

Note: In questions where you are asked about a static method, assume that the method is in a class called `Qn` where n is the question number, e.g., `Q1` for Question 1.

Question 1. [10 points] Consider the following code:

```
int count = 0;
for (int i = 0; i < n*n; i++) { —  $N^2$  times
    count++;  $O(1)$ 
}
for (int j = 0; j < n; j++) { —  $N$  times
    count++;  $O(1)$ 
}
```

low order term dropped
 $N^2 \cdot O(1) + N \cdot O(1)$
 is
 $O(N^2)$

State a big-O upper bound on the running time of this code, using n (the value of the variable n) as the problem size. Briefly explain your answer.

Question 2. [10 points] Consider the following code:

```
int count = 0;
for (int i = 0; i < n; i++) { —  $n$  times
    for (int j = 0; j < i/2; j++) { — average # of iterations is  $n/4$ 
        count++;  $O(1)$ 
    }
}
```

State a big-O upper bound on the running time of this code, using n (the value of the variable n) as the problem size. Briefly explain your answer.

$n \cdot \frac{n}{4} \cdot O(1)$ is $O(n^2)$

Question 3. [10 points] Consider the following method:

```
public static<E> void removeEveryOther(List<E> list) {  
    Iterator<E> i = list.iterator();  
    int count = 0;  
    while (i.hasNext()) {  $\leftarrow N$  times  
        i.next();  $\leftarrow O(1)$   
        if (count % 2 == 1) {  $\leftarrow$  executes for every other element  
            i.remove();  $O(1)$  for linked list,  
        }  $O(N)$  for Array List  
        count++;  $\leftarrow O(1)$   
    }  
}
```

Note that an Iterator's remove method removes from the collection the last element returned by the Iterator's next method.

(a) State a big-O upper bound on the running time of this method if list is an ArrayList. Consider the problem size N to be the number of list elements. Explain briefly.

Iterator Remove() takes time proportional to the number of elements that must be shifted, which is

$(N-2), (N-4), (N-6), \dots, 2, 0$
the sum of this series is $O(N^2)$,
so the overall running time is $O(N^2)$

(b) State a big-O upper bound on the running time of this method if list is a LinkedList. Consider the problem size N to be the number of list elements. Explain briefly.

Iterator remove() is always $O(1)$ for a Linked List, so $O(N)$ overall