

CS350: Data Structures

Trees / Binary Trees

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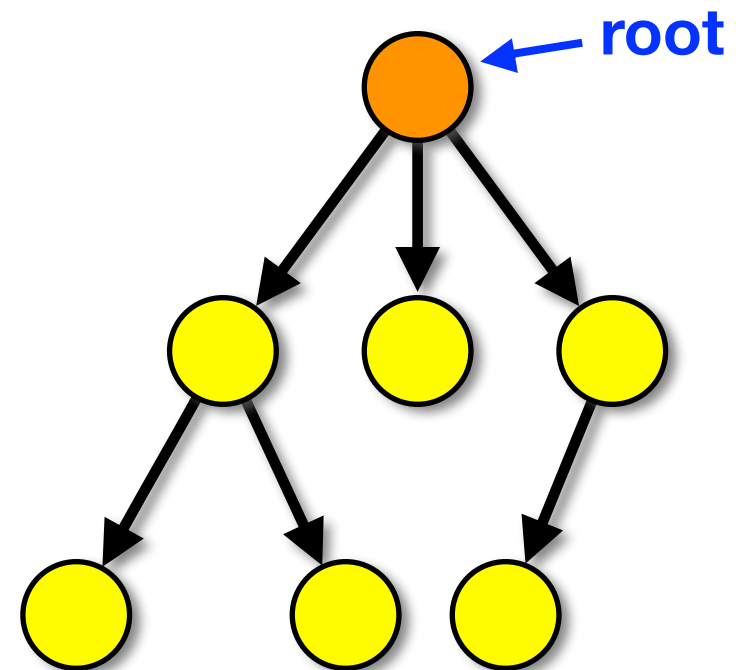
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Trees

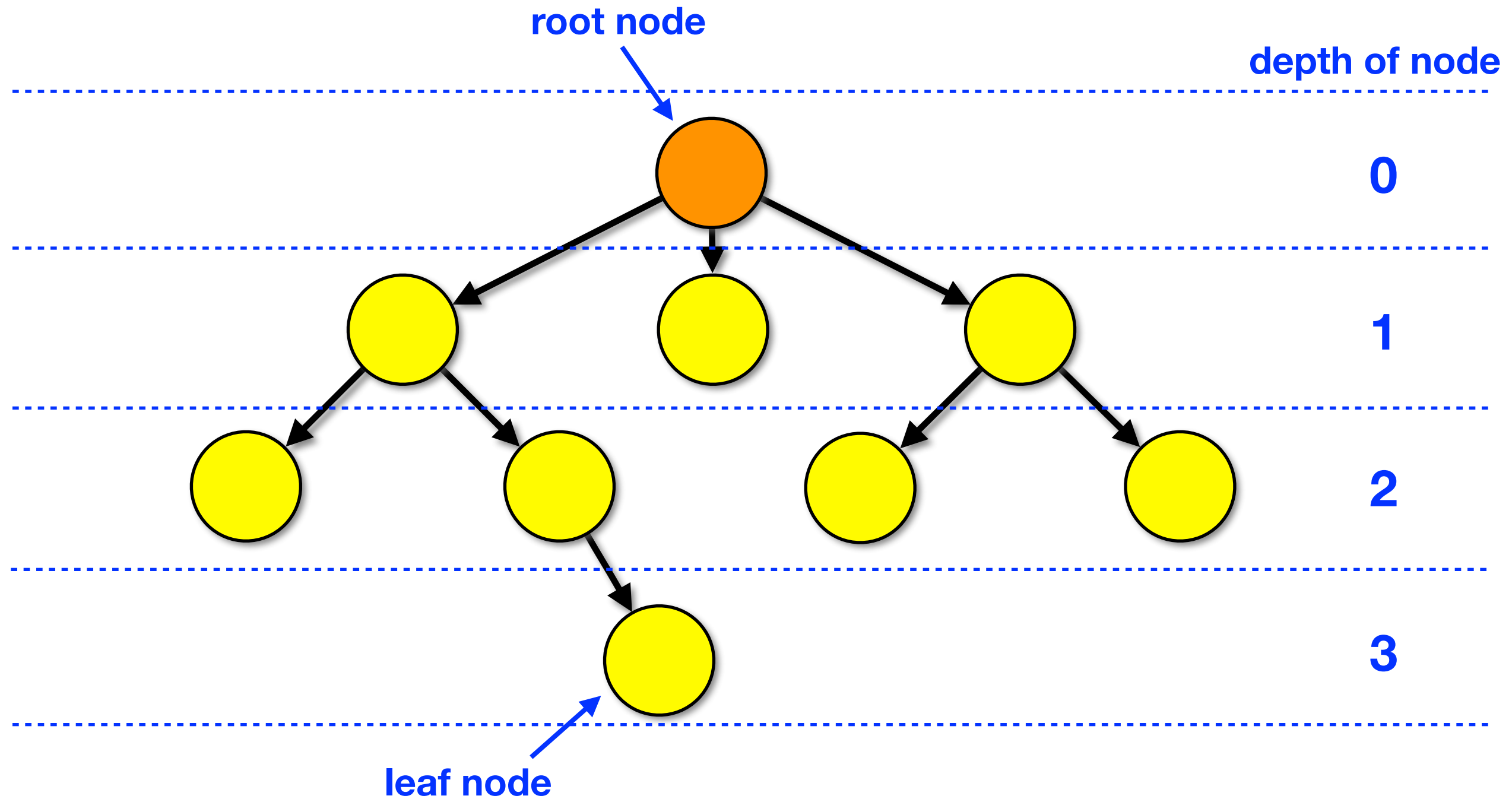
- A **tree** consists of a set of nodes and a set of directed edges that connect pairs of nodes
- A tree has the following properties:
 - A single node that is distinguished as the **root**
 - Every node c , except the root, has a single incoming edge from one other node p
 - p is the **parent** of c
 - c is the **child** of p
 - A single path exists from the root to each node in the tree (no cycles in the tree)
 - A **tree node** has zero or more subtrees
 - Subtrees may be empty



