Option Pricing Prediction Model

Master of Science in Business Analytics, University of Southern California DSO 530: Applied Modern Statistical Learning Methods

Dr. Xin Tong

Hsuan-Ting Wu (3400005886) Liang-Chi Liu (3944052733) Nattawut Kananusorn (5053473152) Suwara Thianrungrot (8623977364) Yi-Ching Lin (7613130093) contact email: lliu4737@usc.edu

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Executive summary

The Nobel Prize winning Black-Scholes formula is a valuable method for evaluating European call options, but could a machine learning model deliver results that are just as good? This project aims to build a supervised learning model that can predict the value of an option and whether the option is worth purchasing. A dataset from S&P 500 contains 1,680 records of stock options and 6 fields, which includes C (current option value), S (current asset value), K (strike price), tau (time to maturity in years), r (annual interest rate) and BS (Over/Under based on whether (result of Black-Scholes formula - C) > 0). To go further in our analysis, we also cleaned the data to ensure the data quality is beyond the standard.

Before building the models, we decided to keep S, K, tau and r as variables since these four variables are all necessary for predicting value and BS in the practical business world. We also standardized these values as another variable group to compare with the non-standardized group to see which sets will have better performance when putting in the models.

Then, we came up with two potential approaches for both regression and classification problems. As for the first approach, we split the dataset into training and testing sets. Next, GridSearchCV was performed with 5-fold cross validation to find the best hyperparameters on 7 regression models and 9 classification models utilizing the training set. After all models were tuned, we compared the out-of-sample R squared in regression models as well as the accuracy on the testing set in classification models as one of the decision factors for choosing the final model. In addition, we also took its stability of cross validation scores in training set into consideration. To sum up, we find out that the performance of standardized variables are more stable than non-standardized variables. Therefore, for the second approach, we decided to use the entire dataset with standardized variables in our models. We conducted GridSearchCV with 10-fold cross validation to find the best hyperparameters on all models and check the out-of-sample R squared in regression models and accuracy scores in classification models. After running these two approaches, we decided to select the second approach to select our final model due to underfitting issues in the first approach.

For our final models, a Gradient Boosting Tree model was selected for the regression problem for its high 99.922% out-of-sample R-squared value. A XGBoost model was selected for the classification problem due to a high accuracy of 94.328%.

In conclusion, the final model can be used to predict the S\$P500 call options value and make a decision whether the option is worth purchasing. Currently, we can find out that our machine learning models might outperform the Black-scholes formula, when predicting values of European call options. This is because the machine learning model is more flexible with the capability of adding more variables and tuning hyperparameters. We can keep track of the model performance and periodically validate the model. However, one thing we need to remind the user is that we cannot use our training models to predict any other stock price because different assets might have different nature shown on the data.

Project Background

A European call option is a type of contract that allows the holder to exercise their option to buy shares at the strike price on the day of its expiration date. For example, an investor purchases a call option of stock X on June 2 with a strike price of \$100 and an expiration date on June 30. These are some possible scenarios on June 30:

- Stock X's price is higher than \$100, the investor can then exercise their option and purchase it with only \$100.
- Stock X's price is lower than \$100, the investor can choose to not exercise their option.

Project Objectives

The objective of this project is to build a supervised learning model that can predict the value of an option and whether the option is worth purchasing.

Our Data Set

The data was provided to us from the S&P 500. It contains 6 variables and 1,680 rows, with each row being an individual option. There are 5 numeric variables, which include C (current option value), S (current asset value), K (strike price), Tau (time to maturity in years) and r (annual interest rate). There is only one categorical variable which is BS (Over/Under based on whether (result of Black-Scholes formula - C) > 0). Detailed fields description can be found in technical appendix Table 1 and 2.

Data Cleaning

After doing some data exploration, we discovered 2 rows with null values (Table 3 in technical appendix). We decided to drop them as the empty fields could have an effect on the model.

We observed a record with a value of 0 in the S field. This is considered an outlier as it is unlikely that a stock will be worth \$0 plus the all other values here are between 375 and 490 (Figure 1 in technical appendix). We decided to drop this row.

Two other outliers were detected in the tau field with values of 146 and 250. Since stock options should not have a maturity time of over 100 years, and all other values here are between 0.0039 and 0.3929 (Figure 2 in technical appendix), we decided to drop these 2 rows.

After dealing with outliers, we convert BS to a binary column:

- If the BS is Under, then it converts to 0.
- If the BS is Over, then it converts 1.

Lastly, we created 5 additional columns by standardizing the variables S, K, r, tau, and value using the StandardScaler library in Python to make sure all variables weigh the same.

In total, we dropped 5 rows and created 5 new variables. The end result was a dataset of 1,675 rows and 11 columns, which will be used for building our models.

