MT4113, Computing in Statistics

Lecture 2 - Algorithms to functions

19 September 2018

- Algorithms
- 2 Some elements of algorithms
- 3 Code and Pseudocode
- Control structures in R
- **5** Modular programming

Algorithms

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 - ▶ halts in finite time i.e., the algorithm needs to terminate

Example algorithm

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 Put water in pan.
 When the water boils, turn over the egg timer.
 When the timer has run out, turn off the heat.
 Pour some cold water into the pan to cool the water.
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 - What is wrong with this algorithm?

Some elements of algorithms

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 - x := x * 2

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 - Printing results on screen
 - Saving results to file

Control structures: conditional execution

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- Example:

```
* Algorithm cakemix (sweet tooth) *
In a bowl mix together:
  8 oz butter
  4 medium eggs
  2tsp vanilla extract
  8 oz self raising flour
  if (sweet tooth) then
    8 oz caster sugar
  else
    4 oz caster sugar
  end if
  . . .
```

Control structures: iteration

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- Number of iterations known at outset example:

```
* Algorithm scramble (n) *

Do these statements n times:
   take an egg out of the fridge;
   crack the egg's shell on the edge of the bowl;
   pull the egg apart above the bowl;
   let the contents of the egg fall into the bowl;
   put the egg shell into the bin.

Stir egg conetnts in the bowl.

Pour contents of bowl into the frying pan.
...
```

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Notice the way indenting has been used to group commands together.
 Numbering could also be used (1.1, 1.2, etc.)

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```
* Algorithm cup of water * ...
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If the level is above the line pour a little water out;

If the level is below the line pour a little water in;
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• Warning - potential for an infinite loop!

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• Warning - potential for an infinite loop!

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- ► Turn exact test into a "good enough" test see Lecture 4
- ► Add a stated limit on the number of iterations see Optimziation lectures

Recursion

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- Example:

```
* Algorithm factorial (n) *
If n == 1 then factorial = 1
    Else factorial = n * factorial(n - 1)
```

Code and Pseudocode

What is code?

• Code: instructions in a computer language that implement an algorithm.

• Example: factorial program in R

```
my.factorial <- function(n) {
   if (n == 1) {
      return(1)
   } else {
      return(n * my.factorial (n-1))
   }
}</pre>
```

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   if (n == 1) {
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   }
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```

• What's wrong with this function?

• Pseudocode: instructions in a generic, informal, unspecified computer language that specify an algorithm.

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- Tip: for anything other than completely trivial tasks, write out pseudocode on paper before writing any code on the computer!
 - ► (For more on this, see next lecture)

Control structures in R

Conditional execution

• Single condition

Multiple conditions

if
$$((x < 10) | (y >= 12)) z <- 44$$

if
$$((x < 10)&(y >= 12))$$
 z <- 44

Two alternative outcomes

```
if (x < 10) {
  y <- 44
} else {
  z <- 44
}</pre>
```

• Multiple alternative outcomes for the same variable

[1] "Wednesday will hold in store thrilling lecture"

 Multiple alternative outcomes via nested conditional statements - more flexible but less elegant

```
if (x < 10) {
  y <- 44
} else {
  if (p == 14) {
    z <- 44
} else {
    y <- x + a
    today <- "Wednesday"
}
}</pre>
```

Iteration (loops) - number of iterations known at outset

```
for (i in 1:10) {
  x[i] <- x[i] * pi
}</pre>
```

(Note - in many cases such loops can be vectorized.)

Iteration - number of iterations unknown at outset

While loop:

```
while (i < 27) {
  x[i] <- x[i] * pi
}</pre>
```

Repeat until loop:

```
repeat {
  x[i] <- x[i] * pi
  if (i >= 27) break
}
```

What is the difference between these?

Vectorization

 Many operations in R can be vectorized - these run much faster than loops

```
n<-1E8
x <- rnorm(n)
system.time(
  for (i in 1:n) {
    x[i] <- x[i] * pi
  }
)</pre>
```

```
## user system elapsed
## 14.18 0.03 14.33
```

```
n<-1E8
x <- rnorm(n)
system.time(
    x <- x * pi
)</pre>
```

```
## user system elapsed
## 0.16 0.05 0.21
```

If data organized into data frames or matrices

```
data(iris3)
apply(X = iris3, MARGIN = 2, FUN = mean)
```

```
## Sepal L. Sepal W. Petal L. Petal W. ## 5.843333 3.057333 3.758000 1.199333
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- If data organized into data frames or matrices
- You often need to iterate across colums or rows of the data

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- There are several variants of apply sapply, lapply, tapply, mapply, %by%
- See, e.g., Matloff (2011) Sections 5.2 and 5.4 (esp 5.4.2)
- Vectorization in R takes some getting used to but persistence pays off!

Modular programming

Modular programming

what is "modular programming"?

Splitting a program into discrete, reuseable blocks of code so that each block does a small amount.

Motivation

Convert -99 to NA in a dataset, of which this is a fraction