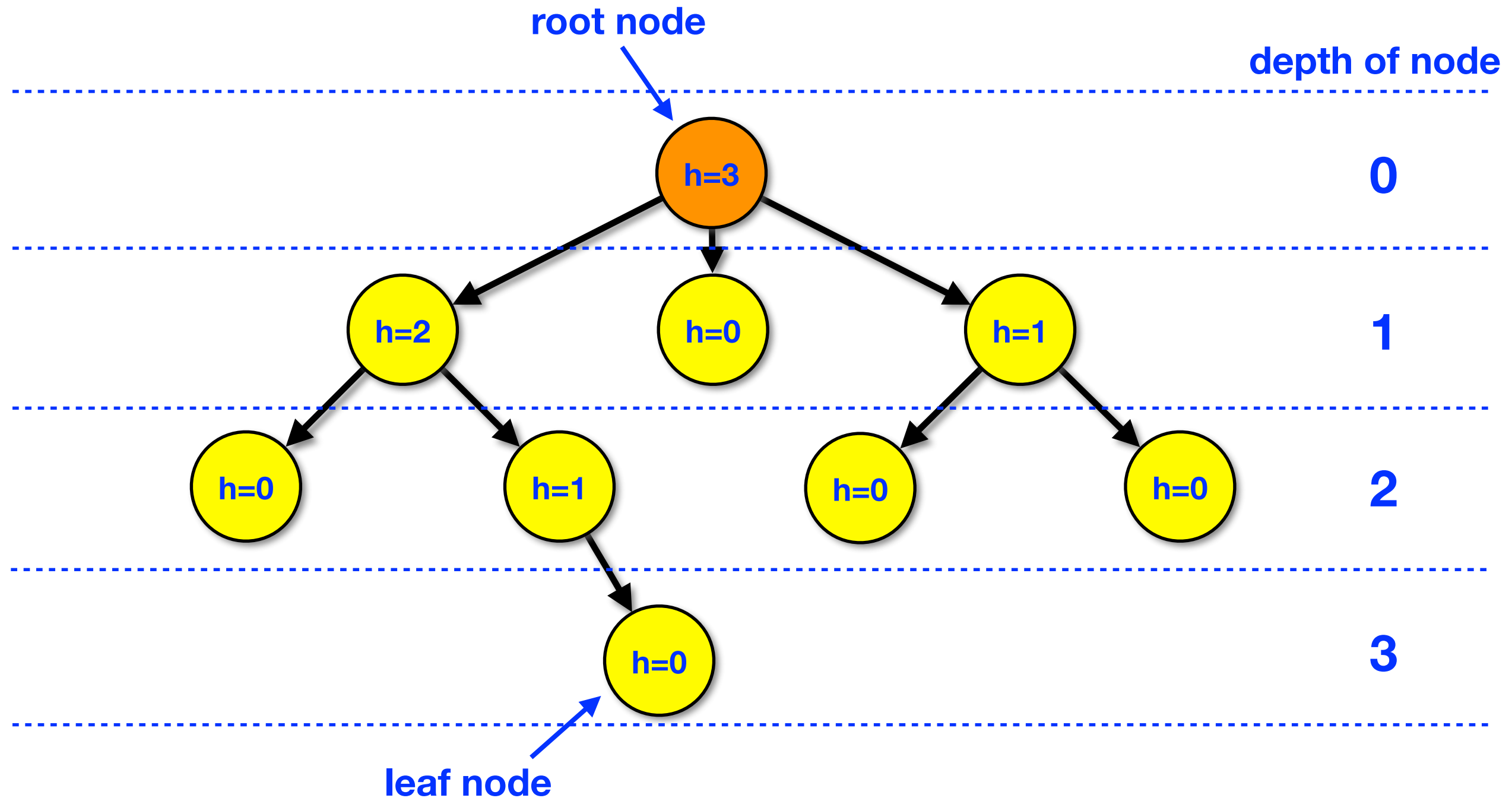
Tree Properties

- **A tree with N nodes must have $N-1$ edges**
 - Every node, except the root node, has one incoming edge
- **The **depth** of a node in a tree is the length of the path from the root to the node**
 - The depth of the root is always 0
- **The **height** of a node in a tree is length of the path from the node to the deepest leaf**
