Experimental Analysis of the Tournament Size on Genetic Algorithms

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ABSTRACT

We perform an experimental study about the effect of the tournament size parameter from the Tournament Selection operator. Tournament Selection is a classic operator for Genetic Algorithms and Genetic Programming. It is simple to implement and has only one control parameter, the tournament size. Even though it is commonly used, most practitioners still rely on rules of thumb when choosing the tournament size. For example, almost all works in the past 15 years use a value of 2 for the tournament size, with little reasoning behind that choice. To understand the role of the tournament size, we run a real-valued GA on 24 BBOB problems with 10, 20 and 40 dimensions. We also vary the crossover operator and the generational policy of the GA. For each combination of the above factors we observe how the quality of the final solution changes with the tournament size. Our findings do not support the indiscriminate use of tournament size 2, and recommend a more careful set up of this parameter.

CCS CONCEPTS

Computing methodologies → Genetic algorithms;

KEYWORDS

Genetic Algorithm, Tournament Selection, Selection Schemes

ACM Reference Format:

1 INTRODUCTION

The Tournament Selection is a very popular selection operator for Genetic Algorithms and Evolutionary Computation in general. Some of the reasons for this popularity are that it is very simple to implement, and that it has a single control parameter, the *Tournament Size*, also known as "Tournament's k".

How should the value of the Tournament Size be chosen? Early works claimed that the value of k could be used to control the balance between exploration and exploitation in the search [6]. As k gets larger, the selection pressure is expected to increase, and better solutions are expected to exert a larger influence in the following generations [17].

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GECCO '18, July 15–19, 2018, Kyoto, Japan
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ACM ISBN 978-x-xxxx-xxxx-x/YY/MM...\$15.00

On the other hand, works in the past 15 years have commonly used very small values for k, such as 2 or 3 [4, 7, 15, 19, 20, 22, 23]. The reason for this change is hard to identify, as most papers either do not justify their choice of parameters, or lightly mention a concern over computational cost for this rule of thumb.

Precious few works look too closely at their choice of tournament size. One example is Nicolau [19] who tried to empirically define a relationship between population size and tournament size for fine tuning a binary GA.

In order to question and further understand these assumptions and rules of thumb, we present an experimental study on the role of the tournament selection size. Our study focuses on a real-valued GA applied to the noise-free Black Box Optimization Benchmark (BBOB) functions.

We vary the mutation operator (uniform or SBX), the generational scheme, the modality of the objective function (unimodal or multimodal), and the dimensionality of the objective function (10, 20, 40). We observe how the quality of the final answer changes as the value of k changes.

Our results show that for functions with only one local optimum (easier problems), the choice of k does not show an effect on the final result. For harder problems, when the functions have many local optimum we saw an effect. The exact best value of k may depend on the function, dimensionality and algorithm composition and this relationship is not clear. Instead of using k equals to 2 or 3, we recommend that the choice of this parameter be considered more carefully.

2 THE TOURNAMENT SELECTION

A selection scheme is a process that aims to improve the average quality of the GA by giving solutions of higher quality a higher probability of composing the next generation [6]. The tournament selection, as any selection mechanism in GA, simply favors the selection of better individuals of a population to influence the next generation.

Tournament Selection is a selection scheme that has a unique set of characteristics that makes it a very popular choice [6]. It is simple to code, and its complexity is O(n) on the size of the population [9] which makes it efficient for both nonparallel and parallel architectures.

The tournament selection is also translation and scaling invariant [16], which means that the behavior of the selection scheme is not affected by the scale of the fitness values [2].

It is often claimed that the tournament selection is able to adjust the selection pressure by changing its only parameter, which controls the number of individuals chosen to take part in the tournament. That is an important feature, because any selection scheme should have the capacity to adjust its selection pressure given different domains. When only two individuals are selected, it is often

called a binary tournament [6, 9], which is a popular choice. However, in principle there is no limit for the size of the tournament.

2.1 The Tournament Selection Procedure

Tournament selection is conducted as: choose a number K of solutions randomly from the population and select the best solution from this group as a parent for the crossover operator. Repeat this operation for each parent necessary. This K is the tournament size parameter that we investigate in this paper.

