

PBHL-B574_simulation_code

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2023-04-24

Simulation example 1 code

correlated data when $\rho = 0.5$.

```
library(PGEE) # requiring `mvtnorm` and `MASS` packages
set.seed(12345) # for reproducibility
# correlated normal responses
# True parameter vector

# covariate matrices
ar1_cor <- function(n, rho) {
  exponent <- abs(matrix(1:n - 1, nrow = n, ncol = n, byrow = TRUE) -
    (1:n - 1))
  rho^exponent
}
exch_cor <- function(n, rho) {
  mat <- matrix(rho, nrow = n, ncol = n)
  diag(mat) <- 1
  return(mat)
}

# strength of within cluster correlation
rho_values <- c(0.5, 0.8)

# Create the function to simulate data set
# consisting of N=200 study participants
# with 4 observations per participant
# p = 200 covariates
simulate<-function(N, rho){
  # The number of repeated measurements is 4
  timepoints=4
  # The number of covariates is 200
  p <- 200
  # b_0
  beta0 <- c(2, 3, 1.5, 2, rep(0, p - 4))
  # Simulate errors from MVN
  e_i <- c(sapply(1, function(x) t(mvrnorm(n = N, mu = rep(0, timepoints),
Sigma = exch_cor(4, rho)))) )
  # Generate ID variable
  id <- c(sapply(1:N, function(x) rep(x, timepoints)))
  # Simulate x_ij
  # x_ij,1 from Bernoulli(0.5)
```

```

x_1 <- c(sapply(1: N, function(x) rep(t(rbinom(1, 1, 0.5)),
                                     timepoints)))

# x_ij, 2-200 from MVN
x_2 <- matrix(sapply(1:(p-1), function(x) t(mvrnorm(n = N, mu =
rep(0,timepoints),
                                     Sigma =
ar1_cor(4,0.5))))), ncol=c(p-1))
colnames(x_2) <- paste0("x", 2:200)
X <- cbind(x_1,x_2)
# Simulate response
y<- X %%% beta0 +e_i
# Return data frame
data.frame(id,y,X)
}
# generate simulation data with correlated normal responses
data_sim1 <- simulate(N=200, rho=rho_values[1])
data_sim2 <- simulate(N=200, rho=rho_values[2])

colnames(data_sim1)[1:10]
head(data_sim1,5)[1:10]

formula <- "y ~.-id"
family <- gaussian(link = "identity")
lambda.vec <- seq(0.1,0.9,0.1)
# find the optimum lambda
cv_sim1 <- CVfit(formula = formula, id = id, data = data_sim1, family =
family, scale.fix = TRUE,
                scale.value = 1, fold = 4, lambda.vec = lambda.vec, pindex =
c(1,2), eps = 10^-6,
                maxiter = 30, tol = 10^-3)
print(cv_sim1) # 0.4 is the best lambda
names(cv_sim1)
cv_sim1$lam.opt
cv_sim2 <- CVfit(formula = formula, id = id, data = data_sim2, family =
family, scale.fix = TRUE,
                scale.value = 1, fold = 4, lambda.vec = lambda.vec, pindex =
c(1,2), eps = 10^-6,
                maxiter = 30, tol = 10^-3)
print(cv_sim2) # 0.5 is the best lambda
names(cv_sim2)
cv_sim2$lam.opt

# number of generated data set for each set up = 100
nsim=100
b0 <- c(2, 3, 1.5, 2, rep(0, 200 - 4))

# Perform the simulation - PGEE and rho=0.5
# Perform the simulation - rho=0.5
for(i in 1:nsim){

