

CS420: Operating Systems

Cryptography

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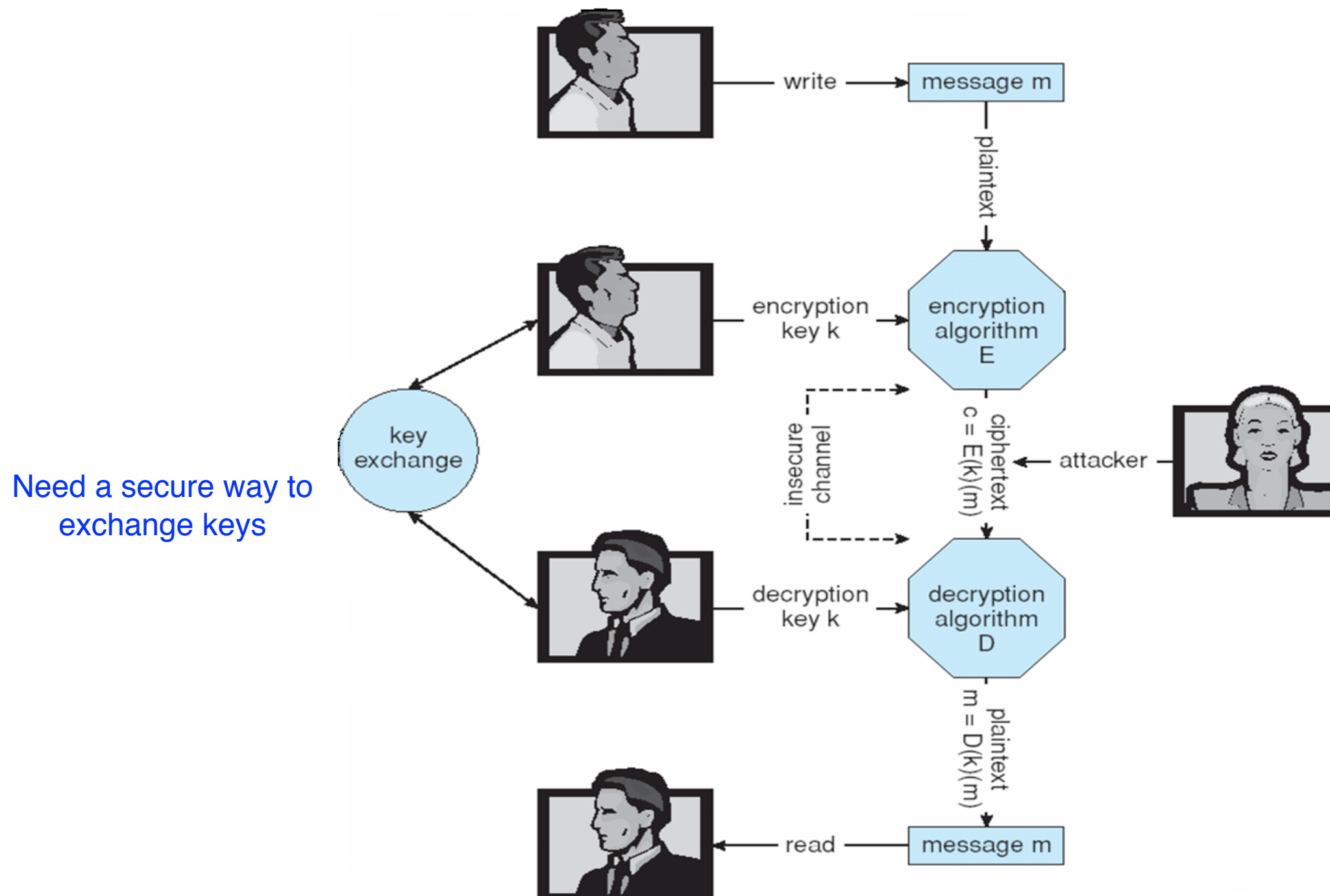
Cryptography as a Security Tool

- **Broadest security tool available when communicating with unknown users over a network**
 - An eavesdropper may be listening to your communication
 - **Encryption** can prevent an eavesdropper from reading messages
 - Difficult to know what machine you are communicating with over network
 - **Authentication** can confirm the identity of remote machine

Cryptography as a Security Tool (cont.)