2.2 Selection Schemes and BBOB functions

Holtschulte and Moses [14] used rank selection in their GA implementation and applied it to the BBOB functions. They declared that rank selection should be replaced by an elitism selection scheme to improve the performance of their GA implementation by spreading of high quality solutions through the population.

The roulette-wheel and the tournament selection are two of these elitist selection schemes. However, it has been shown that roulette-wheel leads to premature convergence [3].

Nicolau, [19] used the tournament selection in his GA with the goal of solving the BBOB functions. He declares "for harder problem domains, such as the ones on the BBOB-Benchmark suite, the tournament selection scheme is more appropriate.".

These two studies in addition to the tournament selection popularity and its power to be adjusted for different domains, give us motive to analyze the tournament selection behavior considering the BBOB functions.

2.3 Tournament Pressure

Muhlenbein et al., in [18], introduced the concept of selection intensity, which is to measure the pressure of selection schemes. The selection intensity is defined as the expected average fitness of the population after selection. This definition can only be applied because the tournament selection is scale and translation invariant [6].

Blickle et. al [6], declare that the selection intensity can be analytically calculated for tournament sizes of 2 and 3 and for larger values with numerical integration. They calculate the selection intensity for values between 2 and 30 and showed that with higher values for the tournament size the selection intensity increases. This calculation allows the prediction of the convergence time and can be used to compare different selection schemes.

Blickle et .al [5] compared some selection schemes, given their selection intensity. They concluded that for the same selection intensity the tournament selection has the smallest loss of diversity and the highest selection variance when compared with the truncation selection, the linear ranking, the exponential rank, and the proportional rank.

Miller et al. [17], argued that with higher tournament sizes, the selection pressure rises resulting in higher convergence rates, because the convergence rate of a GA is largely determined by the selection pressure. Accordingly, if the selection pressure is too low, the convergence rate will be slower if it is too high, there is an increased chance of the GA prematurely converging.

Based on the studies from above, we understand that the convergence directly influences the the final results of a GA, once any

variation on the convergence rates changes the lost of diversity, and the selection variance. Consequently, it is important to explore the values for tournament size, since this value seems to determine the balance of exploration and exploitation by changing the selection intensity. It is possible that this balance could vary given a domain, once it is expected that every domain holds a specific characteristic that would need a different proportion of this balance.

2.4 Tournament Size in the Literature

In 1991, Goldberg [8], analyzed the tournament selection with size 2 in a real-coded GA. He recognized empirically that after some time only individuals with relatively high function values would be represented in the population. He recognizes that selection may emphasize highly fit individuals leading to a small number of alternatives considered.

Agrawal [1], in 1995, implemented real-coded GA with tournament selection with size 2. Their goal was to compare the results of the simulated binary crossover (SBX) with the binary single-point crossover and the blend crossover. They concluded that the SBX has search power similar to the single-point crossover and the SBX performs better in difficult test functions than the blend crossover. They understand that for some functions the selection pressure is not enough.

In 1999, Tsutsui et al. [24] proposed a simplex crossover (SPX), a multi-parent recombination operator for real-coded genetic algorithms. For their experiments, they used a real-coded GA with tournament selection with size 2 and showed that "SPX works well on functions having multi modality and/or epistasis with a medium number of parents: 3-parent on a low dimensional function or 4 parents on high dimensional functions.".

Later, in 2000, Deb [7], implemented a binary GA and a real-coded GA, with tournament size 2. He aimed to devise a penalty function approach that does not require any penalty parameter. Because all of their search spaces are defined in the real space, the real-coded GA was more suited in finding feasible solutions, but in all cases, this approach " [has] a niche over classical methods to handle constraints". The concluded with declaring that some parametric study should be done on the important parameters to improve the performance.

In 2001, Beyer et al. [4], analyzed the results of using the simulated binary crossover (SBX), the fuzzy recombination operator and the blend crossover (BLX), all with no mutation and tournament size 2 in a real-coded GA. The results indicated that those crossovers exhibit similar performance and linear convergence order.

Sawyerr et al. [22], in 2015, proposed the RCGAu, hybrid real-coded genetic algorithm with "uniform random direction" search mechanism. They used tournament selection with size 3 to explore the suite of noiseless black-box optimization testbed and the results showed great performance in some functions such as f_7 and f_{21} .