Variable Selection

Currently, we have 8 independent variables, which are S, K, r, Tau and their standardized values. We split them into a non-standardized group and a standardized group. We will not perform subset selection within the group since these four variables are all necessary for predicting value and BS. In practice, options traders use the price of the underlying security, time, and volatility to estimate an option's fair value. In terms of the price of the underlying security, it is related to S, K and r. Tau stands for time, which approximates the risk and the uncertainty. In conclusion, we can find that these four variables are actually being used in a real life setting. Therefore, we will use either the non-standardized group or the standardized group with these four variables in our regression and classification models.

Model Selection

We came up with two potential approaches to conduct model selection for both regression and classification problems:

1st Approach (The results are shown in technical appendix Table 6 and 7)

- 1. Set up the random seed as 20, separate the dataset with 80:20 ratio and stratify by y.
- 2. Create a 5-fold CV with KFold/StratifiedKFold and set shuffle = True.
- 3. Use non-standardized variables in the training set and conduct cross validation with 5-fold CV created in step two to find the best hyperparameters for each model utilizing GridSearchCV. Models and corresponding hyperparameters used in GridSearchCV can be found in technical appendix Table 4&5.
- 4. Validate tuned models with testing set and compare
 - (1) Out of sample R squared on the testing set for regression models.
 - (2) Accuracy scores on testing set and the variation of accuracy scores in training set from cross validation for classification models.
- 5. Repeat steps 1 to 4 again with standardized variables and compare the results.

2nd Approach

- 1. Create a 10-fold CV with KFold/StratifiedKFold and set shuffle = True.
- 2. Since we found that standardized variables perform better in terms of stability in the first approach, we only use standardized variables in the whole dataset and conduct cross validation with 10-fold CV created in step two to find the best hyperparameters for each model utilizing GridSearchCV. The models and corresponding hyperparameters used in GridSearchCV are the same as the first approach.
- 3. Compare different models with average out of sample R squared for regression models and average accuracy score for classification models.

Final Approach and Key Result

Final Approach

Eventually, we have selected the second approach to solve these problems. After we trained the model with the first approach, we found that the 5-fold average out-of-sample R-squared and accuracy score on the training set (80% split data) were lower than those on the testing set (20% split data).

split data). This is the underfitting problem when the model is unable to capture the relationship between the input and output variables accurately. In addition, our data set is fixed and extremely small, having only 1,680 rows which might not be large enough to achieve the goal of training and validation data set. For a training data set, the more data we have, the better performance we achieve on the model. For a validation data set, it should be large to be fair and avoid any random errors. Therefore, we have decided to use the whole data set to train the model and achieve these two conditions by using 10-fold cross validation to find the best parameter and the best performance model. However, we kept with the standardized data because we found that it gives the accuracy score on each run (5-fold cross validation) less volatile.

Final Model for Regression

We determined that the final model for regression problem is Gradient Boosting Tree with the following hyperparameters:

Criterion: friedman_mse

max_depth: 4
min_leaf: 1
min_split: 5
n_estinators: 800
learning rate: 0.1

This model performs the best with 99.922% average out-of-sample R-squared. Table 1 below shows the hyperparameters and results of each model for Regression.

Model **Parameters** R2 **Linear Regression** 99.242% Criterion max_depth min_leaf min_split splitter 99.264% **Decision Tree** squared_error None best min_leaf min_split Criterion max_depth n_estimators **Random Forest** 99.651% 200 None mae 1 2 Gradient Criterion max_depth min_leaf min_split n_estimators learning_rate 99.922% **Boosting Tree** friedman_mse 800 0.1 learning rate max_depth n_estimators **XGBoost** 99.916% 0.1 4 800 max_depth n_estimators learning_rate LightGBM 99.570% 200 0.1 -1 activation # of nodes # of layer learning_rate **Neural Network** 99.242% relu 10 2 adaptive

Table 1: Hyperparameters and results of each model for Regression

Final Model for Classification

We determined that the final model for classification problem is XGBoost with the following hyperparameters:

- colsample_bytree: 0.8

- gamma: 1.5

- max_depth: 4

- min_child_weight: 1

- subsample: 0.6

This model performs the best with 94.328% mean accuracy score or 5.672 classification error. Table 2 below shows the hyperparameters and results of each model for Classification.

