 2> f_z = dfdz(f2, dz);
00041     // TODO: use element-wize add
00042     div = f1 + f2;
00043     return div;
00044 }
00045
00046
00047 #endif //WAVESIMC_HELPER_FUNC_HPP
```

6.4 solver.hpp

```
00001 //
00002 // Created by Yan Cheng on 11/28/22.
00003 //
00004
00005 #ifndef WAVESIMC_SOLVER_HPP
00006 #define WAVESIMC_SOLVER_HPP
00007
00008 #include "CustomLibraries/np.hpp"
00009 #include "helper_func.hpp"
00010
00011 boost::multi_array<double, 3> wave_solver(boost::multi_array<double, 2> c,
00012                                           double dt, double dx, double dz, int nt, int nx, int nz,
00013                                           boost::multi_array<double, 3> f,
00014                                           boost::multi_array<double, 2> sigma_1,
       boost::multi_array<double, 2> sigma_2)
00015 {
00016     // TODO: "same shape" functionality of np::zeros
00017     boost::multi_array<double, 3> u = np::zeros(nt, nx, nz);
00018     boost::multi_array<double, 2> u_xx = np::zeros(nx, ny);
00019     boost::multi_array<double, 2> u_zz = np::zeros(nx, ny);
00020     boost::multi_array<double, 2> q_1 = np::zeros(nx, ny);
00021     boost::multi_array<double, 2> q_2 = np::zeros(nx, ny);
00022
00023     // TODO: make multiplication between scalar and boost::multi_array<double, 2> work
00024     // Basically we need to make * and ** work
00025     const boost::multi_array<double, 2> C1 = 1 + dt * (sigma_1 + sigma_2)/((double) 2);
00026     // Question: Is ((double) 2) necessary?
00027     const boost::multi_array<double, 2> C2 = sigma_1 * sigma_2 * (dt**2) - 2;
00028     const boost::multi_array<double, 2> C3 = 1 - dt*(sigma_1 + sigma_2)/2;
00029     const boost::multi_array<double, 2> C4 = (dt*c)**2;
00030     const boost::multi_array<double, 2> C5 = 1 + dt*sigma_1/2;
00031     const boost::multi_array<double, 2> C6 = 1 + dt*sigma_2/2;
00032     const boost::multi_array<double, 2> C7 = 1 - dt*sigma_1/2;
00033     const boost::multi_array<double, 2> C8 = 1 - dt*sigma_2/2;
00034
00035     for (int n = 0; n < nt; n++)
00036     {
00037         u_xx = d2fdx2(u[n], dx);
00038         u_zz = d2fdz2(u[n], dz);
00039
00040         u[n+1] = (C4*(u_xx/(dx**2) + u_zz/(dz**2) - divergence(q_1*sigma_1, q_2*sigma_2, dx, dz)
00041                       + sigma_2*dfdx(q_1, dx) + sigma_1*dfdz(q_2, dz) + f[n]) -
00042                   C2 * u[n] - C3 * u[n-1]) / C1;
00043
00044         q_1 = (dt*dfdx(u[n], dx) + C7*q_1) / C5;
00045         q_2 = (dt*dfdz(u[n], dx) + C8*q_2) / C6;
00046
00047         // Dirichlet boundary condition
00048         for (int i = 0; i < nx; i++)
00049         {
00050             u[n+1][i][0] = 0;
00051             u[n+1][i][nx-1] = 0;
00052         }
00053         for (int j = 0; j < nz; j++)
00054         {
00055             u[n+1][0][j] = 0;
00056             u[n+1][nz-1][j] = 0;
00057         }
00058     }
00059     return u;
00060 }
00061
00062 #endif //WAVESIMC_SOLVER_HPP
```

6.5 source.hpp

```
00001 //
00002 // Created by Yan Cheng on 11/28/22.
00003 //
00004
00005 #ifndef WAVESIMC_SOURCE_HPP
00006 #define WAVESIMC_SOURCE_HPP
00007
00008
00009 boost::multi_array<double, 3> ricker(int i_s, int j_s, double f=10, double amp=1e0, double shift=0.1)
00010 {
00011     const double pi = 3.141592654;
00012
00013     boost::multi_array<double, 1> t = np::linspace(tmin, tmax, nt);
00014
00015     // TODO: element-wise operators
00016     boost::multi_array<double, 1> pft2 = (pi * f * (t - shift))**2;
00017     boost::multi_array<double, 1> r = amp * (1 - 2 * pft2) * exp(-pft2);
00018
00019     boost::multi_array<double, 1> x = np.zeros(nx);
00020     boost::multi_array<double, 1> z = np.zeros(nz);
00021     x[i_s] = 1.0;
00022     z[j_s] = 1.0;
00023     boost::multi_array<double, 3> TXZ = np::meshgrid(r, x, z, sparse=True, indexing='ij');
00024
00025     return TXZ;
00026 }
00027
00028 #endif //WAVESIMC_SOURCE_HPP
```

6.6 wave.cpp