- **Means to constrain potential senders (sources) and / or receivers (destinations) of messages**
 - Based on secrets (keys)
 - Enables
 - Confirmation of source
 - Receipt of message only by certain destination
 - Trust relationship between sender and receiver

Secure Communication Over Insecure Medium



Encryption

- **Encryption algorithm consists of**

- Set K of keys
- Set M of Messages
- Set C of ciphertexts (encrypted messages)
- A function $E : K \rightarrow (M \rightarrow C)$. That is, for each $k \in K$, $E(k)$ is a function for generating ciphertexts from messages
 - Both E and $E(k)$ for any k should be efficiently computable functions
- A function $D : K \rightarrow (C \rightarrow M)$. That is, for each $k \in K$, $D(k)$ is a function for generating messages from ciphertexts
 - Both D and $D(k)$ for any k should be efficiently computable functions

- **An encryption algorithm must provide this essential property: Given a ciphertext $c \in C$, a computer can compute m such that $E(k)(m) = c$ only if it possesses $D(k)$**

- Thus, a computer holding $D(k)$ can decrypt ciphertexts to the plaintexts used to produce them, but a computer not holding $D(k)$ cannot decrypt ciphertexts
- Since ciphertexts are generally exposed (for example, sent on the network), it is important that it be infeasible to derive $D(k)$ from the ciphertexts

Symmetric Encryption

- **Same key used to encrypt and decrypt**
 - $E(k)$ can be derived from $D(k)$, and vice versa
 - Requires sender and receiver to know a shared secret key
- **DES is a commonly used symmetric block-encryption algorithm**
 - Encrypts a block of data at a time
 - Triple-DES considered more secure (DES applied 3 times)
- **Advanced Encryption Standard (AES) is widely used (favored by many)**

Diffie Hellman Key Exchange

- **Does not require sender / receiver know a shared secret key**
 - Sender and receiver each have two keys: a **shared public key** and a **private key**
 - These keys are used to create a shared secret key
- **Does NOT provide authentication**
- **Vulnerable to man-in-the-middle attacks**
 - Another public key cryptography technique that avoids this problem is **RSA**

