

# CS420: Operating Systems

## Cryptography

---

James Moscola

Department of Engineering & Computer Science  
York College of Pennsylvania



# Cryptography as a Security Tool

---

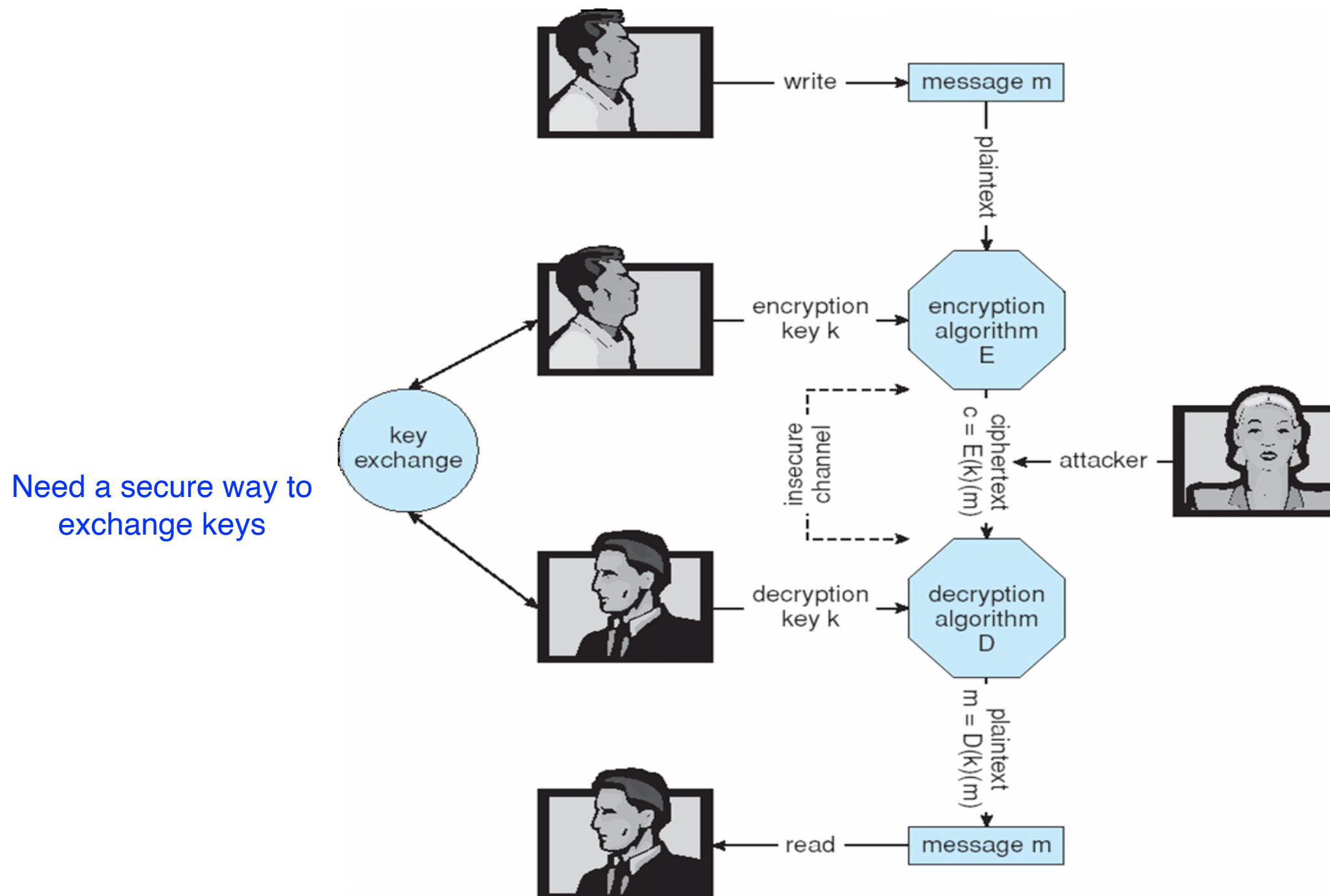
- **Broadest security tool available when communicating with unknown users over a network**
  - An eavesdropper may be listening to your communication
    - **Encryption** can prevent an eavesdropper from reading messages
  - Difficult to know what machine you are communicating with over network
    - **Authentication** can confirm the identity of remote machine

# Cryptography as a Security Tool (cont.)

---

- **Means to constrain potential senders (sources) and / or receivers (destinations) of messages**
  - Based on secrets (keys)
  - Enables
    - Confirmation of source
    - Receipt of message only by certain destination
    - Trust relationship between sender and receiver

# Secure Communication Over Insecure Medium



# Encryption

---

- **Encryption algorithm consists of**

- Set  $K$  of keys
- Set  $M$  of Messages
- Set  $C$  of ciphertexts (encrypted messages)
- A function  $E : K \rightarrow (M \rightarrow C)$ . That is, for each  $k \in K$ ,  $E(k)$  is a function for generating ciphertexts from messages
  - Both  $E$  and  $E(k)$  for any  $k$  should be efficiently computable functions
- A function  $D : K \rightarrow (C \rightarrow M)$ . That is, for each  $k \in K$ ,  $D(k)$  is a function for generating messages from ciphertexts
  - Both  $D$  and  $D(k)$  for any  $k$  should be efficiently computable functions

- **An encryption algorithm must provide this essential property: Given a ciphertext  $c \in C$ , a computer can compute  $m$  such that  $E(k)(m) = c$  only if it possesses  $D(k)$**