```
00001 // For the core algorithm, we need six functionalities:
00002 // 1) create the computational domain,
00003 // 2) create a velocity profile (1 & 2 can be put together)
00004 // 3) create attenuation coefficients,
00005 // 4) create source functions,
00006 // 5) helper functions to compute eg. df/dx
00007 // 6) use all above to create a solver function for wave equation
00008
00009 // Standard IO libraries
00010 #include <iostream>
00011 #include <fstream>
00012 #include "CustomLibraries/np.hpp"
00013
00014 #include <math.h>
00015
00016 #include "solver.hpp"
00017 #include "computational.hpp"
00018 #include "coeff.hpp"
00019 #include "source.hpp"
00020 #include "helper_func.hpp"
00021
00022
00023 int main()
00024 {
00025     double dx, dy, dz, dt;
00026     dx = 1.0;
00027     dy = 1.0;
00028     dz = 1.0;
00029     dt = 1.0;
00030     std::vector<boost::multi_array<double, 4» my_arrays = np::gradient(A, {dx, dy, dz, dt});
00031     return 0;
00032 }
```

6.7 np.hpp

```
00001 #ifndef NP_H_
00002 #define NP_H_
00003
00004 #include "boost/multi_array.hpp"
00005 #include "boost/array.hpp"
00006 #include "boost/cstdlib.hpp"
00007 #include <type_traits>
00008 #include <cassert>
00009 #include <iostream>
00010 #include <functional>
00011 #include <type_traits>
```

```
00012
00019 namespace np
00020 {
00021
00022     typedef double ndArrayValue;
00023
00025     template <std::size_t ND>
00026     inline boost::multi_array<ndArrayValue, ND>::index
00027     getIndex(const boost::multi_array<ndArrayValue, ND> &m, const ndArrayValue *requestedElement,
      const unsigned short int direction)
00028     {
00029         int offset = requestedElement - m.origin();
00030         return (offset / m.strides()[direction] % m.shape()[direction] + m.index_bases()[direction]);
00031     }
00032
00034     template <std::size_t ND>
00035     inline boost::array<typename boost::multi_array<ndArrayValue, ND>::index, ND>
00036     getIndexArray(const boost::multi_array<ndArrayValue, ND> &m, const ndArrayValue *requestedElement)
00037     {
00038         using indexType = boost::multi_array<ndArrayValue, ND>::index;
00039         boost::array<indexType, ND> _index;
00040         for (unsigned int dir = 0; dir < ND; dir++)
00041         {
00042             _index[dir] = getIndex(m, requestedElement, dir);
00043         }
00044
00045         return _index;
00046     }
00047
00050     template <typename Array, typename Element, typename Functor>
00051     inline void for_each(const boost::type<Element> &type_dispatch,
00052                          Array A, Functor &xform)
00053     {
00054         for_each(type_dispatch, A.begin(), A.end(), xform);
00055     }
00056
00058     template <typename Element, typename Functor>
00059     inline void for_each(const boost::type<Element> &, Element &Val, Functor &xform)
00060     {
00061         Val = xform(Val);
00062     }
00063
00065     template <typename Element, typename Iterator, typename Functor>
00066     inline void for_each(const boost::type<Element> &type_dispatch,
00067                          Iterator begin, Iterator end,
00068                          Functor &xform)
00069     {
00070         while (begin != end)
00071         {
00072             for_each(type_dispatch, *begin, xform);
00073             ++begin;
00074         }
00075     }
00076
00079     template <typename Array, typename Functor>
00080     inline void for_each(Array &A, Functor xform)
00081     {
00082         // Dispatch to the proper function
00083         for_each(boost::type<typename Array::element>(), A.begin(), A.end(), xform);
00084     }
00085
00089     template <long unsigned int ND>
00090     inline constexpr std::vector<boost::multi_array<double, ND>> gradient(boost::multi_array<double,
      ND> inArray, std::initializer_list<double> args)
00091     {
00092         // static_assert(args.size() == ND, "Number of arguments must match the number of dimensions
      of the array");
00093         using arrayIndex = boost::multi_array<double, ND>::index;
00094
00095         using ndIndexArray = boost::array<arrayIndex, ND>;
00096
00097         // constexpr std::size_t n = sizeof...(Args);
00098         std::size_t n = args.size();
00099         // std::tuple<Args...> store(args...);
00100         std::vector<double> arg_vector = args;
00101         boost::multi_array<double, ND> my_array;
00102         std::vector<boost::multi_array<double, ND>> output_arrays;
00103         for (std::size_t i = 0; i < n; i++)
00104         {
00105             boost::multi_array<double, ND> dfdh = inArray;
00106             output_arrays.push_back(dfdh);
00107         }
00108
00109         ndArrayValue *p = inArray.data();
00110         ndIndexArray index;
00111         for (std::size_t i = 0; i < inArray.num_elements(); i++)
00112         {
```