Table 2: Hyperparameters and results of each model for Classification

Model			Accuracy				
Logistic Bograssian	penalty	solver	С			91.465%	
Logistic Regression	12	newton-cg	0.1			91.405%	
Decision Tree	max_depth	min_leaf	min_split			91.637%	
Decision free	9	1	2			91.03770	
Random Forest	max_depth	min_leaf	min_split	n_estimators		93.669%	
Kandom Forest	9	1	5	150		93.009%	
Gradient Boosting	max_depth	min_leaf	min_split	n_estimators	learning_rate	93.614%	
Tree	5	4	5	100	0.1	93.014%	
XGBoost	colsample_bytree	gamma	max_depth	min_child_weight	subsample	94.328%	
Adboost	0.8	1.5	4	1	0.6	94.320%	
LightGBM	lambda_l1	lambda_l2	max_depth	n_estimators		93.970%	
LightGbivi	0	1	7	100		93.970%	
Neural Network	activation	hidden_layer_sizes	learning_rate			93.489%	
Neural Network	relu	(100, 2)	invscaling			93.489%	
CVAA	kernel	gamma	С			02 2120/	
SVM	rbf	0.1	10			93.312%	
KNN	n_neighbors					02.0729/	
KNN	9					93.072%	

Conclusion and Business Understanding

In conclusion, the predictive model has been built in which we are able to predict a Value and BS of S&P 500 call options for a new data set. Firstly, the data set was explored and cleaned of the missing value and any entries errors. We also converted BS from 'Under' and 'Over' to number '0' and '1', respectively. All variables are standardized before being used to train the model to reduce the difference of their measures. All four variables, S, K, r, Tau, are included in the model due to the nature of call options related to those variables and usually being used in a real life setting. Then, we have tried several approaches and eventually applied the 10-fold cross validation to find the best hyperparameters in several algorithms we used on both regression and classification problems as our final approach. The best model for regression problem is Gradient Boosting Tree, resulting in 99.922% average out-of-sample R-squared while the best model for classification problem is XGBoost, resulting in 94.328% average accuracy score.

There are two issues to be considered after we have built the model to ensure the future use of the model. Firstly, the machine learning model might perform better than the Black-scholes, a concept currently used in the industry, because it is more flexible and adaptable. While the Black-scholes is fixed with some assumptions which are not realistic, the machine learning model can add more dimensions of variables and can tune the hyperparameter to have the model that most reflects reality. Another interesting point is that machine learning models can predict what is the same underlying security on training data. Like our model, it can predict new S&P 500 call options, but cannot predict anything else because different assets might have different nature shown on the data

Technical Appendix

Table 1: Numeric fields description

Variable	Description	Data type	% Populated	Min	Max
Value (C)	Current option value	Float	99%	0.125	60.15
S	Current asset value	Float	99%	0	455.89
K	Strike price of option	Float	99%	375	500
tau	Time to maturity in years	Float	99%	0.0039	250
r	Annual interest rate	Float	100%	0.0295	0.0319

Table 2: Categorical fields description

Variable	Description	Data type	% Populated	Most common value	Unique values
BS	Over/Under based on whether (result of Black-Scholes formula - C) > 0	String	100%	Over	2

Table 3: Data with Missing Values

Index	Value	S	K	tau	r	BS
292	8.625	NaN	NaN	NaN	0.03003	Over
818	NaN	431.2846	NaN	0.230159	0.02972	Over

Figure 1: Distribution of S and K



Figure 2: Box plot of tau

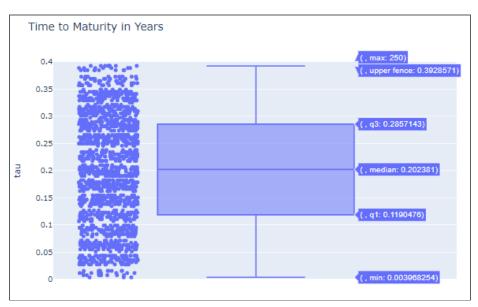


Table 4: Models and hyperparameters applied in GridSearchCV (Regression)

Model	Parameter	Values			
Linear regression	NA	NA			
Random Forest	max_depth	[2, 4, 5, 10, none]			
	min_samples_leaf	[1, 5, 10]			
	min_samples_split	[2, 5, 10, 20]			
	n_estimators	[100, 150, 200]			
	criterion	[mse, mae, poisson]			
Gradient Boosting Classifier	learning_rate	[0.01, 0.1]			
Classifier	max_depth	[2, 4, 5, 10, none]			
	min_samples_leaf	[1, 5, 10]			
	min_samples_split	[2, 5, 10]			
	n_estimators	[100, 150, 200, 500, 800]			
	criterion	[friedman_mse, mse, mae]			
XGBoost	n_estimators	[100, 150, 200, 500, 800]			
	learning_rate	[0.1, 0.01]			
	max_depth	[2, 4, 5, 10, none]			
Neural Network	learning_rate	[constant, invscaling, adaptive]			
	hidden_layer_sizes	[(3,), (5,), (10,), (3,3), (5,5), (10,10)]			
	activation	[logistic, relu, Tanh]			
Decision Tree	max_depth	[2, 4, 5, 10, none]			
	min_samples_leaf	[1, 5, 10]			
	min_samples_split	[2, 5, 10, 20, 50]			
	criterion	[squared_error, friedman_mse, absolute_error, poisson]			
	splitter	[best, random]			
LightGBM	max_depth	[2, 4, 5, 10, -1]			
	n_estimators	[100, 150, 200, 500]			
	learning_rate	[0.1, 0.01]			