 - The height of the tree is the height of the root node
- **A node that has no children is called a **leaf node****
- **A '**arity**' of a node is the maximum number of children the node can have**

Tree Properties

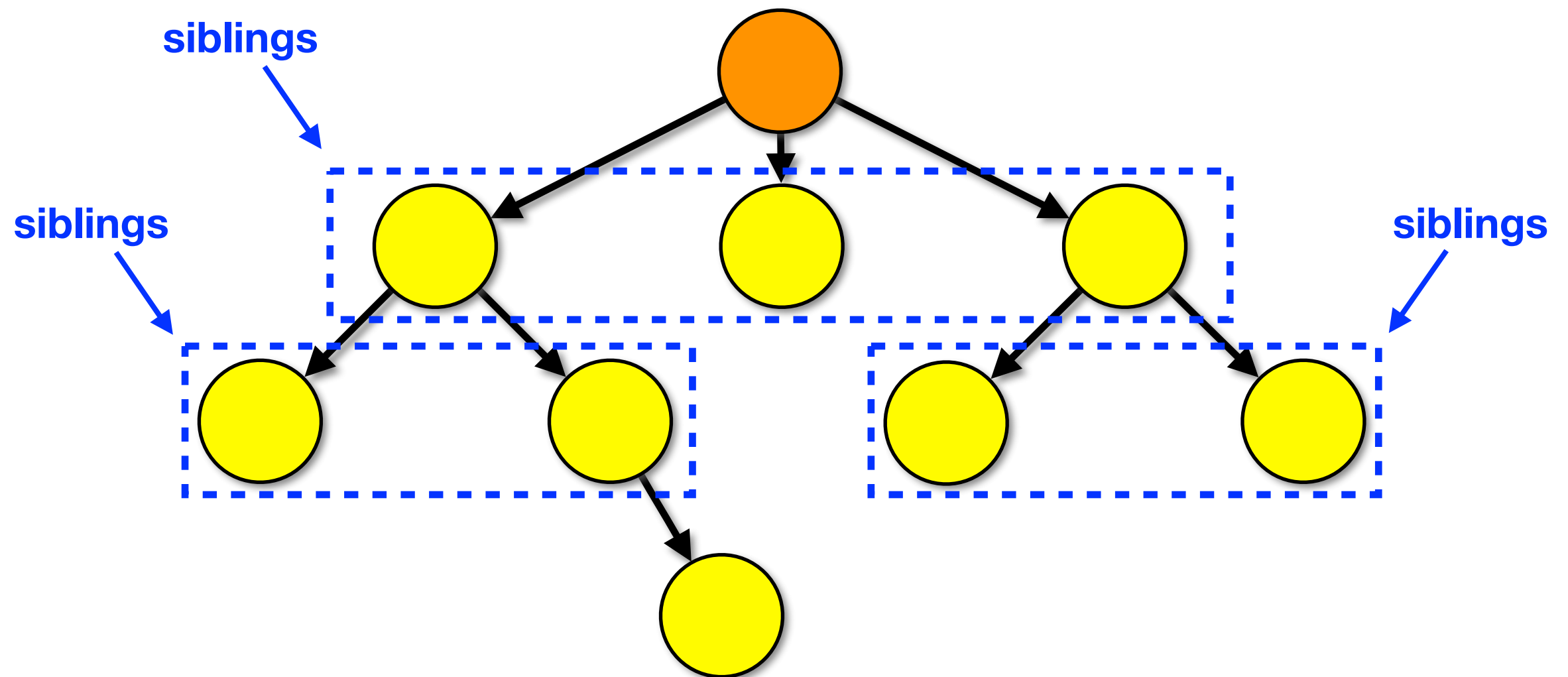


Tree Properties (Each Node Showing Its Height)