```
00113             index = getIndexArray(inArray, p);
00114             /*
00115             std::cout « "Index: ";
00116             for (std::size_t j = 0; j < n; j++)
00117             {
00118                 std::cout « index[j] « " ";
00119             }
00120             std::cout « "\n";
00121             */
00122             // Calculating the gradient now
00123             // j is the axis/dimension
00124             for (std::size_t j = 0; j < n; j++)
00125             {
00126                 ndIndexArray index_high = index;
00127                 double dh_high;
00128                 if ((long unsigned int)index_high[j] < inArray.shape()[j] - 1)
00129                 {
00130                     index_high[j] += 1;
00131                     dh_high = arg_vector[j];
00132                 }
00133                 else
00134                 {
00135                     dh_high = 0;
00136                 }
00137                 ndIndexArray index_low = index;
00138                 double dh_low;
00139                 if (index_low[j] > 0)
00140                 {
00141                     index_low[j] -= 1;
00142                     dh_low = arg_vector[j];
00143                 }
00144                 else
00145                 {
00146                     dh_low = 0;
00147                 }
00148 
00149                 double dh = dh_high + dh_low;
00150                 double gradient = (inArray(index_high) - inArray(index_low)) / dh;
00151                 // std::cout « gradient « "\n";
00152                 output_arrays[j](index) = gradient;
00153             }
00154             // std::cout « " value = " « inArray(index) « "  check = " « *p « std::endl;
00155             ++p;
00156         }
00157         return output_arrays;
00158     }
00159 
00161     inline boost::multi_array<double, 1> linspace(double start, double stop, long unsigned int num)
00162     {
00163         double step = (stop - start) / (num - 1);
00164         boost::multi_array<double, 1> output(boost::extents[num]);
00165         for (std::size_t i = 0; i < num; i++)
00166         {
00167             output[i] = start + i * step;
00168         }
00169         return output;
00170     }
00171 
00172     enum indexing
00173     {
00174         xy,
00175         ij
00176     };
00177 
00183     template <long unsigned int ND>
00184     inline std::vector<boost::multi_array<double, ND» meshgrid(const boost::multi_array<double, 1>
       (&cinput)[ND], bool sparsing = false, indexing indexing_type = xy)
00185     {
00186         using arrayIndex = boost::multi_array<double, ND>::index;
00187         using ndIndexArray = boost::array<arrayIndex, ND>;
00188         std::vector<boost::multi_array<double, ND» output_arrays;
00189         boost::multi_array<double, 1> ci[ND];
00190         // Copy elements of cinput to ci, do the proper inversions
00191         for (std::size_t i = 0; i < ND; i++)
00192         {
00193             std::size_t source = i;
00194             if (indexing_type == xy && (ND == 3 || ND == 2))
00195             {
00196                 switch (i)
00197                 {
00198                 case 0:
00199                     source = 1;
00200                     break;
00201                 case 1:
00202                     source = 0;
00203                     break;
00204                 default:
```