Table 5: Models and hyperparameters applied in GridSearchCV (Classification)

Model	Parameter	Values			
Logistic regression	penalty	[11, 12]			
	С	[0.001, 0.01, 0.1, 1, 10, 100, 1000]			
	solver	[newton-cg, lbfgs, liblinear]			
Random Forest	max_depth	[2, 3, 4, 5, 6, 7, 8, 9, 10]			
	min_samples_leaf	[1, 2, 4]			
	min_samples_split	[2, 5, 10]			
	n_estimators	[50, 100, 150, 200]			
Gradient Boosting	learning_rate	[0.001, 0.01, 0.1]			
Classifier	max_depth	[2, 5, 10]			
	min_samples_leaf	[1, 2, 4]			
	min_samples_split	[2, 5, 10]			
	n_estimators	[10, 100]			
SVM	С	[0.1, 1, 10, 100, 1000]			
	gamma	[1, 0.1, 0.01, 0.001, 0.0001]			
	kernel	[rbf]			
XGBoost	min_child_weight	[1, 5, 10]			
	gamma	[0.5, 1, 1.5, 2, 5]			
	subsample	[0.6, 0.8, 1.0]			
	colsample_bytree	[0.6, 0.8, 1.0]			
	max_depth	[3, 4, 5]			
KNN	n_neighbor	[3, 4, 5, 6, 7, 8, 9, 10, 11, 12]			
Neural Network	learning_rate	[constant, invscaling, adaptive]			
	hidden_layer_sizes	[(100,1), (100,2), (100,3)]			
	activation	[logistic, relu, Tanh]			
Decision Tree	max_depth	[2, 3, 4, 5, 6, 7, 8, 9, 10]			

	min_samples_leaf	[1, 2, 4]
	min_samples_split	[2, 5, 10]
LightGBM	max_depth	[2, 3, 4, 5, 6, 7, 8, 9, 10]
	n_estimators	[50, 100, 150, 200]
	lambda_l1	[0, 1, 1.5]
	lambda_12	[0, 1]

Table 6: Hyperparameters and results of each model for Regression in the first Approach

Model	Parameters					R2		
Linear Regression								Test
Linear Regression							91.083%	91.140%
Decision Tree	Criterion	max_depth	min_leaf	min_split	splitter		Train	Test
Decision Tree	absolute_error	18	1	2	random		98.632%	98.859%
Random Forest	Criterion	max_depth	min_leaf	min_split	n_estimators		Train	Test
Kandom Forest	mse	None	1	2	100		99.460%	99.552%
Gradient	Criterion	max_depth	min_leaf	min_split	n_estimators	learning_rate	Train	Test
Boosting Tree	mse	4	1	10	800	0.1	99.874%	99.902%
XGBoost	learning_rate	max_depth	n_estimators				Train	Test
AGBOOST	0.1	4	800				99.858%	99.898%
LightGBM	learning_rate	max_depth	n_estimators				Train	Test
LightGBIVI	0.1	-1	150				99.346%	99.713%
Neural Network	activation	# of nodes	# of layer	learning_rate			Train	Test
Neural Network	relu	10	2	adaptive			99.102%	98.998%

Table 7: Hyperparameters and results of each model for Classification in the first Approach

Model			Accura	су			
Logistic Dograssion	penalty	solver	С			Train	Test
Logistic Regression	12	newton-cg	1			91.493%	91.642%
Desision Tree	max_depth	min_leaf	min_split			Train	Test
Decision Tree	9	2	2			90.746%	92.239%
Dandom Farast	max_depth	min_leaf	min_split	n_estimators		Train	Test
Random Forest	10	2	5	50		92.239%	92.537%
Gradient Boosting	max_depth	min_leaf	min_split	n_estimators	learning_rate	Train	Test
Tree	5	4	2	100	0.1	92.239%	92.537%
XGBoost	colsample_bytree	gamma	max_depth	min_child_weight	subsample	Train	Test
AGBOOST	0.8	1	4	1	0.6	93.284%	93.134%
LightGBM	lambda_l1	lambda_l2	max_depth	n_estimators		Train	Test
LightGbivi	1	1	4	150		92.836%	93.731%
Neural Network	activation	hidden_layer_sizes	learning_rate			Train	Test
Neural Network	relu	(100, 3)	constant			93.209%	93.134%
SVM	kernel	gamma	С			Train	Test
SVIVI	rbf	0.1	100			92.687%	93.433%
KNN	n_neighbors					Train	Test
KININ	9					92.015%	92.537%