```
##
            b
                     d
                     5
## 1
            8 -99 -99 -99 6
   3
            5
                     5 - 99 4
       6 - 99
                     6
   4
## 5
            8
                6
            7
## 6 10
                9
                     9
                          5 5
```

```
df$a[df$a == -99] <- NA

df$b[df$b == -99] <- NA

df$c[df$c == -98] <- NA

df$d[df$d == -99] <- NA

df$e[df$e == -99] <- NA

df$f[df$g == -99] <- NA
```

What happened?

• Functions are the R way to implement modular programming

```
fix.missing <- function(x) {
   x[x == -99] <- NA
   return(x)
}

df$a <- fix.missing(df$a)
df$b <- fix.missing(df$b)
df$c <- fix.missing(df$c)
df$d <- fix.missing(df$d)
df$e <- fix.missing(df$d)</pre>
```

df\$f <- fix.missing(df\$e)</pre>

Functions are the R way to implement modular programming

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fix.missing <- function(x) {
  x[x == -99] \leftarrow NA
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df$a <- fix.missing(df$a)
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- Still too much redundant code
 - ▶ DRY principle
 - Don't Repeat Yourself

• Make use of inherent vectorisation in R

fix.missing(df)

```
##
              d
        7 2 5 2 4
## 1
         8 NA NA NA 6
## 3
         5
            9
               5 NA 4
       NA
            9
               6
            6
               1
## 6
     10
            9
               9
                  5 5
```

Modules in R

 In R, modular programming is implemented through the use of functions

```
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Modules in R

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- Syntax:

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```

Example R function

 Exploratory data analysis function - shows 3 plots and returns a summary of data vector x

```
eda <- function (x) {
  par(mfrow = c(1 ,3))
  hist(x, probability = TRUE)
  lines(density(x))
  boxplot(x, horizontal = TRUE)
  rug(x)
  qqnorm(x)
  return(summary(x))
}</pre>
```

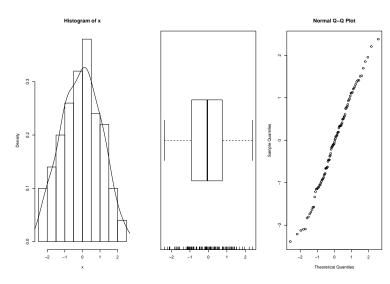
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}</pre>
```

• (N.B. There are a few "bad" things about this function – see next lecture for what!)

x <- rnorm(100) eda(x)</pre>



 In general programmer-speak, the things you pass into modules are called "parameters"

```
print.and.multiply <- function (x, y) {
    cat('Inside function x=', x, 'y=', y, '\n')
    return(x * y)
}</pre>
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    return(x * y)
}</pre>
```

• x and y are function arguments

```
print.and.multiply <- function (x, y) {</pre>
    cat('Inside function x=', x, 'y=', y, '\n')
    return(x * y)
var.1 < -10
var.2 < -20
print.and.multiply(var.1, var.2)
## Inside function x= 10 y= 20
```

• In computer languages, there are two ways to make parameters (arguments) available to functions:

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- These copies are stored in a separate location in memory from the original variables
- So, changes to the variable inside the function have no affect on its' value outside the function

```
print.and.multiply <- function (x, y) {</pre>
    cat('Inside function x=', x, 'y=', y, '\n')
    x \leftarrow x * y
    return(x)
var.1 < -10
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print.and.multiply(var.1, var.2)
## Inside function x= 10 y= 20
## [1] 200
var.1
```

• Aside - what would happen if you now typed x?

[1] 10

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- The memory location of the variable passed in is given to the function
- Therefore any changes to the variable within the function affect its' value after the function has completed
- The following code will not work in R as it does not allow passing by reference:

```
print.and.multiply <- function (ByReference x, y) {</pre>
    cat('Inside function x=', x, 'y=', y, '\n')
    x \leftarrow x * y
    return(x)
var.1 < -10
var.2 < -20
print.and.multiply(var.1, var.2)
## [1] 200
var.1
## [1] 200
```

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 - Inefficient the computer has to make a copy of all variables takes time and money
- Passing by reference
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 - Dangerous anything you do to the variables inside the function affects their value outside

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- So how do you get information out of a function in R?

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- Some (e.g., C) allow you to specify whether variables passed by value can be changed within the function - best of both worlds!
- Base R only supports passing by value
- So how do you get information out of a function in R?
 - ▶ Use return see next section!

• The main way to return values from functions is via the return statement

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print.and.multiply <- function (x, y) {
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```

• You can have more than one return statment (see factorial function earlier)

• If you want to return more than one variable, use a named list

```
print.and.multiply <- function (x, y) {
    return(list(x = x, y = y, mult = x * y))
}
print.and.multiply(10,20)</pre>
```

```
## [1] 10

##

## $y

## [1] 20

##

## $mult

## [1] 200
```

\$x

Pass everything requried by the function in as an argument

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- See next lecture for details, and many other tips for good programming practice...