```
00205                     break;
00206                 }
00207             }
00208             ci[i] = boost::multi_array<double, 1>();
00209             ci[i].resize(boost::extents[cinput[source].num_elements()]);
00210             ci[i] = cinput[source];
00211         }
00212         // Deducing the extents of the N-Dimensional output
00213         boost::detail::multi_array::extent_gen<ND> output_extents;
00214         std::vector<size_t> shape_list;
00215         for (std::size_t i = 0; i < ND; i++)
00216         {
00217             shape_list.push_back(ci[i].shape()[0]);
00218         }
00219         std::copy(shape_list.begin(), shape_list.end(), output_extents.ranges_.begin());
00220 
00221         // Creating the output arrays
00222         for (std::size_t i = 0; i < ND; i++)
00223         {
00224             boost::multi_array<double, ND> output_array(output_extents);
00225             ndArrayValue *p = output_array.data();
00226             ndIndexArray index;
00227             // Looping through the elements of the output array
00228             for (std::size_t j = 0; j < output_array.num_elements(); j++)
00229             {
00230                 index = getIndexArray(output_array, p);
00231                 boost::multi_array<double, 1>::index index_1d;
00232                 index_1d = index[i];
00233                 output_array(index) = ci[i][index_1d];
00234                 ++p;
00235             }
00236             output_arrays.push_back(output_array);
00237         }
00238         return output_arrays;
00239     }
00240 
00242     template <class T, long unsigned int ND>
00243     inline boost::multi_array<T, ND> element_wise_apply(const boost::multi_array<T, ND> &input_array,
    std::function<T(T)> func)
00244     {
00245 
00246         // Create output array copying extents
00247         using arrayIndex = boost::multi_array<double, ND>::index;
00248         using ndIndexArray = boost::array<arrayIndex, ND>;
00249         boost::detail::multi_array::extent_gen<ND> output_extents;
00250         std::vector<size_t> shape_list;
00251         for (std::size_t i = 0; i < ND; i++)
00252         {
00253             shape_list.push_back(input_array.shape()[i]);
00254         }
00255         std::copy(shape_list.begin(), shape_list.end(), output_extents.ranges_.begin());
00256         boost::multi_array<T, ND> output_array(output_extents);
00257 
00258         // Looping through the elements of the output array
00259         const T *p = input_array.data();
00260         ndIndexArray index;
00261         for (std::size_t i = 0; i < input_array.num_elements(); i++)
00262         {
00263             index = getIndexArray(input_array, p);
00264             output_array(index) = func(input_array(index));
00265             ++p;
00266         }
00267         return output_array;
00268     }
00269 
00270     // Complex operations
00271 
00272     template <class T, long unsigned int ND>
00273     inline boost::multi_array<T, ND> sqrt(const boost::multi_array<T, ND> &input_array)
00274     {
00275         std::function<T(T)> func = (T(*)(T))std::sqrt;
00276         return element_wise_apply(input_array, func);
00277     }
00278     template <class T>
00279     inline T sqrt(const T input)
00280     {
00281         return std::sqrt(input);
00282     }
00283 
00284     template <class T, long unsigned int ND>
00285     inline boost::multi_array<T, ND> exp(const boost::multi_array<T, ND> &input_array)
00286     {
00287         std::function<T(T)> func = (T(*)(T))std::exp;
00288         return element_wise_apply(input_array, func);
00289     }
00290     template <class T>
00291     inline T exp(const T input)
```

```
00292     {
00293         return std::exp(input);
00294     }
00295 
00296     template <class T, long unsigned int ND>
00297     inline boost::multi_array<T, ND> log(const boost::multi_array<T, ND> &input_array)
00298     {
00299         std::function<T(T)> func = std::log<T>();
00300         return element_wise_apply(input_array, func);
00301     }
00302     template <class T>
00303     inline T log(const T input)
00304     {
00305         return std::log(input);
00306     }
00307     template <class T, long unsigned int ND>
00308     inline boost::multi_array<T, ND> pow(const boost::multi_array<T, ND> &input_array, const T
    exponent)
00309     {
00310         std::function<T(T)> pow_func = [exponent](T input)
00311         { return std::pow(input, exponent); };
00312         return element_wise_apply(input_array, pow_func);
00313     }
00314     template <class T>
00315     inline T pow(const T input, const T exponent)
00316     {
00317         return std::pow(input, exponent);
00318     }
00319 
00323     template <class T, long unsigned int ND>
00324     boost::multi_array<T, ND> element_wise_duo_apply(boost::multi_array<T, ND> const &lhs,
    boost::multi_array<T, ND> const &rhs, std::function<T(T, T)> func)
00325     {
00326         // Create output array copying extents
00327         using arrayIndex = boost::multi_array<double, ND>::index;
00328         using ndIndexArray = boost::array<arrayIndex, ND>;
00329         boost::detail::multi_array::extent_gen<ND> output_extents;
00330         std::vector<size_t> shape_list;
00331         for (std::size_t i = 0; i < ND; i++)
00332         {
00333             shape_list.push_back(lhs.shape()[i]);
00334         }
00335         std::copy(shape_list.begin(), shape_list.end(), output_extents.ranges_.begin());
00336         boost::multi_array<T, ND> output_array(output_extents);
00337 
00338         // Looping through the elements of the output array
00339         const T *p = lhs.data();
00340         ndIndexArray index;
00341         for (std::size_t i = 0; i < lhs.num_elements(); i++)
00342         {
00343             index = getIndexArray(lhs, p);
00344             output_array(index) = func(lhs(index), rhs(index));
00345             ++p;
00346         }
00347         return output_array;
00348     }
00349 
00351     template <typename T, typename inT, long unsigned int ND>
00352     inline constexpr boost::multi_array<T, ND> zeros(inT (&dimensions_input)[ND]) requires
    std::is_integral<inT>::value && std::is_arithmetic<T>::value
00353     {
00354         // Deducing the extents of the N-Dimensional output
00355         boost::detail::multi_array::extent_gen<ND> output_extents;
00356         std::vector<size_t> shape_list;
00357         for (std::size_t i = 0; i < ND; i++)
00358         {
00359             shape_list.push_back(dimensions_input[i]);
00360         }
00361         std::copy(shape_list.begin(), shape_list.end(), output_extents.ranges_.begin());
00362         // Applying a function to return zero always to all of its elements
00363         boost::multi_array<T, ND> output_array(output_extents);
00364         std::function<T(T)> zero_func = [](T input)
00365         { return 0; };
00366         return element_wise_apply(output_array, zero_func);
00367     }
00368 
00370     template <typename T, long unsigned int ND>
00371     inline constexpr T max(boost::multi_array<T, ND> const &input_array) requires
    std::is_arithmetic<T>::value
00372     {
00373         T max = 0;
00374         bool max_not_set = true;
00375         const T *data_pointer = input_array.data();
00376         for (std::size_t i = 0; i < input_array.num_elements(); i++)
00377         {
00378             T element = *data_pointer;
00379             if (max_not_set || element > max)
```