```

```

print(i)
N=200
rho=rho_values[1] # rho=0.5, 0.8
data<-simulate(N, rho)
myfit1_indp <- PGEE(formula = formula, id = id, data = data, na.action =
NULL,
                    family = family, constr = "independence", Mv = NULL,
                    beta_int = c(rep(0,dim(data)[2]-1)), R = NULL,
scale.fix = TRUE,
                    scale.value = 1, lambda = cv_sim1$lam.opt, pindex =
c(1,2), eps = 10^-6,
                    maxiter = 30, tol = 10^-6, silent = TRUE)
myfit1_exch <- PGEE(formula = formula, id = id, data = data, na.action =
NULL,
                    family = family, constr = "exchangeable", Mv = NULL,
                    beta_int = c(rep(0,dim(data)[2]-1)), R = NULL,
scale.fix = TRUE,
                    scale.value = 1, lambda = cv_sim1$lam.opt, pindex =
c(1,2), eps = 10^-6,
                    maxiter = 30, tol = 10^-6, silent = TRUE)
myfit1_ar1 <- PGEE(formula = formula, id = id, data = data, na.action =
NULL,
                    family = family, constr = "AR-1", Mv = NULL,
                    beta_int = c(rep(0,dim(data)[2]-1)), R = NULL, scale.fix
= TRUE,
                    scale.value = 1, lambda = cv_sim1$lam.opt, pindex =
c(1,2), eps = 10^-6,
                    maxiter = 30, tol = 10^-6, silent = TRUE)
pgee_b1 <- coef(myfit1_indp)
pgee_b2 <- coef(myfit1_exch)
pgee_b3 <- coef(myfit1_ar1)
myfit2_indp <- MGEE(formula = formula, id = id, data = data, na.action =
NULL,
                    family = family, constr = "independence", Mv = NULL,
                    beta_int = c(rep(0,dim(data)[2]-1)), R = NULL,
scale.fix = TRUE,
                    scale.value = 1,
                    maxiter = 30, tol = 10^-6, silent = TRUE)
myfit2_exch <- MGEE(formula = formula, id = id, data = data, na.action =
NULL,
                    family = family, constr = "exchangeable", Mv = NULL,
                    beta_int = c(rep(0,dim(data)[2]-1)), R = NULL,
scale.fix = TRUE,
                    scale.value = 1,
                    maxiter = 30, tol = 10^-6, silent = TRUE)
myfit2_ar1 <- MGEE(formula = formula, id = id, data = data, na.action =
NULL,
                    family = family, constr = "AR-1", Mv = NULL,
                    beta_int = c(rep(0,dim(data)[2]-1)), R = NULL, scale.fix
= TRUE,

```

```

        scale.value = 1,
        maxiter = 30, tol = 10^-6, silent = TRUE)
gee_b1 <- coef(myfit2_indp)
gee_b2 <- coef(myfit2_exch)
gee_b3 <- coef(myfit2_ar1)
myfit3_indp <- MGEE(formula = formula, id = id, data = data, na.action =
NULL,
                    family = family, constr = "independence", Mv = NULL,
                    beta_int = c(0, b0), R = NULL, scale.fix = TRUE,
                    scale.value = 1,
                    maxiter = 30, tol = 10^-6, silent = TRUE)
myfit3_exch <- MGEE(formula = formula, id = id, data = data, na.action =
NULL,
                    family = family, constr = "exchangeable", Mv = NULL,
                    beta_int = c(0, b0), R = NULL, scale.fix = TRUE,
                    scale.value = 1,
                    maxiter = 30, tol = 10^-6, silent = TRUE)
myfit3_ar1 <- MGEE(formula = formula, id = id, data = data, na.action =
NULL,
                    family = family, constr = "AR-1", Mv = NULL,
                    beta_int = c(0, b0), R = NULL, scale.fix = TRUE,
                    scale.value = 1,
                    maxiter = 30, tol = 10^-6, silent = TRUE)
oracle_b1 <- coef(myfit3_indp)
oracle_b2 <- coef(myfit3_exch)
oracle_b3 <- coef(myfit3_ar1)
if(i==1){
  pgee1_beta1<-pgee_b1
  pgee1_beta2<-pgee_b2
  pgee1_beta3<-pgee_b3
  gee1_beta1<-gee_b1
  gee1_beta2<-gee_b2
  gee1_beta3<-gee_b3
  oracle1_beta1<-oracle_b1
  oracle1_beta2<-oracle_b2
  oracle1_beta3<-oracle_b3
} else {
  pgee1_beta1<-rbind(pgee1_beta1,pgee_b1)
  pgee1_beta2<-rbind(pgee1_beta2,pgee_b2)
  pgee1_beta3<-rbind(pgee1_beta3,pgee_b3)
  gee1_beta1<-rbind(gee1_beta1,gee_b1)
  gee1_beta2<-rbind(gee1_beta2,gee_b2)
  gee1_beta3<-rbind(gee1_beta3,gee_b3)
  oracle1_beta1<-rbind(oracle1_beta1,oracle_b1)
  oracle1_beta2<-rbind(oracle1_beta2,oracle_b2)
  oracle1_beta3<-rbind(oracle1_beta3,oracle_b3)
}}

# MSE when rho=0.5
pgee1_mse <- c(mean(colSums((pgee1_beta1[, -1] - b0)^2))/nrow(pgee1_beta1),

