

# **PHYS 170 Study Notes**

## **Mechanics**

Yecheng Liang

# Contents

1. General Principles .....	3
1.1. The Four Horseman of Mechanics .....	3
1.2. US Customary Units .....	3
1.3. Gravity .....	3
1.4. Vector Notation .....	3
1.5. Angle Unit .....	3
2. Force Vectors .....	4
2.1. Addition .....	4
2.2. Force Components .....	4
3. Equilibrium of a Particle .....	5
4. Force System Resultants .....	6
5. Equilibrium of a Rigid Body .....	7
6. Friction .....	8
7. Kinematics of a Particle .....	9
8. Kinetics of a Particle: Force and Acceleration .....	10
9. Kinetics of a Particle: Work and Energy .....	11
10. Kinetics of a Particle: Impulse and Momentum .....	12

# 1. General Principles

## 1.1. The Four Horseman of Mechanics

- Length
- Mass
- Time
- Force

So you basically take three of them and solve the 1 left.

## 1.2. US Customary Units

LENGTH	MASS	TIME	FORCE
meter m	kilogram kg	second s	force $\text{kg m s}^{-2}$
foot ft	slug $\text{lb s}^2 \text{ft}^{-1}$	second s	pound lb

Table 1: SI and US Customary (FPS) Units for Mechanics

## 1.3. Gravity

$$F = G \frac{m_1 m_2}{r^2} \quad (1.1)$$

$$F = ma \quad (1.2)$$

In this course, we will use

$$g = 9.81 \text{ m s}^{-2} \quad (2)$$

which happens to be true for Vancouver.

## 1.4. Vector Notation

In this course, vectors are upright bold, and vector magnitudes are italicized bold.

$$\mathbf{A} \text{ has a magnitude of } \mathbf{A}. \quad (3)$$

## 1.5. Angle Unit

In this course, angles are in degrees.

## 2. Force Vectors

Force, having both magnitude and direction, is a vector. Intuitively, we can apply all kinds of vector operations to forces, as you would learn in MATH 152.

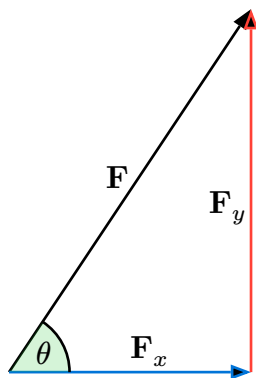
### 2.1. Addition

Use “Tip to tail” for triangular method of addition: draw the vectors head to tail, and the resultant vector is the vector from the tail of the first vector to the head of the last vector.

### 2.2. Force Components

$$\mathbf{F} = x\mathbf{i} + y\mathbf{j} \quad (4)$$

where  $x, y$  are magnitudes of the force in the  $\mathbf{i}, \mathbf{j}$  directions.



Force  $\mathbf{F}$  can be represented as a combination of  $\mathbf{F}_x$  and  $\mathbf{F}_y$

$$\mathbf{F} = \mathbf{F}_x + \mathbf{F}_y \quad (5)$$

or as a polar coordinate of angle  $\theta = \arctan\left(\frac{\mathbf{F}_y}{\mathbf{F}_x}\right)$  and magnitude  $\mathbf{F}$

$$\mathbf{F} = \mathbf{F}(\cos(\theta) + \sin(\theta)) \quad (6)$$

### **3. Equilibrium of a Particle**

## **4. Force System Resultants**

## 5. Equilibrium of a Rigid Body

## 6. Friction



## **7. Kinematics of a Particle**

## **8. Kinetics of a Particle: Force and Acceleration**

## **9. Kinetics of a Particle: Work and Energy**

## **10. Kinetics of a Particle: Impulse and Momentum**