



✓ **Congratulations! You passed!**

TO PASS 70% or higher

Keep Learning

GRADE

71.42%

## Big-O

TOTAL POINTS 7

### 1. Introduction and Learning Outcomes

1 / 1 point

The goal of this assignment is to practice with big-O notation.

Recall that we write  $f(n) = O(g(n))$  to express the fact that  $f(n)$  grows no faster than  $g(n)$ : there exist constants  $N$  and  $c > 0$  so that for all  $n \geq N$ ,  $f(n) \leq c \cdot g(n)$ .

Is it true that  $\log_2 n = O(n^2)$ ?

☒ Yes

☐ No

✓ **Correct**

A logarithmic function grows slower than a polynomial function.

### 2. $n \log_2 n = O(n)$

0 / 1 point

☐ Yes

☐ No

✗ **Incorrect**

You didn't select an answer.

### 3. $n^2 = O(n^3)$

1 / 1 point

☒ Yes

☐ No

✓ **Correct**

$n^a$  grows slower than  $n^b$  for constants  $a < b$ .

### 4. $n = O(\sqrt{n})$

1 / 1 point

☐ Yes

☒ No

✓ **Correct**

$\sqrt{n} = n^{1/2}$  grows slower than  $n = n^1$  as  $1/2 < 1$ .

### 5. $5^{\log_2 n} = O(n^2)$

1 / 1 point

☐ Yes

☒ No

✓ **Correct**

Recall that  $a^{\log_b c} = c^{\log_b a}$  so  $5^{\log_2 n} = n^{\log_2 5}$ . This grows faster than  $n^2$  since  $\log_2 5 = 2.321\dots > 2$ .

### 6. $n^5 = O(2^{3 \log_2 n})$

0 / 1 point

☒ Yes

☐ No

✗ **Incorrect**

Hint:  $2^{n \log_2 n} = (2^{\log_2 n})^n = n^n$

7.  $2^n = O(2^{n+1})$

1 / 1 point

☒ Yes

☐ No

✓ **Correct**

$2^{n+1} = 2 \cdot 2^n$ , that is,  $2^n$  and  $2^{n+1}$  have the same growth rate and hence  $2^n = \Theta(2^{n+1})$ .