Goldberg et AL [10], in 1993, implemented a binary GA using the tournament selection as a convenient way to control selection pressure. They wanted to study the theory aspects of the GA focusing in the mixing building block. The actual effect of the tournament value was not investigated empirically in the work.

In 1999, Harik et al. [13] studied a simple GA and experimented with the tournament size. Their work shows that a given solution

quality can be obtained faster by the tournament size equal to 4 or 8, instead of tournament size equal to 2 or 40.

Also, Harik et al. [12] implement a binary coded GA using tournament selection. They analyze the impact of the tournament size on their GA with a 100-bit one-max function. They inspected this implementation with tournament sizes of 2, 4, and 8. They observed that the proportion of the building blocks changed with the tournament size, being higher for smaller tournament sizes.

In 2007, Kaelo et al. [15] compared the usage of the tournament size in a real-coded GA. They discuss the impact of using tournament size of 2 and tournament size of 3. The results of comparing these two tournament sizes indicated that the tournament with size 3 is more greedy, reduces the number of functions evaluations greatly and also improves CPU usage, therefore, it impacts negatively in the success rate of their GA.

Also in 2009, Nicolau [19] implemented a binary GA to solve the noise-free BBOB 2009 testbed. Trough a quick experimentation with a subset of benchmark functions which yielded the following equation:

$$k = P/500$$
, where P is the population size. (1)

From the works reviewed here, it is possible to understand that there is a preference to small values for the tournament size. We traced back to 1991, and we found out that it has been a popular choice ever since. We must highlight that these values are usually chosen without much justification.

3 NOISE FREE BENCHMARK BBOB FUNCTIONS

The noise free benchmark BBOB functions [11] are a selected group of functions that are often used to evaluate the performance of evolutionary computation algorithms.

These functions can be separated in two groups by their complexity. The first group is composed on unimodal functions while the second group is composed on multimodal functions. Here we consider that unimodal functions are functions with only one local optimum (equal to the global optimum) while multimodal functions are functions that have many local optimum (with one of them being the global optimum).

The unimodal functions used here are: Sphere Function, Ellipsoidal Function (F2), Linear Slope, Atractive Sector Function, Step Ellipsoidal Function, Rosenbrock Function - original, Rosenbrock Function - rotated, Ellipsoidal Function (F10), Discus Function, Bent Cigar Function, Sharp Ridge Function, and Different Powers Function.

While the multimodal functions used here are: Rastrigin Function (F3), Buche-Rastring Function, Rastring Function (F15), Weierstrass Function, Schaffers F7 Function, Schaffers F7 Function moderately ill-conditioned, Composite Griewank-Rosenbrock Function F8F2, Schwefel Function, Gallagher's Gaussian 101-me Peaks Function, Gallagher's Gaussian 21-hi Peaks Function, Katsuura Function, and Lunacek bi-Rastrigin Function.

4 EXPERIMENT DESIGN

4.1 The Genetic Algorithm

To test the influence of the tournament size we implemented a simple real-valued Genetic Algorithm to explore the search space of the 24 noise free N dimension BBOB benchmark functions [11], while changing the value of the tournament size.

Genome Representation and Evolutionary Tools. Each solution is represented as real valued array, where each element is one input to a N dimension noise free benchmark BBOB function. Therefore, each possible solution of the GA has size of N real value elements. The values of any solution are defined to the be into the interval [-5, 5], since the target functions are bounded by this interval. We considerer two crossover operators when experimenting with the GA: the Uniform crossover and the Simulated Binary crossover (SBX). The other evolutionary operators are elitism and Gaussian mutation. The relevant parameters were set as in the Table 1 and Table 2.

40000
800
0.9
0.1
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Table 1: GA Relevant Parameters

Mean	0
Standard Deviation	1
Ind. Prob. Attribute to be Mutated	0.1

Table 2: Gaussian Mutation parameters

Fitness Function. The fitness function considered are the N dimensions noise free benchmark BBOB functions [11].