Regression

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```
[]: import pandas as pd
     import numpy as np
     import pandas as pd
     from sklearn.preprocessing import StandardScaler
     from sklearn.model_selection import train_test_split
     from sklearn.linear_model import LinearRegression
     from sklearn.tree import DecisionTreeRegressor
     from sklearn.ensemble import RandomForestClassifier
     from sklearn.ensemble import RandomForestRegressor
     from sklearn.ensemble import GradientBoostingRegressor
     from xgboost import XGBRegressor
     from sklearn.neural network import MLPRegressor
     from sklearn.neighbors import KNeighborsClassifier
     from sklearn.model selection import cross val score
     from lightgbm import LGBMRegressor
     import matplotlib.pyplot as plt
     from sklearn.model_selection import KFold, StratifiedKFold
     from sklearn.model_selection import GridSearchCV
     import lightgbm as lgb
     import seaborn as sns
     from sklearn import tree
     import lightgbm as lgb
     from xgboost import XGBClassifier
     from sklearn.linear_model import LogisticRegression
     from sklearn.naive_bayes import GaussianNB, MultinomialNB, BernoulliNB
     from sklearn.tree import DecisionTreeClassifier
     from sklearn.ensemble import GradientBoostingClassifier
     from sklearn.svm import SVC
     from sklearn.ensemble import VotingClassifier
     from sklearn.metrics import accuracy_score, precision_score, recall_score,
     →f1_score, confusion_matrix, classification_report, mean_squared_error, __
     ⊸r2 score
     from sklearn.utils import class_weight
     from sklearn.neural_network import MLPClassifier
     import warnings
     warnings.filterwarnings("ignore")
```

1 Import data

```
[]: data = pd.read_csv('option_train.csv')
[]: data.head()

Encode BS column - 1 is Over, 0 is Under
[]: data['BS_encode'] = [1 if i == 'Over' else 0 for i in data['BS']]
[]: data.shape
```

2 Data filtering

2.1 Drop 2 records that has null values

```
[]: data.dropna(axis=0, inplace = True)
```

2.2 Drop 3 outliers

```
[]: data.describe()
[]: data.sort_values(by = 'tau', ascending = False)
[]: data.sort_values(by = 'S', ascending = True)
[]: data.drop([12,33,879], inplace = True)
```

3 Z-Scaling before building the models

```
[]: stdx = StandardScaler()
    stdy = StandardScaler()
    X = data[['S','K','tau','r']]
    y_value = data['Value']
    y_BS = data['BS_encode']
    X_z = stdx.fit_transform(data[['S','K','tau','r']])
    y_z = (stdy.fit_transform(data[['Value']])).reshape(-1)
[]: print(X_z.shape)
    print(y_z.shape)
    print(y_BS.shape)
```

4 Method 1

4.1 Regression Models

```
[]: X_train, X_test, y_train, y_test = train_test_split(X_z, y_z, test_size = .2, □ → random_state = 20)
```

4.1.1 Linear Regression

There is no hyperparameter that can be tuned to improve the r2

```
[]: kf5 = KFold(n_splits = 5, shuffle = True)

LR = LinearRegression()
    cv = cross_val_score(LR, X_train, y_train, cv = kf5)
    print(cv, 'mean: ', cv.mean())

LR.fit(X_train, y_train)
    y_pred = LR.predict(X_test)
    print(LR.score(X_test, y_test))
    print(mean_squared_error(y_test, y_pred))
```

4.1.2 Decision Tree

4.1.3 Random Forest

```
[]: kf5 = KFold(n splits = 5, shuffle = True)
     RF_param = {'n_estimators' : [10, 50, 100, 150, 200],
                 'criterion': ['mse', 'mae', 'poisson'],
                  'max_depth': list(range(2,11,2))+[None],
                  'min_samples_split' : [2,5,10,20],
                  'min_samples_leaf' : [1,5,10]}
     RF = RandomForestRegressor()
     RF_cv = GridSearchCV(RF, RF_param, cv = kf5, refit=True, verbose=3)
     RF_cv.fit(X_train, y_train)
     print(RF_cv.best_score_)
     print(RF_cv.best_params_)
[]: RF = RandomForestRegressor(criterion = 'mse', max_depth = None,
     min_samples_leaf = 1, min_samples_split = 2, n_estimators = 100)
     cv = cross_val_score(RF, X_train, y_train, cv = kf5)
     print(cv, 'mean: ', cv.mean())
     RF.fit(X_train, y_train)
     y_pred = RF.predict(X_test)
     print(RF.score(X_test, y_test))
     print(mean_squared_error(y_test, y_pred))
```

4.1.4 Gradient Boosting Tree