```
00380             {
00381                 max = element;
00382                 max_not_set = false;
00383             }
00384             ++data_pointer;
00385         }
00386         return max;
00387     }
00388 
00390     template <class T, class... Ts, class = std::enable_if_t<(std::is_same_v<T, Ts> && ...)>
00391     inline constexpr T max(T input1, Ts... inputs) requires std::is_arithmetic<T>::value
00392     {
00393         T max = input1;
00394         for (T input : {inputs...})
00395         {
00396             if (input > max)
00397             {
00398                 max = input;
00399             }
00400         }
00401         return max;
00402     }
00403 
00405     template <typename T, long unsigned int ND>
00406     inline constexpr T min(boost::multi_array<T, ND> const &input_array) requires
      std::is_arithmetic<T>::value
00407     {
00408         T min = 0;
00409         bool min_not_set = true;
00410         const T *data_pointer = input_array.data();
00411         for (std::size_t i = 0; i < input_array.num_elements(); i++)
00412         {
00413             T element = *data_pointer;
00414             if (min_not_set || element < min)
00415             {
00416                 min = element;
00417                 min_not_set = false;
00418             }
00419             ++data_pointer;
00420         }
00421         return min;
00422     }
00423 
00425     template <class T, class... Ts, class = std::enable_if_t<(std::is_same_v<T, Ts> && ...)>
00426     inline constexpr T min(T input1, Ts... inputs) requires std::is_arithmetic<T>::value
00427     {
00428         T min = input1;
00429         for (T input : {inputs...})
00430         {
00431             if (input < min)
00432             {
00433                 min = input;
00434             }
00435         }
00436         return min;
00437     }
00438 }
00439 
00440 // Override of operators in the boost::multi_array class to make them more np-like
00441 // Basic operators
00442 // All of the are element-wise
00443 
00444 // Multiplication operator
00446 template <class T, long unsigned int ND>
00447 inline boost::multi_array<T, ND> operator*(boost::multi_array<T, ND> const &lhs, boost::multi_array<T,
       ND> const &rhs)
00448 {
00449     std::function<T(T, T)> func = std::multiplies<T>();
00450     return np::element_wise_duo_apply(lhs, rhs, func);
00451 }
00452 
00454 template <class T, long unsigned int ND>
00455 inline boost::multi_array<T, ND> operator*(T const &lhs, boost::multi_array<T, ND> const &rhs)
00456 {
00457     std::function<T(T)> func = [lhs](T item)
00458     { return lhs * item; };
00459     return np::element_wise_apply(rhs, func);
00460 }
00462 template <class T, long unsigned int ND>
00463 inline boost::multi_array<T, ND> operator*(boost::multi_array<T, ND> const &lhs, T const &rhs)
00464 {
00465     return rhs * lhs;
00466 }
00467 
00468 // Plus operator
00470 template <class T, long unsigned int ND>
00471 boost::multi_array<T, ND> operator+(boost::multi_array<T, ND> const &lhs, boost::multi_array<T, ND>
```