Generational Scheme. Two generation schemes were used, the first is named the (λ, λ) , also called the comma version, and the second is named the $(\lambda + \lambda)$, also called the plus version. The (λ, λ) scheme has a λ population of parents and for every generation it creates the λ offspring to compose the next population. The $(\lambda + \lambda)$ scheme creates the λ offspring and the best λ individuals from combined population of offspring and parents are select to the next generation [21].

Code for reproduction of the experiment is available at [anonymous].

4.2 Experiments

We made two experiments aiming to verify the impact of different values for the tournament size. In the first experiment, we analyzed the relation between the tournament size and the performance on the BBOB benchmark functions with 10, 20 and 40 dimensions, when combined with the Uniform crossover or with the SBX, with the generational scheme (λ,λ) . Then, we analyzed the same relation

from before with the same functions and dimensions, but with the generational scheme $(\lambda + \lambda)$ and only the SBX crossover. We consider that the impact the results may be different acknowledged the 2 groups of functions and therefore we analyze the results by grouping all functions together, or the unimodal functions or the multimodal functions.

We used the Friedman Test to determine whether any of the values for the tournament size show a significant difference in the average performance. In each of these tests, we set $\alpha=0.05$. For this analysis, the dependent variable being the average performance, the blocking variable is the BBOB function number and the treatment variable is the tournament size value.

5 RESULTS

Function Group	Dimension size	Chi-squared	P-value
Unimodal	10	24.955	0.2992
Multimodal	10	66.904	2.012e-06
Unimodal	20	20.24	0.5681
Multimodal	20	57.525	5.152e-05
Unimodal	40	25.34	0.2811
Multimodal	40	37.091	0.02312

Table 3: Friedman Test results for Uniform Crossover - (λ, λ) scheme.

Function Group	Dimension size	Chi-squared	P-value
Unimodal	10	53.379	0.0002011
Multimodal	10	81.653	8.645e-09
Unimodal	20	113.02	3.181e-14
Multimodal	20	88.885	5.302e-10
Unimodal	40	163.13	< 2.2e-16
Multimodal	40	118.46	3.316e-15

Table 4: Friedman Test results for SBX Crossover - (λ, λ) scheme.

Function Group	Dimension size	Chi-squared	P-value
Unimodal	10	54.011	0.0001639
Multimodal	10	75.724	8.073e-08
Unimodal	20	73.078	2.15e-07
Multimodal	20	95.524	3.867e-11
Unimodal	40	115.38	1.198e-14
Multimodal	40	87.318	9.762e-10

Table 5: Friedman Test results for SBX Crossover - $(\lambda + \lambda)$ scheme.

5.1 Overall Analysis

The Friedman Test showed no significant difference for the unimodal functions with the uniform crossover and with any dimension. Tough for the multimodal functions with any dimension, the test found significant difference. For example, in Figure 2, it is possible to see that for the Gallagher's Gaussian 21-hi Peaks Function higher values for the tournament size indicate better results.

On all other cases, the Friedman Test showed significant difference in values among tournament size. The results are listed in Tables 3, 4 and 5.

5.2 Functions Analysis

To get a finer intuition about the results, we show some visual examples, separated in two groups of Figures. The first group, shows the mean value achieved by the GA for the Gallagher's Gaussian 21-hi Peaks Function and the second group for the Discus Function (other functions are available as supplemental material). All Figures represent the mean of 40 repetitions given a certain dimension.

The Figures 1 and 2 exemplify that for the Gallagher's Gaussian 21-hi Peaks Function (with 10, 20 and 40 dimensions) changing the tournament size for higher values tend to increase the quality of the results, for the generational scheme (λ, λ) . While for the generational scheme $(\lambda + \lambda)$, the Figure 3 that exemplifies that for the Gallagher's Gaussian 21-hi Peaks Function changing the dimension has a dominating impact on the final values found by the GA. This means that for the same function but with different dimensions the values changing the tournament size may increase or decrease the quality of the results.

The dominance of the dimensionality observed in Figure 3 also occurs in the Discus Function. The Figures 4, 5, (with 10, 20 and 40 dimensions) show changing the dimensionality of the problem may have a high impact in the choice of the tournament value with the generational scheme (λ, λ) . The Figure 6 show that with the generational scheme $(\lambda + \lambda)$ changing the tournament size leads to significant better final values found by the GA. From the Figures we understand that smaller values positively affect the results, specially with low dimensionality.

