

Question 1. [25 points] State a big-O upper bound on the running time of the following method, where the problem size N is the number of elements in the array passed as the method's parameter. Explain your answer briefly.

$N = \text{arr.length}$

```

public static int q1(int[] arr) {
    int sum = 0;
    for (int i = 0; i < arr.length; i++) { —  $N$  times
        for (int j = 0; j < arr.length; j++) { —  $N$  times
            sum += (arr[i] * arr[j]); —  $O(1)$ 
        }
    }
    return sum;
}

```

$$N \cdot N \cdot O(1) \quad \text{is} \quad O(N^2)$$

Question 2. [25 points] State a big-O upper bound on the running time of the following method, where the problem size N is the number of elements in the array passed as the method's parameter. Explain your answer briefly.

$N = \text{arr.length}$

```

public static int q2(int[] arr) {
    int sum = 0;
    for (int i = 0; i < arr.length; i++) { —
        int max = arr.length;
        if (max > 10000) {
            max = 10000;
        }
        for (int j = 0; j < max; j++) { —  $O(1)$ 
            sum += (arr[i] * arr[j]); —  $O(1)$ 
        }
    }
    return sum;
}

```

} max is at most 10,000, thus $O(1)$

$$N \cdot O(1) \cdot O(1) \quad \text{is} \quad O(N)$$

Question 3. [25 points] State a big-O upper bound on the running time of the following method, where the problem size N is the number of elements in the `ArrayList` passed as the method's parameter. Explain your answer briefly.

```

public static int q3(ArrayList<Integer> arr) {
    int sum = 0;
    for (int i = 0; i < arr.size(); i++) {
        sum += arr.get(i);
    }
    return sum;
}

```

$N = \text{arr.size}()$

$\text{size}() \rightarrow N$ times

$\text{get}(i) \rightarrow O(1)$

$$N \cdot O(1) \text{ is } O(N)$$

Question 4. [25 points] State a big-O upper bound on the running time of the following method, where the problem size N is the number of elements in the `LinkedList` passed as the method's parameter. Explain your answer briefly.

```

public static int q4(LinkedList<Integer> arr) {
    int sum = 0;
    for (int i = 0; i < arr.size(); i++) {
        sum += arr.get(i);
    }
    return sum;
}

```

$N = \text{arr.size}()$

$\text{size}() \rightarrow O(1)$

$\text{get}(i) \rightarrow N$ times

time is proportional to number of elements that must be skipped to reach the element at index i — average is $N/2$

$$N \cdot N/2 \cdot O(1) \text{ is } O(N^2)$$