```
    const &rhs)
00472 {
00473     std::function<T(T, T)> func = std::plus<T>();
00474     return np::element_wise_duo_apply(lhs, rhs, func);
00475 }
00476
00478 template <class T, long unsigned int ND>
00479 inline boost::multi_array<T, ND> operator+(T const &lhs, boost::multi_array<T, ND> const &rhs)
00480 {
00481     std::function<T(T)> func = [lhs](T item)
00482     { return lhs + item; };
00483     return np::element_wise_apply(rhs, func);
00484 }
00485
00487 template <class T, long unsigned int ND>
00488 inline boost::multi_array<T, ND> operator+(boost::multi_array<T, ND> const &lhs, T const &rhs)
00489 {
00490     return rhs + lhs;
00491 }
00492
00493 // Subtraction operator
00495 template <class T, long unsigned int ND>
00496 boost::multi_array<T, ND> operator-(boost::multi_array<T, ND> const &lhs, boost::multi_array<T, ND>
    const &rhs)
00497 {
00498     std::function<T(T, T)> func = std::minus<T>();
00499     return np::element_wise_duo_apply(lhs, rhs, func);
00500 }
00501
00503 template <class T, long unsigned int ND>
00504 inline boost::multi_array<T, ND> operator-(T const &lhs, boost::multi_array<T, ND> const &rhs)
00505 {
00506     std::function<T(T)> func = [lhs](T item)
00507     { return lhs - item; };
00508     return np::element_wise_apply(rhs, func);
00509 }
00510
00512 template <class T, long unsigned int ND>
00513 inline boost::multi_array<T, ND> operator-(boost::multi_array<T, ND> const &lhs, T const &rhs)
00514 {
00515     return rhs - lhs;
00516 }
00517
00518 // Division operator
00520 template <class T, long unsigned int ND>
00521 boost::multi_array<T, ND> operator/(boost::multi_array<T, ND> const &lhs, boost::multi_array<T, ND>
    const &rhs)
00522 {
00523     std::function<T(T, T)> func = std::divides<T>();
00524     return np::element_wise_duo_apply(lhs, rhs, func);
00525 }
00526
00528 template <class T, long unsigned int ND>
00529 inline boost::multi_array<T, ND> operator/(T const &lhs, boost::multi_array<T, ND> const &rhs)
00530 {
00531     std::function<T(T)> func = [lhs](T item)
00532     { return lhs / item; };
00533     return np::element_wise_apply(rhs, func);
00534 }
00535
00537 template <class T, long unsigned int ND>
00538 inline boost::multi_array<T, ND> operator/(boost::multi_array<T, ND> const &lhs, T const &rhs)
00539 {
00540     return rhs / lhs;
00541 }
00542
00544 #endif
```

6.8 main.cpp

```
00001 #include <iostream>
00002 #include <string>
00003 #include "ExternalLibraries/cxxopts.hpp"
00004 #include "CustomLibraries/np.hpp"
00005
00006 // Command line arguments
00007 cxxopts::Options options("WaveSimC", "A wave propagation simulator written in C++ for seismic data
    processing.");
00008 int main(int argc, char *argv[])
00009 {
00010     // Parse command line arguments
00011     options.add_options()("d,debug", "Enable debugging")("i,input_file", "Input file path",
    cxxopts::value<std::string>())("o,output_file", "Output file path",
```

```
      cxxopts::value<std::string>())("v,verbose", "Verbose output",
      cxxopts::value<bool>()->default_value("false"));
00012     auto result = options.parse(argc, argv);
00013
00014     std::cout « "Hello World"
00015               « "\n";
00016 }
```

6.9 variadic.cpp