```

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        mean(colSums((pgee1_beta2[, -1] - b0)^2))/nrow(pgee1_beta2),
        mean(colSums((pgee1_beta3[, -1] - b0)^2))/nrow(pgee1_beta3))
names(pgee1_mse) <- c("indp", "exch", "ar1")
gee1_mse <- c(mean(colSums((gee1_beta1[, -1] - b0)^2))/nrow(gee1_beta1),
             mean(colSums((gee1_beta2[, -1] - b0)^2))/nrow(gee1_beta2),
             mean(colSums((gee1_beta3[, -1] - b0)^2))/nrow(gee1_beta3))
names(gee1_mse) <- c("indp", "exch", "ar1")
oracle1_mse <- c(mean(colSums((oracle1_beta1[, -1] -
b0)^2))/nrow(oracle1_beta1),
                mean(colSums((oracle1_beta2[, -1] -
b0)^2))/nrow(oracle1_beta2),
                mean(colSums((oracle1_beta3[, -1] -
b0)^2))/nrow(oracle1_beta3))
names(oracle1_mse) <- c("indp", "exch", "ar1")

# U/O/EXACT when rho=0.5
num_indp_pgee1 <- apply(pgee1_beta1[, -1], 1, function(x) sum(abs(x) > 10^-3))
num_exch_pgee1 <- apply(pgee1_beta2[, -1], 1, function(x) sum(abs(x) > 10^-3))
num_ar1_pgee1 <- apply(pgee1_beta3[, -1], 1, function(x) sum(abs(x) > 10^-3))
prop_pgee1_indp <- c(mean(num_indp_pgee1 < 4), mean(num_indp_pgee1 > 4),
mean(num_indp_pgee1 == 4))
prop_pgee1_exch <- c(mean(num_exch_pgee1 < 4), mean(num_exch_pgee1 > 4),
mean(num_exch_pgee1 == 4))
prop_pgee1_ar1 <- c(mean(num_ar1_pgee1 < 4), mean(num_ar1_pgee1 > 4),
mean(num_ar1_pgee1 == 4))
prop_pgee1 <- rbind(prop_pgee1_indp, prop_pgee1_exch, prop_pgee1_ar1)
colnames(prop_pgee1) <- c("U", "O", "EXACT")
rownames(prop_pgee1) <- c("pgee1_indp", "pgee1_exch", "pgee1_ar1")
prop_pgee1
num_indp_gee1 <- apply(gee1_beta1[, -1], 1, function(x) sum(abs(x) > 10^-3))
num_exch_gee1 <- apply(gee1_beta2[, -1], 1, function(x) sum(abs(x) > 10^-3))
num_ar1_gee1 <- apply(gee1_beta3[, -1], 1, function(x) sum(abs(x) > 10^-3))
prop_gee1_indp <- c(mean(num_indp_gee1 < 4), mean(num_indp_gee1 > 4),
mean(num_indp_gee1 == 4))
prop_gee1_exch <- c(mean(num_exch_gee1 < 4), mean(num_exch_gee1 > 4),
mean(num_exch_gee1 == 4))
prop_gee1_ar1 <- c(mean(num_ar1_gee1 < 4), mean(num_ar1_gee1 > 4),
mean(num_ar1_gee1 == 4))
prop_gee1 <- rbind(prop_gee1_indp, prop_gee1_exch, prop_gee1_ar1)
colnames(prop_gee1) <- c("U", "O", "EXACT")
rownames(prop_gee1) <- c("gee1_indp", "gee1_exch", "gee1_ar1")
prop_gee1
# TP when rho=0.5
mean(apply(pgee1_beta1[, 2:5], 1, function(x) sum(abs(x) > 10^-3)))
mean(apply(pgee1_beta2[, 2:5], 1, function(x) sum(abs(x) > 10^-3)))
mean(apply(pgee1_beta3[, 2:5], 1, function(x) sum(abs(x) > 10^-3)))
mean(apply(gee1_beta1[, 2:5], 1, function(x) sum(abs(x) > 10^-3)))
mean(apply(gee1_beta2[, 2:5], 1, function(x) sum(abs(x) > 10^-3)))
mean(apply(gee1_beta3[, 2:5], 1, function(x) sum(abs(x) > 10^-3)))
# FP when rho=0.5

```

