



✓ **Congratulations! You passed!**  
TO PASS 60% or higher

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66.66%

## Hashing

TOTAL POINTS 3

1. What is the minimum size of an array that can be used in the direct addressing scheme to store a map from 7-digit phone numbers to names?

1 / 1 point

- ☒ 10000000  
☐ 20000000  
☐ 1000000

✓ **Correct**

Correct! 7-digit phone numbers correspond to integers from 0 to 9999999.

2. If it is guaranteed that the total length of all occurrences of a *Pattern* in a *Text* is at most  $L$ , which of the below estimates of the average running time of Rabin-Karp's algorithm to find all occurrences of the *Pattern* in the *Text* is the most tight out of the correct ones?

1 / 1 point

- ☐  $O(|Text| |Pattern| + L)$   
☐  $O(|Text| |Pattern| L)$   
☒  $O(|Text| + |Pattern| + L)$   
☐  $O(|Text| + |Pattern|)$

✓ **Correct**

Correct! Estimate from the lecture is  $O(|Text| + (q + 1)|Pattern|)$ , where  $q$  is the number of occurrences of the *Pattern* in the *Text*, and  $L = q|Pattern|$  in this case.

3. Let us slightly change the polynomial hash function for strings and set  $h(S) = (\sum_{j=0}^{|S|-1} x^{|S|-1-j} S[j]) \bmod p$ . Let us fix some *Text* and some *Pattern*. Denote by  $H[i]$  the hash function of the substring  $Text[i..i + |Pattern| - 1]$  of the *Text* starting from position  $i$  and having the same length as *Pattern* (for all appropriate positions  $i$  where the *Pattern* can occur in the *Text*). Which of the below formulas is the correct recurrence to compute  $H[i + 1]$  given  $H[i]$ ?

0 / 1 point

- ☐  $H[i + 1] = (xH[i] + Text[i + |Pattern| - 1] - x^{|Pattern|} Text[i]) \bmod p$   
☒  $H[i + 1] = (xH[i] + x^{|Pattern|} Text[i + |Pattern|] - Text[i]) \bmod p$   
☐  $H[i] = (xH[i + 1] + Text[i] - x^{|Pattern|} Text[i + |Pattern|]) \bmod p$   
☐  $H[i + 1] = (xH[i] + Text[i + |Pattern|] - x^{|Pattern|} Text[i]) \bmod p$

✗ **Incorrect**

Note that the first letter of the substring should be multiplied by the largest power of  $x$ , and the last letter of the substring should be multiplied by  $x^0 = 1$  while computing the hash function for it.