For all Figures, the gray shaded area represents the 95% confidence level interval of a linear regression model. This demonstrate that sometimes choosing small values for the tournament size, such as 2 or 3 may be a very poor choice. For all Figures, the mean of 40 repetitions is shown as bullets and the red line is shows the objective target value for the function.

5.3 Convergence Analysis

To make sure that the GA formulation under study is converging, we performed a visual examination. Figures 7, 8 and 9 are randomly selected examples namely the Weierstrass Function, the Rosenbrock Function - original, and the Buche-Rastrigin Function. The GA is converging towards the optimum target value, represented by the bottom, red, horizontal line.

Similar Figures for all other combinations are available as supplementary materials.

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6 CONCLUSION

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We proposed an experimental analysis of the impact of the tournament size on the BBOB benchmark functions. We verified that there are few mathematical or experimental studies that supports a choice of value for the tournament size. Usually, the tournament size is chosen to be 2 or 3, based on "previous results".

We analyzed a group of tournament size values on different selection operators. We found in the results that using the tournament size with values like 2 or 3 may not be good choices, depending on the characteristic of the problem you are exploring. We showed evidences that support this affirmative.

Our experiments demonstrated that for every domain of problems, the tournament selection may behave differently according to the "best" choice of the tournament value, with some having more benefit with higher values. Also we realized that for the same problems, the choice of the tournament value may change with different dimensionality as well as with the generational scheme selected to compose the GA.

In conclusion, we suggest that future works consider some sort of self-adaptative procedure should be tried. We believe that using this technique may diminish the time spend on the design process, once it minimizes the impact of bad choice of values for the tournament size by adjusting this parameter on-line during the search process. Also, it would make the GA able to smoothly accommodate any kind of variation, for example, as an increase (decrease) in the size of dimensionality or using different generational schemes as well.

We are aware that our work is limited to few tournament size values. Also, we understand that the other parameters may have some influence in the results. We propose that more investigations need to be done, in order to better understand the role of the tournament size value related to the quality of final results. Also, we would like to explore how much the results were influenced by the particular sets of GA operators studied here.

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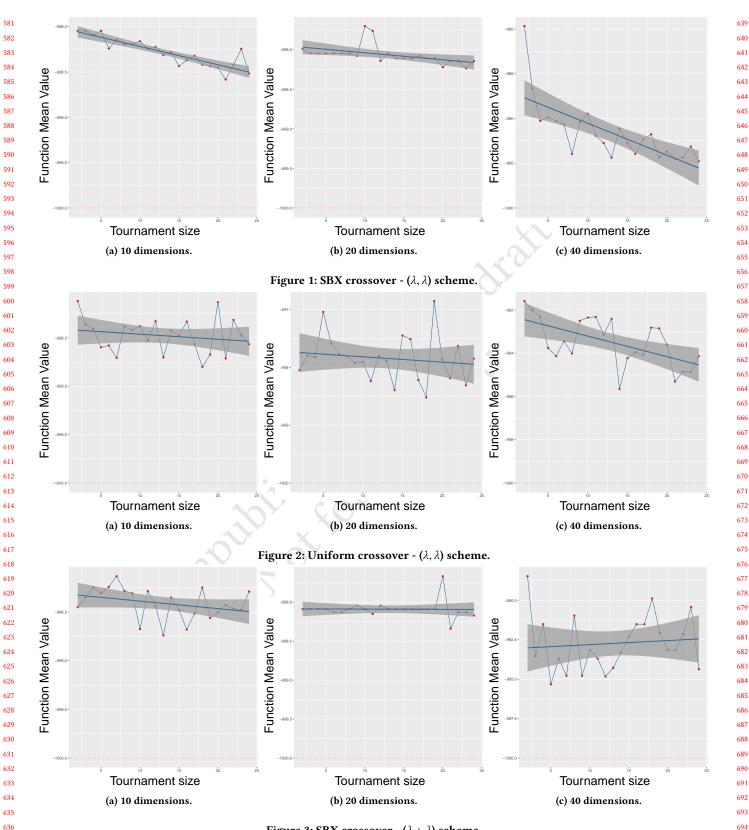