```

mean(apply(pgee1_beta1[, -c(1:5)], 1, function(x) sum(abs(x) > 10^-3)))
mean(apply(pgee1_beta2[, -c(1:5)], 1, function(x) sum(abs(x) > 10^-3)))
mean(apply(pgee1_beta3[, -c(1:5)], 1, function(x) sum(abs(x) > 10^-3)))
mean(apply(ggee1_beta1[, -c(1:5)], 1, function(x) sum(abs(x) > 10^-3)))
mean(apply(ggee1_beta2[, -c(1:5)], 1, function(x) sum(abs(x) > 10^-3)))
mean(apply(ggee1_beta3[, -c(1:5)], 1, function(x) sum(abs(x) > 10^-3)))

```

correlated data when $\rho = 0.8$.

Perform the simulation - rho=0.8

```

for(i in 1:nsim){
  print(i)
  N=200
  rho=rho_values[2] # rho=0.5, 0.8
  data<-simulate(N, rho)
  myfit1_indp <- PGEE(formula = formula, id = id, data = data, na.action =
NULL,
                      family = family, constr = "independence", Mv = NULL,
                      beta_int = c(rep(0,dim(data)[2]-1)), R = NULL,
scale.fix = TRUE,
                      scale.value = 1, lambda = cv_sim1$lam.opt, pindex =
c(1,2), eps = 10^-6,
                      maxiter = 30, tol = 10^-6, silent = TRUE)
  myfit1_exch <- PGEE(formula = formula, id = id, data = data, na.action =
NULL,
                      family = family, constr = "exchangeable", Mv = NULL,
                      beta_int = c(rep(0,dim(data)[2]-1)), R = NULL,
scale.fix = TRUE,
                      scale.value = 1, lambda = cv_sim1$lam.opt, pindex =
c(1,2), eps = 10^-6,
                      maxiter = 30, tol = 10^-6, silent = TRUE)
  myfit1_ar1 <- PGEE(formula = formula, id = id, data = data, na.action =
NULL,
                      family = family, constr = "AR-1", Mv = NULL,
                      beta_int = c(rep(0,dim(data)[2]-1)), R = NULL, scale.fix
= TRUE,
                      scale.value = 1, lambda = cv_sim1$lam.opt, pindex =
c(1,2), eps = 10^-6,
                      maxiter = 30, tol = 10^-6, silent = TRUE)
  pgee_b1 <- coef(myfit1_indp)
  pgee_b2 <- coef(myfit1_exch)
  pgee_b3 <- coef(myfit1_ar1)
  myfit2_indp <- MGEE(formula = formula, id = id, data = data, na.action =
NULL,
                      family = family, constr = "independence", Mv = NULL,
                      beta_int = c(rep(0,dim(data)[2]-1)), R = NULL,
scale.fix = TRUE,
                      scale.value = 1,
                      maxiter = 30, tol = 10^-6, silent = TRUE)
  myfit2_exch <- MGEE(formula = formula, id = id, data = data, na.action =
NULL,

```

```

        family = family, constr = "exchangeable", Mv = NULL,
        beta_int = c(rep(0,dim(data)[2]-1)), R = NULL,
scale.fix = TRUE,
        scale.value = 1,
        maxiter = 30, tol = 10^-6, silent = TRUE)
myfit2_ar1 <- MGEE(formula = formula, id = id, data = data, na.action =
NULL,
        family = family, constr = "AR-1", Mv = NULL,
        beta_int = c(rep(0,dim(data)[2]-1)), R = NULL, scale.fix
= TRUE,
        scale.value = 1,
        maxiter = 30, tol = 10^-6, silent = TRUE)
gee_b1 <- coef(myfit2_indp)
gee_b2 <- coef(myfit2_exch)
gee_b3 <- coef(myfit2_ar1)
myfit3_indp <- MGEE(formula = formula, id = id, data = data, na.action =
NULL,
        family = family, constr = "independence", Mv = NULL,
        beta_int = c(0, b0), R = NULL, scale.fix = TRUE,
        scale.value = 1,
        maxiter = 30, tol = 10^-6, silent = TRUE)
myfit3_exch <- MGEE(formula = formula, id = id, data = data, na.action =
NULL,
        family = family, constr = "exchangeable", Mv = NULL,
        beta_int = c(0, b0), R = NULL, scale.fix = TRUE,
        scale.value = 1,
        maxiter = 30, tol = 10^-6, silent = TRUE)
myfit3_ar1 <- MGEE(formula = formula, id = id, data = data, na.action =
NULL,
        family = family, constr = "AR-1", Mv = NULL,
        beta_int = c(0, b0), R = NULL, scale.fix = TRUE,
        scale.value = 1,
        maxiter = 30, tol = 10^-6, silent = TRUE)
oracle_b1 <- coef(myfit3_indp)
oracle_b2 <- coef(myfit3_exch)
oracle_b3 <- coef(myfit3_ar1)
if(i==1){
  pgee2_beta1<-pgee_b1
  pgee2_beta2<-pgee_b2
  pgee2_beta3<-pgee_b3
  gee2_beta1<-gee_b1
  gee2_beta2<-gee_b2
  gee2_beta3<-gee_b3
  oracle2_beta1<-oracle_b1
  oracle2_beta2<-oracle_b2
  oracle2_beta3<-oracle_b3
} else {
  pgee2_beta1<-rbind(pgee2_beta1,pgee_b1)
  pgee2_beta2<-rbind(pgee2_beta2,pgee_b2)
  pgee2_beta3<-rbind(pgee2_beta3,pgee_b3)

```