```
[]: GB = GradientBoostingRegressor(criterion = 'mse', learning_rate = 0.1, u → max_depth = 4, min_samples_leaf = 1, min_samples_split = 10, n_estimators = 0.800)

cv = cross_val_score(GB, X_train, y_train, cv = kf5)

print(cv, 'mean: ', cv.mean())
```

```
GB.fit(X_train, y_train)
y_pred = GB.predict(X_test)
print(GB.score(X_test, y_test))
print(mean_squared_error(y_test, y_pred))
```

4.1.5 Xgboost

```
[]: XG = XGBRegressor(learning_rate = 0.1, max_depth = 4, n_estimators = 800)
    cv = cross_val_score(XG, X_train, y_train, cv = kf5)
    print(cv, 'mean: ', cv.mean())

XG.fit(X_train, y_train)
    y_pred = XG.predict(X_test)
    print(XG.score(X_test, y_test))
    print(mean_squared_error(y_test, y_pred))
```

4.1.6 LGB

```
[]: LG = LGBMRegressor(learning_rate = 0.1, max_depth = -1, n_estimators = 150)
    cv = cross_val_score(LG, X_train, y_train, cv = kf5)
    print(cv, 'mean: ', cv.mean())

LG.fit(X_train, y_train)
    y_pred = LG.predict(X_test)
```

```
print(LG.score(X_test, y_test))
print(mean_squared_error(y_test, y_pred))
```

4.1.7 Neural Network

4.1.8 Summary Result

```
[]: r2 = []
mse = []
```

```
for regression in regressions:
    regression.fit(X_train, y_train)
    y_pred = regression.predict(X_test)
    r2.append(r2_score(y_test, y_pred))
    mse.append(mean_squared_error(y_test, y_pred))
```

```
[]: models = pd.DataFrame({'Model': ['Linear Regression','Decision Tree', 'Random

→Forest',

'Gradient Boosting Tree', 'Xgboost', 'LGB',

→'Neural Network'],

'r2':r2,

'mse':mse})

models.sort_values(by='r2', ascending=False)
```

5 Method 2

5.1 Regression Models

5.1.1 Linear Model

```
[]: kf10 = KFold(n_splits = 10, shuffle = True)

LR = LinearRegression()
cv = cross_val_score(LR, X_z, y_z, cv = kf10)
LR_r2 = cv.mean()
print(cv, 'mean: ', cv.mean())
```

5.1.2 Decision Tree

5.1.3 Random Forest

5.1.4 Gradient Boosting Tree

5.1.5 XGBoost

```
print(XG_cv.best_score_)
print(XG_cv.best_params_)
```

5.1.6 LGB

5.1.7 Neural Network

5.1.8 Summary Result

```
[]: models = pd.DataFrame({'Model': ['Linear Regression','Decision Tree', 'Random_
→Forest',

'Gradient Boosting Tree', 'Xgboost', 'LGB',
→'Neural Network'],

'parm': ['', DT_best_parm, RF_best_parm, GB_best_parm,
→XG_best_parm, LG_best_parm, NN_best_parm],

'r2': [LR_r2, DT_r2, RF_r2, GB_r2, XG_r2, LG_r2, NN_r2]})

models.sort_values(by='r2', ascending=False).reset_index(drop = True)
```

6 Predict Test data

```
[]: GB_best_parm
[]: test_data = pd.read_csv('option_test_wolabel.csv')
[]: test_data.head()
    Scale test data
[]: X_test_scale = stdx.transform(test_data)
    Train the model with the best parameter and all training data set
[]: GB_use = GradientBoostingRegressor(
         criterion = 'friedman_mse',
         learning_rate = 0.1,
         max_depth = 4,
         min_samples_leaf = 1,
         min_samples_split = 5,
         n_estimators = 800)
     GB_use.fit(X_z,y_z)
     y_pred_z = GB_use.predict(X_test_scale)
[]: y_pred_z
    Transform value back to unscaled data
[]: y_pred = stdy.inverse_transform(y_pred_z.reshape(-1,1))
[]: test_data['value'] = y_pred
[]: test_data
[]: test_data.to_csv('test_data_pred.csv')
```

Classification

 $\mathrm{May}\ 5,\ 2022$

[]: import pandas as pd

```
import numpy as np
     import matplotlib.pyplot as plt
     import seaborn as sns
[]: # read data
     df = pd.read_csv('option_train.csv')
     df.head()
[]: df.groupby('BS')['S'].count()
    1 Data Cleaning
[]: df.isnull().sum()
[]: # change BS to dummy
    df['BS'] = [1 if i == 'Over' else 0 for i in df['BS']]
     df.head()
[]: df.shape
[]: # drop the row with null values
     df = df.dropna(axis=0)
     df.shape
[]: # remove outliers
     df = df[df['tau'] != 250]
     df = df[df['tau'] != 146]
     df = df[df['S']] != 0
     df.shape
```

2 Version 1

3 Preprocessing

4 Test Models