Figure 3: SBX crossover - $(\lambda + \lambda)$ scheme. Average performance on different tournament size - Gallagher's Gaussian 21-hi Peaks Function 2018-02-06 18:16 page 6 (pp. 1-8)

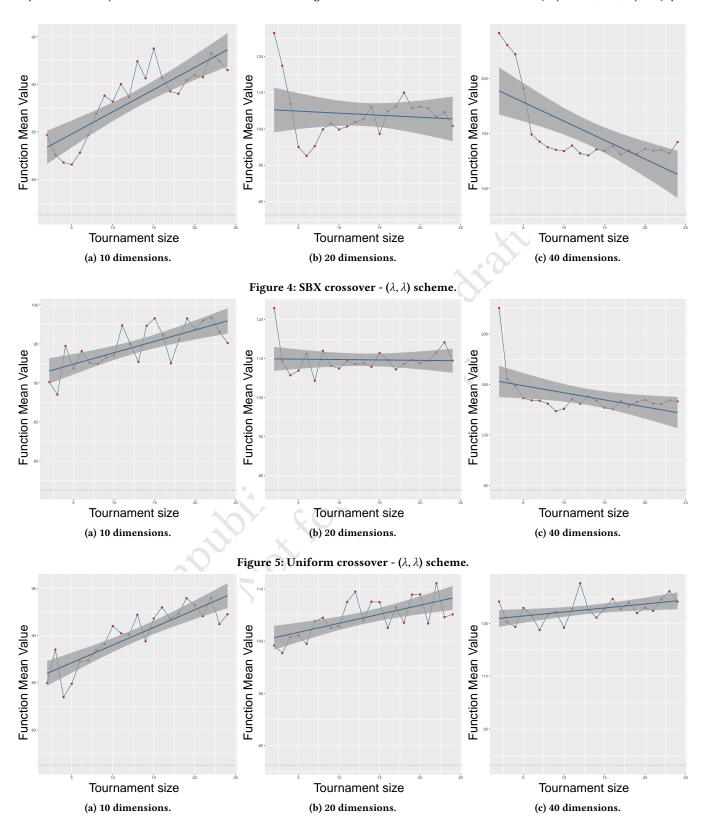


Figure 6: SBX crossover - $(\lambda + \lambda)$ scheme. Average performance on different tournament size - Discus Function

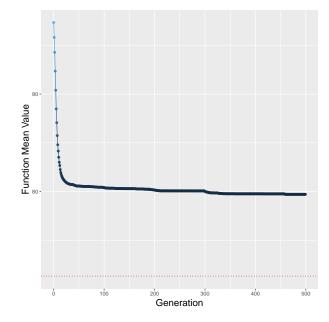


Figure 7: Population convergence for Weierstrass Function with the SBX crossover - $(\lambda + \lambda)$ scheme - 20 dimensions.

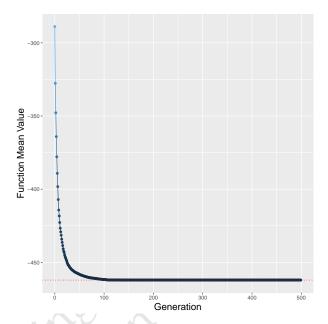


Figure 9: Population convergence for Buche-Rastrigin Function - $(\lambda + \lambda)$ scheme with the SBX crossover - $(\lambda + \lambda)$ scheme.

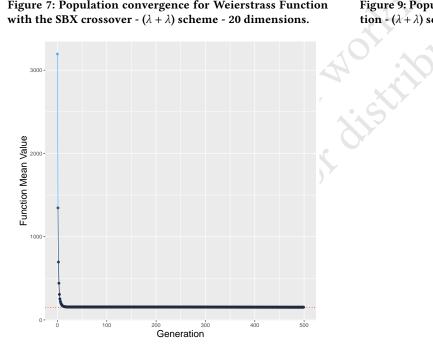


Figure 8: Population convergence for Rosenbrock Function - original with the SBX crossover - (λ, λ) scheme - 10 dimensions.