```

gee2_beta1<-rbind(gee2_beta1,gee_b1)
gee2_beta2<-rbind(gee2_beta2,gee_b2)
gee2_beta3<-rbind(gee2_beta3,gee_b3)
oracle2_beta1<-rbind(oracle2_beta1,oracle_b1)
oracle2_beta2<-rbind(oracle2_beta2,oracle_b2)
oracle2_beta3<-rbind(oracle2_beta3,oracle_b3)
}}

##### test: initial beta values = 0 #####
#####
#####
#####
#####
for(i in 1:2){
  print(i)
  N=200
  rho=rho_values[1] # rho=0.5, 0.8
  data<-simulate(N, rho)
  myfit1_indp <- PGEE(formula = formula, id = id, data = data, na.action =
NULL,
                      family = family, constr = "independence", Mv = NULL,
                      beta_int = NULL, R = NULL, scale.fix = TRUE,
                      scale.value = 1, lambda = cv_sim1$lam.opt, pindex =
c(1,2), eps = 10^-6,
                      maxiter = 30, tol = 10^-6, silent = TRUE)
  myfit1_exch <- PGEE(formula = formula, id = id, data = data, na.action =
NULL,
                      family = family, constr = "exchangeable", Mv = NULL,
                      beta_int = NULL, R = NULL, scale.fix = TRUE,
                      scale.value = 1, lambda = cv_sim1$lam.opt, pindex =
c(1,2), eps = 10^-6,
                      maxiter = 30, tol = 10^-6, silent = TRUE)
  myfit1_ar1 <- PGEE(formula = formula, id = id, data = data, na.action =
NULL,
                      family = family, constr = "AR-1", Mv = NULL,
                      beta_int = NULL, R = NULL, scale.fix = TRUE,
                      scale.value = 1, lambda = cv_sim1$lam.opt, pindex =
c(1,2), eps = 10^-6,
                      maxiter = 30, tol = 10^-6, silent = TRUE)
  pgee_b1 <- coef(myfit1_indp)
  pgee_b2 <- coef(myfit1_exch)
  pgee_b3 <- coef(myfit1_ar1)
  myfit2_indp <- MGEE(formula = formula, id = id, data = data, na.action =
NULL,
                      family = family, constr = "independence", Mv = NULL,
                      beta_int = NULL, R = NULL, scale.fix = TRUE,
                      scale.value = 1,
                      maxiter = 30, tol = 10^-6, silent = TRUE)
  myfit2_exch <- MGEE(formula = formula, id = id, data = data, na.action =
NULL,

```