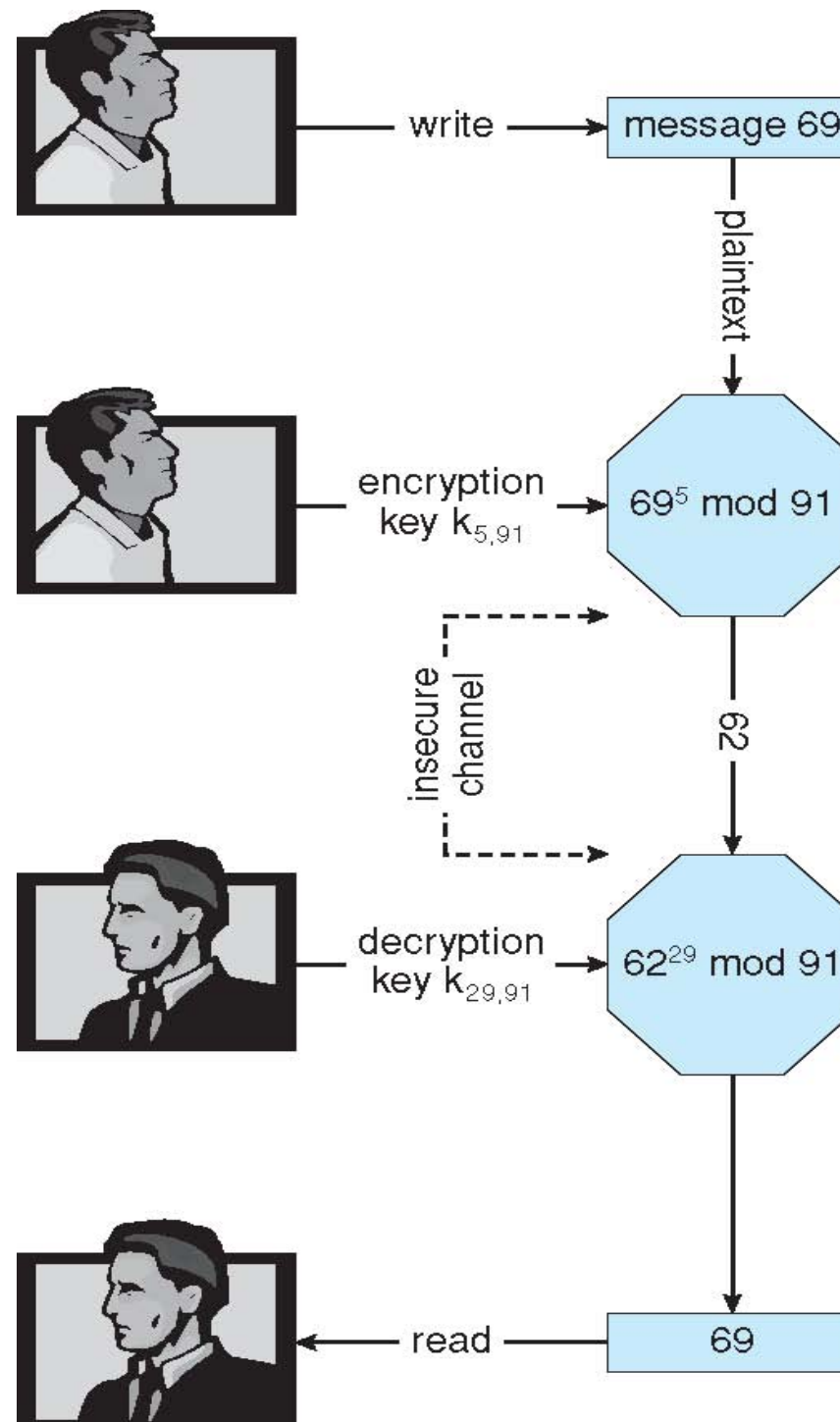
Asymmetric Encryption

- **Public-key encryption based on each user having two keys:**
 - **shared public key** – published key used to encrypt data
 - **private key** – key known only to individual user used to decrypt data
- **Must be an encryption scheme that can be made public without making it easy to figure out the decryption scheme**
 - RSA block cipher is common
 - Efficient algorithm for testing whether or not a number is prime
 - No efficient algorithm is known for finding the prime factors of a number

Asymmetric Encryption (Cont.)

- **Formally, it is computationally infeasible to derive $D(k_d, N)$ from $E(k_e, N)$, and so $E(k_e, N)$ need not be kept secret and can be widely disseminated**
 - $E(k_e, N)$ (or just k_e) is the public key
 - $D(k_d, N)$ (or just k_d) is the private key
 - N is the product of two large, randomly chosen prime numbers p and q (for example, p and q are 512 bits each)
 - Encryption algorithm is $E(k_e, N)(m) = m^{k_e} \bmod N$, where k_e satisfies $k_e k_d \bmod (p-1)(q-1) = 1$
 - The decryption algorithm is then $D(k_d, N)(c) = c^{k_d} \bmod N$

Encryption/Decryption with RSA Asymmetric Cryptography



Authentication

- **Constraining set of potential senders of a message**

- Complementary and sometimes redundant to encryption
- Also can prove message unmodified

- **Algorithm components**

- A set K of keys
- A set M of messages
- A set A of authenticators
- A function $S : K \rightarrow (M \rightarrow A)$
 - That is, for each $k \in K$, $S(k)$ is a function for generating authenticators from messages
 - Both S and $S(k)$ for any k should be efficiently computable functions
- A function $V : K \rightarrow (M \times A \rightarrow \{\text{true}, \text{false}\})$. That is, for each $k \in K$, $V(k)$ is a function for verifying authenticators on messages
 - Both V and $V(k)$ for any k should be efficiently computable functions

Authentication – Digital Signature

- **Based on asymmetric keys and digital signature algorithm**
- **Authenticators produced are digital signatures**
- **In a digital-signature algorithm, computationally infeasible to derive $S(k_s)$ from $V(k_v)$**
 - V is a one-way function
 - Thus, k_v is the public key and k_s is the private key
- **Consider the RSA digital-signature algorithm**
 - Similar to the RSA encryption algorithm, but the key use is reversed
 - Digital signature of message $S(k_s)(m) = H(m)^{k_s} \bmod N$
 - The key k_s again is a pair d, N , where N is the product of two large, randomly chosen prime numbers p and q
 - Verification algorithm is $V(k_v)(m, a) \equiv (a^{k_v} \bmod N = H(m))$
 - Where k_v satisfies $k_v k_s \bmod (p-1)(q-1) = 1$

Digital Certificates

- **Proof of who or what owns a public key**
- **Public key digitally signed a trusted party**
- **Trusted party receives proof of identification from entity and certifies that public key belongs to entity**
- **Certificate authority are trusted party – their public keys included with web browser distributions**
 - They vouch for other authorities via digitally signing their keys, and so on