Tree Properties (Siblings)

All children of a single node are siblings



Tree Properties (Ancestors)

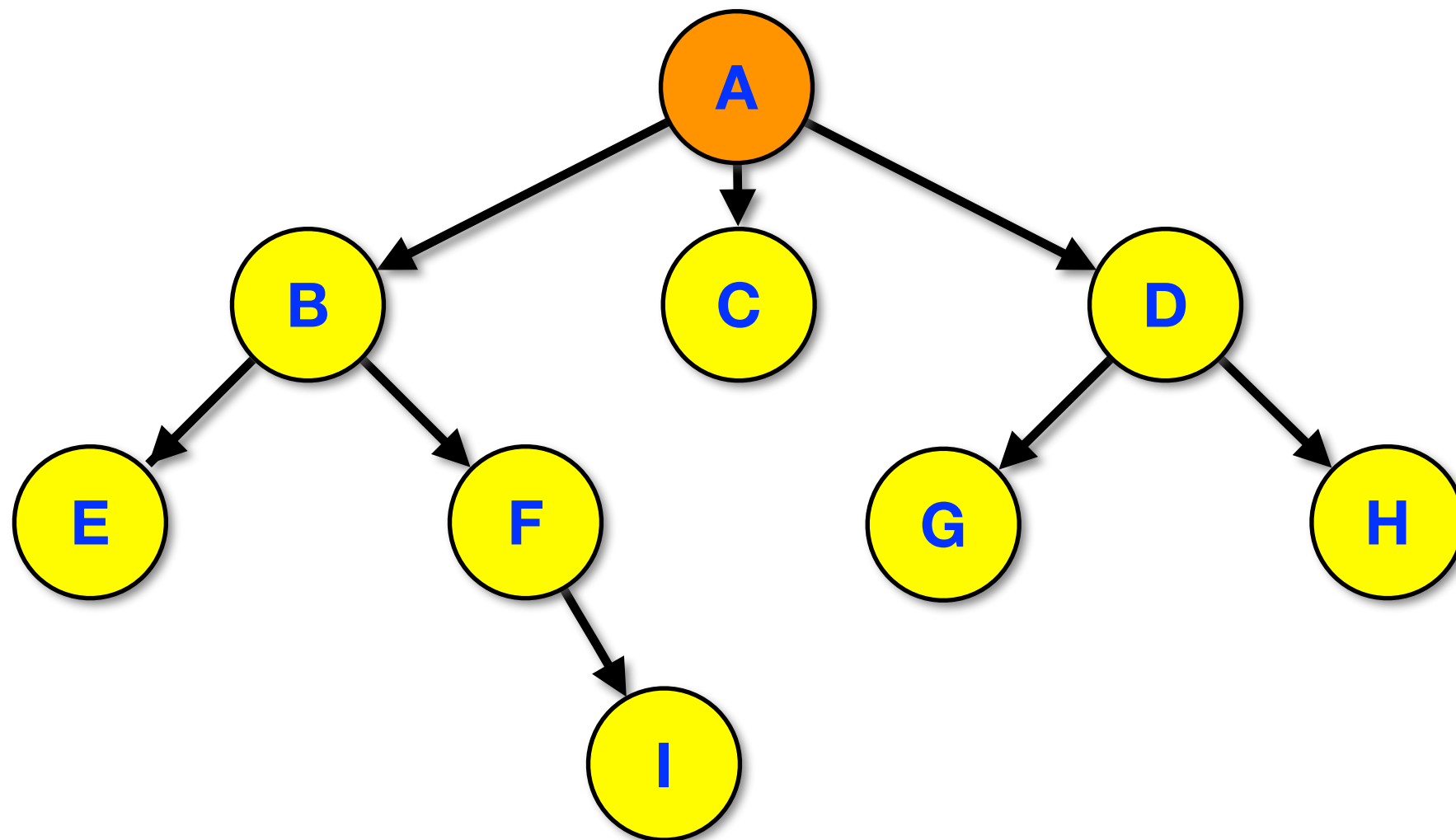
The node E has two **ancestors**: B, A

The node C has one **ancestor**: A

The node I has three **ancestors**: F, B, A

The root node is an ancestor to all other nodes

p is an ancestor of q iff there exists a path from p to q



Tree Properties (Descendants)