```

        family = family, constr = "exchangeable", Mv = NULL,
        beta_int = NULL, R = NULL, scale.fix = TRUE,
        scale.value = 1,
        maxiter = 30, tol = 10^-6, silent = TRUE)
myfit2_ar1 <- MGEE(formula = formula, id = id, data = data, na.action =
NULL,
        family = family, constr = "AR-1", Mv = NULL,
        beta_int = NULL,
        R = NULL, scale.fix = TRUE,
        scale.value = 1,
        maxiter = 30, tol = 10^-6, silent = TRUE)
gee_b1 <- coef(myfit2_indp)
gee_b2 <- coef(myfit2_exch)
gee_b3 <- coef(myfit2_ar1)
myfit3_indp <- MGEE(formula = formula, id = id, data = data, na.action =
NULL,
        family = family, constr = "independence", Mv = NULL,
        beta_int = c(b0), R = NULL, scale.fix = TRUE,
        scale.value = 1,
        maxiter = 30, tol = 10^-6, silent = TRUE)
myfit3_exch <- MGEE(formula = formula, id = id, data = data, na.action =
NULL,
        family = family, constr = "exchangeable", Mv = NULL,
        beta_int = c(b0), R = NULL, scale.fix = TRUE,
        scale.value = 1,
        maxiter = 30, tol = 10^-6, silent = TRUE)
myfit3_ar1 <- MGEE(formula = formula, id = id, data = data, na.action =
NULL,
        family = family, constr = "AR-1", Mv = NULL,
        beta_int = c(b0), R = NULL, scale.fix = TRUE,
        scale.value = 1,
        maxiter = 30, tol = 10^-6, silent = TRUE)
oracle_b1 <- coef(myfit3_indp)
oracle_b2 <- coef(myfit3_exch)
oracle_b3 <- coef(myfit3_ar1)
if(i==1){
  pgee1_beta1<-pgee_b1
  pgee1_beta2<-pgee_b2
  pgee1_beta3<-pgee_b3
  gee1_beta1<-gee_b1
  gee1_beta2<-gee_b2
  gee1_beta3<-gee_b3
  oracle1_beta1<-oracle_b1
  oracle1_beta2<-oracle_b2
  oracle1_beta3<-oracle_b3
} else {
  pgee1_beta1<-rbind(pgee1_beta1,pgee_b1)
  pgee1_beta2<-rbind(pgee1_beta2,pgee_b2)
  pgee1_beta3<-rbind(pgee1_beta3,pgee_b3)
  gee1_beta1<-rbind(gee1_beta1,gee_b1)

```

```

gee1_beta2<-rbind(gee1_beta2,gee_b2)
gee1_beta3<-rbind(gee1_beta3,gee_b3)
oracle1_beta1<-rbind(oracle1_beta1,oracle_b1)
oracle1_beta2<-rbind(oracle1_beta2,oracle_b2)
oracle1_beta3<-rbind(oracle1_beta3,oracle_b3)
}}

```

real-world data

```

library(PGEE) # requiring `mvtnorm` and `MASS` packages
# Load data
data(yeastG1)
data = yeastG1
# get the column names
colnames(data)[1:9]
# see some portion of yeast G1 data
head(data,5)[1:9]
# define the input arguments
formula <- "y ~.-id"
family <- gaussian(link = "identity")
lambda.vec <- seq(0.01,0.2,0.01)
# find the optimum lambda
cv <- CVfit(formula = formula, id = id, data = data, family = family,
scale.fix = TRUE,
            scale.value = 1, fold = 4, lambda.vec = lambda.vec, pindex =
c(1,2), eps = 10^-6,
            maxiter = 30, tol = 10^-6)
# print the results
print(cv)
# see the returned values by CVfit
names(cv)
# get the optimum lambda
cv$lam.opt
# fit the PGEE model
myfit1 <- PGEE(formula = formula, id = id, data = data, na.action = NULL,
              family = family, constr = "independence", Mv = NULL,
              beta_int = c(rep(0,dim(data)[2]-1)), R = NULL, scale.fix =
TRUE,
              scale.value = 1, lambda = cv$lam.opt, pindex = c(1,2), eps =
10^-6,
              maxiter = 30, tol = 10^-6, silent = TRUE)
# get the values returned by myfit object
names(myfit1)

# see a portion of the results returned by coef(summary(myfit1))
head(coef(summary(myfit1)),7)

# see the variables which have non-zero coefficients
index1 <- which(abs(coef(summary(myfit1))[, "Estimate"]) > 10^-3)
names(abs(coef(summary(myfit1))[index1, "Estimate"]))
# see the PGEE summary statistics of these non-zero variables

```

```

coef(summary(myfit1))[index1,]
# fit the GEE model
myfit2 <- MGEE(formula = formula, id = id, data = data, na.action = NULL,
               family = family, corstr = "independence", Mv = NULL,
               beta_int = c(rep(0,dim(data)[2]-1)), R = NULL, scale.fix =
TRUE,
               scale.value = 1, maxiter = 30, tol = 10^-6, silent = TRUE)
# see the significantly associated TFs in PGEE analysis
names(which(abs(coef(summary(myfit1))[index1,"Robust z"]) > 1.96))

# see the significantly associated TFs in GEE analysis
names(which(abs(coef(summary(myfit2))[, "Robust z"]) > 1.96))

```