```
00001 #include "boost/multi_array.hpp"
00002 #include "boost/array.hpp"
00003 #include "CustomLibraries/np.hpp"
00004 #include <cassert>
00005 #include <iostream>
00006
00007 void test_gradient()
00008 {
00009     // Create a 4D array that is 3 x 4 x 2 x 1
00010     typedef boost::multi_array<double, 4>::index index;
00011     boost::multi_array<double, 4> A(boost::extents[3][4][2][2]);
00012
00013     // Assign values to the elements
00014     int values = 0;
00015     for (index i = 0; i != 3; ++i)
00016         for (index j = 0; j != 4; ++j)
00017             for (index k = 0; k != 2; ++k)
00018                 for (index l = 0; l != 2; ++l)
00019                     A[i][j][k][l] = values++;
00020
00021     // Verify values
00022     int verify = 0;
00023     for (index i = 0; i != 3; ++i)
00024         for (index j = 0; j != 4; ++j)
00025             for (index k = 0; k != 2; ++k)
00026                 for (index l = 0; l != 2; ++l)
00027                     assert(A[i][j][k][l] == verify++);
00028
00029     double dx, dy, dz, dt;
00030     dx = 1.0;
00031     dy = 1.0;
00032     dz = 1.0;
00033     dt = 1.0;
00034     std::vector<boost::multi_array<double, 4» my_arrays = np::gradient(A, {dx, dy, dz, dt});
00035
00036     boost::multi_array<double, 1> x = np::linspace(0, 1, 5);
00037     std::vector<boost::multi_array<double, 1» gradf = np::gradient(x, {1.0});
00038     for (int i = 0; i < 5; i++)
00039     {
00040         std::cout « gradf[0][i] « ",";
00041     }
00042     std::cout « "\n";
00043     // np::print(std::cout, my_arrays[0]);
00044 }
00045
00046 void test_meshgrid()
00047 {
00048     boost::multi_array<double, 1> x = np::linspace(0, 1, 5);
00049     boost::multi_array<double, 1> y = np::linspace(0, 1, 5);
00050     boost::multi_array<double, 1> z = np::linspace(0, 1, 5);
00051     boost::multi_array<double, 1> t = np::linspace(0, 1, 5);
00052     const boost::multi_array<double, 1> axis[4] = {x, y, z, t};
00053     std::vector<boost::multi_array<double, 4» my_arrays = np::meshgrid(axis, false, np::xy);
00054     // np::print(std::cout, my_arrays[0]);
00055     int nx = 3;
00056     int ny = 2;
00057     boost::multi_array<double, 1> x2 = np::linspace(0, 1, nx);
00058     boost::multi_array<double, 1> y2 = np::linspace(0, 1, ny);
00059     const boost::multi_array<double, 1> axis2[2] = {x2, y2};
00060     std::vector<boost::multi_array<double, 2» my_arrays2 = np::meshgrid(axis2, false, np::xy);
00061     std::cout « "xv\n";
00062     for (int i = 0; i < ny; i++)
00063     {
00064         for (int j = 0; j < nx; j++)
00065         {
00066             std::cout « my_arrays2[0][i][j] « " ";
00067         }
00068         std::cout « "\n";
00069     }
00070     std::cout « "yv\n";
00071     for (int i = 0; i < ny; i++)
00072     {
00073         for (int j = 0; j < nx; j++)
```

```
00074         {
00075             std::cout « my_arrays2[1][i][j] « " ";
00076         }
00077         std::cout « "\n";
00078     }
00079 }
00080
00081 void test_complex_operations()
00082 {
00083     int nx = 3;
00084     int ny = 2;
00085     boost::multi_array<double, 1> x = np::linspace(0, 1, nx);
00086     boost::multi_array<double, 1> y = np::linspace(0, 1, ny);
00087     const boost::multi_array<double, 1> axis[2] = {x, y};
00088     std::vector<boost::multi_array<double, 2» my_arrays = np::meshgrid(axis, false, np::xy);
00089     boost::multi_array<double, 2> A = np::sqrt(my_arrays[0]);
00090     std::cout « "sqrt\n";
00091     for (int i = 0; i < ny; i++)
00092     {
00093         for (int j = 0; j < nx; j++)
00094         {
00095             std::cout « A[i][j] « " ";
00096         }
00097         std::cout « "\n";
00098     }
00099     std::cout « "\n";
00100     float a = 100.0;
00101     float sqa = np::sqrt(a);
00102     std::cout « "sqrt of " « a « " is " « sqa « "\n";
00103     std::cout « "exp\n";
00104     boost::multi_array<double, 2> B = np::exp(my_arrays[0]);
00105     for (int i = 0; i < ny; i++)
00106     {
00107         for (int j = 0; j < nx; j++)
00108         {
00109             std::cout « B[i][j] « " ";
00110         }
00111         std::cout « "\n";
00112     }
00113
00114     std::cout « "Power\n";
00115     boost::multi_array<double, 1> x2 = np::linspace(1, 3, nx);
00116     boost::multi_array<double, 1> y2 = np::linspace(1, 3, ny);
00117     const boost::multi_array<double, 1> axis2[2] = {x2, y2};
00118     std::vector<boost::multi_array<double, 2» my_arrays2 = np::meshgrid(axis2, false, np::xy);
00119     boost::multi_array<double, 2> C = np::pow(my_arrays2[1], 2.0);
00120     for (int i = 0; i < ny; i++)
00121     {
00122         for (int j = 0; j < nx; j++)
00123         {
00124             std::cout « C[i][j] « " ";
00125         }
00126         std::cout « "\n";
00127     }
00128 }
00129
00130 void test_equal()
00131 {
00132     boost::multi_array<double, 1> x = np::linspace(0, 1, 5);
00133     boost::multi_array<double, 1> y = np::linspace(0, 1, 5);
00134     boost::multi_array<double, 1> z = np::linspace(0, 1, 5);
00135     boost::multi_array<double, 1> t = np::linspace(0, 1, 5);
00136     const boost::multi_array<double, 1> axis[4] = {x, y, z, t};
00137     std::vector<boost::multi_array<double, 4» my_arrays = np::meshgrid(axis, false, np::xy);
00138     boost::multi_array<double, 1> x2 = np::linspace(0, 1, 5);
00139     boost::multi_array<double, 1> y2 = np::linspace(0, 1, 5);
00140     boost::multi_array<double, 1> z2 = np::linspace(0, 1, 5);
00141     boost::multi_array<double, 1> t2 = np::linspace(0, 1, 5);
00142     const boost::multi_array<double, 1> axis2[4] = {x2, y2, z2, t2};
00143     std::vector<boost::multi_array<double, 4» my_arrays2 = np::meshgrid(axis2, false, np::xy);
00144     std::cout « "equality test:\n";
00145     std::cout « (bool)(my_arrays == my_arrays2) « "\n";
00146 }
00147 void test_basic_operations()
00148 {
00149     int nx = 3;
00150     int ny = 2;
00151     boost::multi_array<double, 1> x = np::linspace(0, 1, nx);
00152     boost::multi_array<double, 1> y = np::linspace(0, 1, ny);
00153     const boost::multi_array<double, 1> axis[2] = {x, y};
00154     std::vector<boost::multi_array<double, 2» my_arrays = np::meshgrid(axis, false, np::xy);
00155
00156     std::cout « "basic operations:\n";
00157
00158     std::cout « "addition:\n";
00159     boost::multi_array<double, 2> A = my_arrays[0] + my_arrays[1];
00160
```