```
[]: from sklearn.model_selection import cross_val_score, KFold ## for regression from sklearn.model_selection import StratifiedKFold ## recommended for → classification
```

4.0.1 Logistic Regression

```
[]: kf5 = StratifiedKFold(n splits = 5, shuffle = True)
     log_param = {'penalty' : ['11','12'],
                  'C': np.logspace(-3,3,7),
                  'solver' : ['newton-cg', 'lbfgs', 'liblinear']}
     log = LogisticRegression()
     log_cv = GridSearchCV(log, log_param, cv = kf5, refit=True, verbose=3)
     log_cv.fit(X_train, y_train)
     print(log_cv.best_score_)
     print(log_cv.best_params_)
[]: log = LogisticRegression(C = 10, penalty = 'l1', solver= 'liblinear')
     cv = cross_val_score(log, X_train, y_train, cv = kf5)
     print(cv, 'mean: ', cv.mean())
     log.fit(X_train, y_train)
     y_pred = log.predict(X_test)
     print(confusion_matrix(y_test, y_pred))
     print(classification_report(y_test, y_pred))
     print(log.score(X_test, y_test))
```

4.0.2 Random Forest

```
print(classification_report(y_test, y_pred))
print(rf.score(X_test, y_test))
```

4.0.3 Gradient Boosting

```
[]: kf5 = StratifiedKFold(n_splits = 5, shuffle = True)
   gb_param = {
      "learning_rate": [0.001, 0.01, 0.1],
      'max_depth': [2, 5, 10],
      'min_samples_leaf': [1, 2, 4],
      'min_samples_split': [2, 5, 10],
      "n_estimators": [10, 100]
   }

gb = GradientBoostingClassifier()
   gb_cv = GridSearchCV(gb, gb_param, cv=kf5, refit=True, verbose=3)
   gb_cv.fit(X_train, y_train)
   print(gb_cv.best_score_)
   print(gb_cv.best_params_)
```

4.0.4 SVM

```
[]: svm = SVC(C=1000, gamma=0.001, kernel='rbf')
cv = cross_val_score(svm, X_train, y_train, cv = kf5)
print(cv, 'mean: ', cv.mean())

svm.fit(X_train, y_train)
y_pred = svm.predict(X_test)
print(confusion_matrix(y_test, y_pred))
print(classification_report(y_test, y_pred))
print(svm.score(X_test, y_test))
```

4.0.5 Xgboost

4.0.6 KNN

```
[]: kf5 = StratifiedKFold(n_splits = 5, shuffle = True)
knn_param = {'n_neighbors': [3, 4, 5, 6, 7, 8, 9, 10, 11, 12]}
knn = KNeighborsClassifier()
knn_cv = GridSearchCV(knn, knn_param, cv=kf5, refit=True, verbose=3)
```

```
knn_cv.fit(X_train, y_train)
print(knn_cv.best_score_)
print(knn_cv.best_params_)
```

```
[]: knn = KNeighborsClassifier(n_neighbors = 7)
    cv = cross_val_score(knn, X_train, y_train, cv = kf5)
    print(cv, 'mean: ', cv.mean())

knn.fit(X_train, y_train)
    y_pred = knn.predict(X_test)
    print(confusion_matrix(y_test, y_pred))
    print(classification_report(y_test, y_pred))
    print(knn.score(X_test, y_test))
```

4.0.7 Neural Network

4.0.8 Decision Tree

```
dt_cv.fit(X_train, y_train)
print(dt_cv.best_score_)
print(dt_cv.best_params_)
```

4.0.9 LGB

```
[]: classifiers = [LogisticRegression(C = 10, penalty = 'l1', solver= 'liblinear'),

KNeighborsClassifier(n_neighbors=7),

SVC(C=1000, gamma=0.001, kernel='rbf'),

DecisionTreeClassifier(max_depth=9, min_samples_leaf=1, u

→min_samples_split=2),
```

```
RandomForestClassifier(max_depth=9, min_samples_leaf=2,_u

imin_samples_split=5, n_estimators=200),

GradientBoostingClassifier(learning_rate=0.1, max_depth=5,_u

imin_samples_leaf=2,

min_samples_split=2,_u

imin_samples_split=2,_u

imin_samples
```

```
[]: acc = []
pre = []
rec = []
f1 = []

for classifier in classifiers:
    classifier.fit(X_train, y_train)
    y_pred = classifier.predict(X_test)
    acc.append(accuracy_score(y_test, y_pred))
    pre.append(precision_score(y_test, y_pred, average='weighted'))
    rec.append(recall_score(y_test, y_pred, average='weighted'))
    f1.append(f1_score(y_test, y_pred, average='weighted'))
```