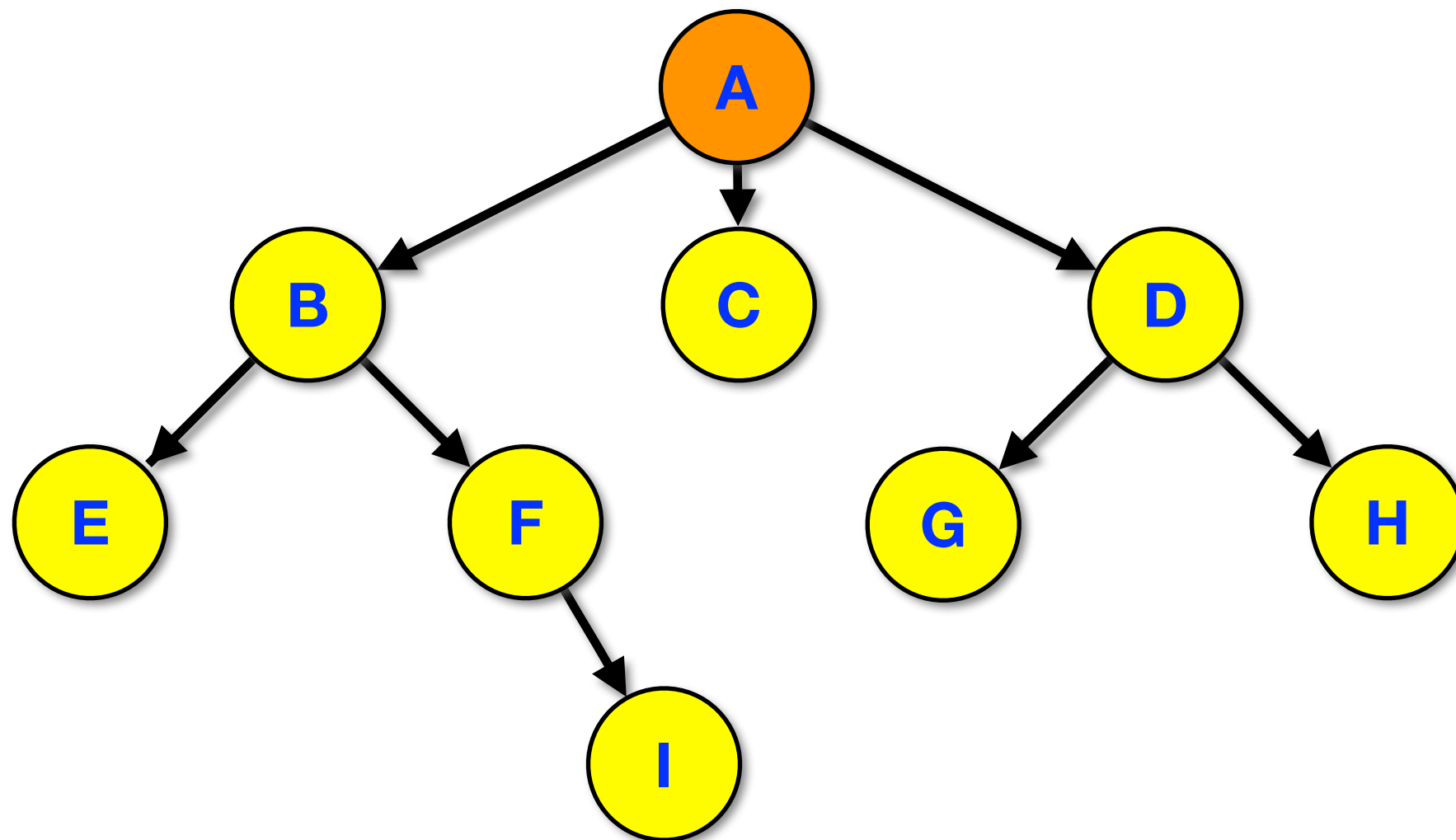
The node D has two descendants: G, H

The node F has one descendant: I

The node C has zero descendants

All nodes are descendants of the root node

p is an descendant of q iff there exists a path from q to p



Tree Implementation

- **A tree structure can be implemented in multiple different ways:**
 - (1) Each parent node stores references to all of its children
 - good approach when arity is small (e.g. binary trees)
 - Not a good choice when arity is high
 - Not a good choice when the number of children is unknown beforehand
 - (2) Each parent node stores references to first child, each child stores references to next sibling
 - A good approach when large fanout (large number of children per node)
 - Parent can have many children without wasting space in cases where there are only a few children

A Parent/Sibling Tree