```
00161     for (int i = 0; i < ny; i++)
00162     {
00163         for (int j = 0; j < nx; j++)
00164         {
00165             std::cout « A[i][j] « " ";
00166         }
00167         std::cout « "\n";
00168     }
00169 
00170     std::cout « "multiplication:\n";
00171     boost::multi_array<double, 2> B = my_arrays[0] * my_arrays[1];
00172 
00173     for (int i = 0; i < ny; i++)
00174     {
00175         for (int j = 0; j < nx; j++)
00176         {
00177             std::cout « B[i][j] « " ";
00178         }
00179         std::cout « "\n";
00180     }
00181     double coeff = 3;
00182     boost::multi_array<double, 1> t = np::linspace(0, 1, nx);
00183     boost::multi_array<double, 1> t_time_3 = coeff * t;
00184     boost::multi_array<double, 1> t_time_2 = 2.0 * t;
00185     std::cout « "t_time_3: ";
00186     for (int j = 0; j < nx; j++)
00187     {
00188         std::cout « t_time_3[j] « " ";
00189     }
00190     std::cout « "\n";
00191     std::cout « "t_time_2: ";
00192     for (int j = 0; j < nx; j++)
00193     {
00194         std::cout « t_time_2[j] « " ";
00195     }
00196     std::cout « "\n";
00197 }
00198 
00199 void test_zeros()
00200 {
00201     int nx = 3;
00202     int ny = 2;
00203     int dimensions[] = {ny, nx};
00204     boost::multi_array<double, 2> A = np::zeros<double>(dimensions);
00205     std::cout « "zeros:\n";
00206     for (int i = 0; i < ny; i++)
00207     {
00208         for (int j = 0; j < nx; j++)
00209         {
00210             std::cout « A[i][j] « " ";
00211         }
00212         std::cout « "\n";
00213     }
00214 }
00215 
00216 void test_min_max()
00217 {
00218     int nx = 24;
00219     int ny = 5;
00220     boost::multi_array<double, 1> x = np::linspace(0, 10, nx);
00221     boost::multi_array<double, 1> y = np::linspace(-1, 1, ny);
00222     const boost::multi_array<double, 1> axis[2] = {x, y};
00223     std::vector<boost::multi_array<double, 2» my_array = np::meshgrid(axis, false, np::xy);
00224     std::cout « "min: " « np::min(my_array[0]) « "\n";
00225     std::cout « "max: " « np::max(my_array[1]) « "\n";
00226     std::cout « "max simple: " « np::max(1.0, 2.0, 3.0, 4.0, 5.0) « "\n";
00227     std::cout « "min simple: " « np::min(1, -2, 3, -4, 5) « "\n";
00228 }
00229 
00230 int main()
00231 {
00232     test_gradient();
00233     test_meshgrid();
00234     test_complex_operations();
00235     test_equal();
00236     test_basic_operations();
00237     test_zeros();
00238     test_min_max();
00239 }
```