```
[]: models = pd.DataFrame({'Model': ['Logistic Regression','KNN', 'SVM', 'Decision_

→Tree', 'Random Forest',

'Gradient Boosting','Neural

→Network','Xgboost', 'LGB'],

'Accuracy':acc,

'Precision':pre,

'Recall':rec,

'F1':f1})

models.sort_values(by='Accuracy', ascending=False)
```

5 Standardize (Use scaled_X_train)

5.0.1 Final

```
RandomForestClassifier(max_depth=10, min_samples_leaf=2,__

→min_samples_split=5, n_estimators=50),
                    GradientBoostingClassifier(learning_rate=0.1, max_depth=5,__

→min_samples_leaf=4,
                                               min_samples_split=2,_
     \rightarrown_estimators=100),
                    MLPClassifier(activation='relu', hidden_layer_sizes=(100, 3),
      →learning_rate='constant'),
                    XGBClassifier(colsample_bytree=0.8, gamma=1, max_depth=4,__
      →min_child_weight=1, subsample=0.6),
                    lgb.LGBMClassifier(lambda_11=1, lambda_12=1, max_depth=4,__
      []: acc = []
     pre = []
     rec = []
     f1 = []
     for classifier in classifiers:
         classifier.fit(scaled_X_train, y_train)
        y_pred = classifier.predict(scaled_X_test)
        acc.append(accuracy_score(y_test, y_pred))
        pre.append(precision_score(y_test, y_pred, average='weighted'))
        rec.append(recall_score(y_test, y_pred, average='weighted'))
        f1.append(f1_score(y_test, y_pred, average='weighted'))
[]: models = pd.DataFrame({'Model': ['Logistic Regression', 'KNN', 'SVM', 'Decision_
     →Tree', 'Random Forest',
                                      'Gradient Boosting','Neural⊔
     →Network','Xgboost', 'LGB'],
                            'Accuracy':acc,
                            'Precision':pre,
                            'Recall':rec,
                            'F1':f1})
```

6 Version 2

models.sort_values(by='Accuracy', ascending=False)

```
[]: from sklearn.preprocessing import StandardScaler

X = df.loc[:, ['S', 'K', 'tau', 'r']]
y = df.loc[:, 'BS']

scaler = StandardScaler()
scaled_X = scaler.fit_transform(X)
print(scaled_X.shape)
```

```
[]: from sklearn.model_selection import cross_val_score, KFold ## for regression
     from sklearn.model_selection import StratifiedKFold ## recommended for_
     \rightarrow classification
     # importing the modules
     import lightgbm as lgb
     from xgboost import XGBClassifier
     from sklearn.model selection import cross val score, cross validate,
     →GridSearchCV
     from sklearn.linear_model import LogisticRegression
     from sklearn.neighbors import KNeighborsClassifier
     from sklearn.naive_bayes import GaussianNB, MultinomialNB, BernoulliNB
     from sklearn.tree import DecisionTreeClassifier
     from sklearn.svm import SVC
     from sklearn.ensemble import RandomForestClassifier, GradientBoostingClassifier
     from sklearn.metrics import accuracy_score, precision_score, recall_score,
     →f1_score, confusion_matrix, classification_report
     from sklearn.utils import class_weight
     from sklearn.neural_network import MLPClassifier
```

6.0.1 Logistic Regression

6.0.2 Random Forest

6.0.3 Gradient Boosting

```
kf10 = StratifiedKFold(n_splits = 10, shuffle = True)
gb_param = {
    "learning_rate": [0.001, 0.01, 0.1],
    'max_depth': [2, 5, 10],
    'min_samples_leaf': [1, 2, 4],
    'min_samples_split': [2, 5, 10],
    "n_estimators": [10, 100]
    }

gb = GradientBoostingClassifier()
gb_cv = GridSearchCV(gb, gb_param, cv=kf10, refit=True, verbose=3)
gb_cv.fit(scaled_X, y)
print(gb_cv.best_score_)
print(gb_cv.best_params_)
```

6.0.4 SVM

6.0.5 Xgboost

6.0.6 KNN

```
[]: kf10 = StratifiedKFold(n_splits = 10, shuffle = True)
knn_param = {'n_neighbors': [3, 4, 5, 6, 7, 8, 9, 10, 11, 12]}

knn = KNeighborsClassifier()
knn_cv = GridSearchCV(knn, knn_param, cv=kf10, refit=True, verbose=3)
knn_cv.fit(scaled_X, y)
print(knn_cv.best_score_)
print(knn_cv.best_params_)
```

6.0.7 Neural Network

6.0.8 Decision Tree

6.0.9 LGB

7 Final model: XGBoost in version 2