- Thus, a computer holding  $D(k)$  can decrypt ciphertexts to the plaintexts used to produce them, but a computer not holding  $D(k)$  cannot decrypt ciphertexts
- Since ciphertexts are generally exposed (for example, sent on the network), it is important that it be infeasible to derive  $D(k)$  from the ciphertexts

# Symmetric Encryption

---

- **Same key used to encrypt and decrypt**
  - $E(k)$  can be derived from  $D(k)$ , and vice versa
  - Requires sender and receiver to know a shared secret key
- **DES is a commonly used symmetric block-encryption algorithm**
  - Encrypts a block of data at a time
  - Triple-DES considered more secure (DES applied 3 times)
- **Advanced Encryption Standard (AES) is widely used (favored by many)**

# Diffie Hellman Key Exchange

---

- **Does not require sender / receiver know a shared secret key**
  - Sender and receiver each have two keys: a **shared public key** and a **private key**
  - These keys are used to create a shared secret key
- **Does NOT provide authentication**
- **Vulnerable to man-in-the-middle attacks**
  - Another public key cryptography technique that avoids this problem is **RSA**

# Asymmetric Encryption

---

- **Public-key encryption based on each user having two keys:**
  - **shared public key** – published key used to encrypt data
  - **private key** – key known only to individual user used to decrypt data
- **Must be an encryption scheme that can be made public without making it easy to figure out the decryption scheme**
  - RSA block cipher is common
  - Efficient algorithm for testing whether or not a number is prime
  - No efficient algorithm is known for finding the prime factors of a number

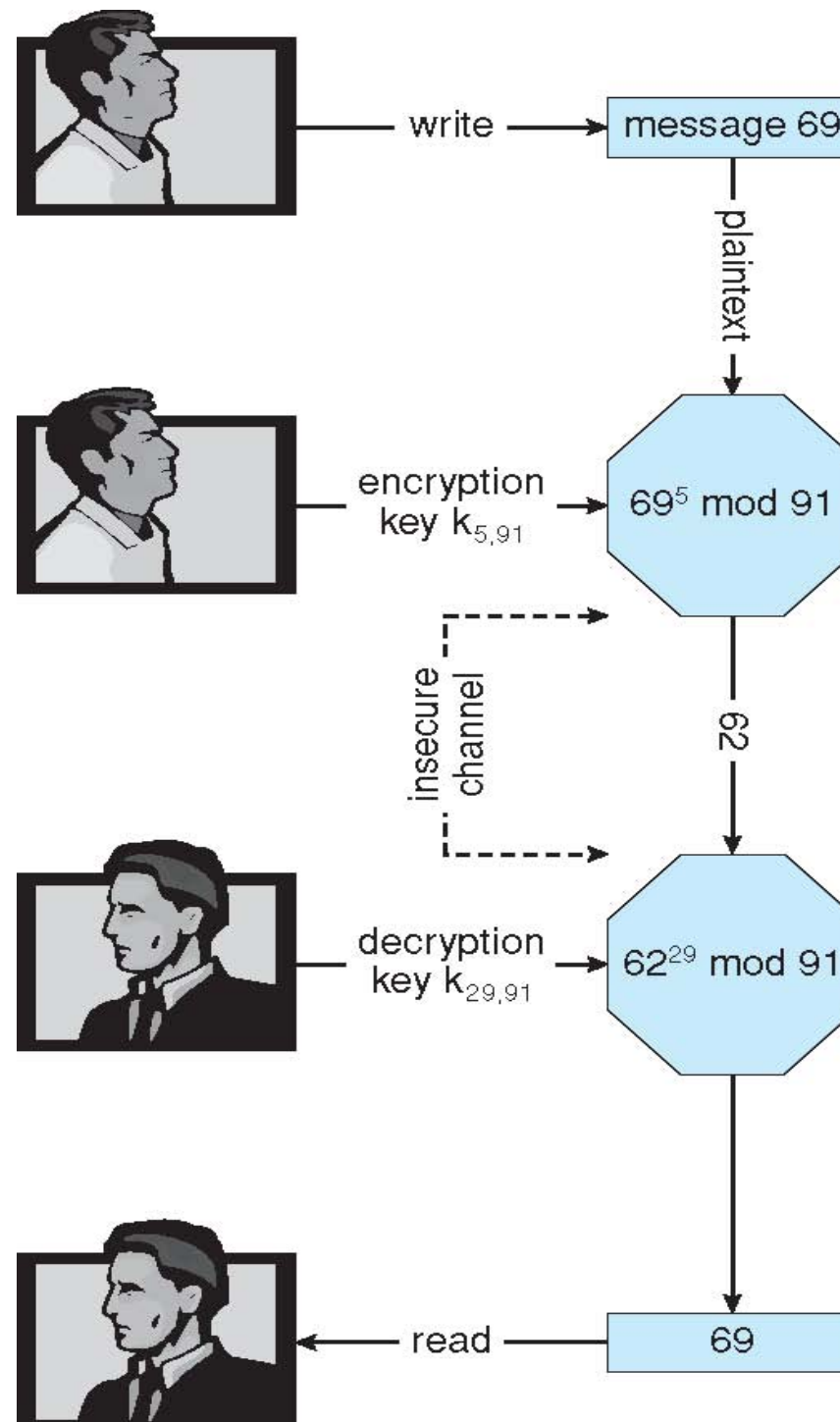


# Asymmetric Encryption (Cont.)

---

- **Formally, it is computationally infeasible to derive  $D(k_d, N)$  from  $E(k_e, N)$ , and so  $E(k_e, N)$  need not be kept secret and can be widely disseminated**
  - $E(k_e, N)$  (or just  $k_e$ ) is the public key
  - $D(k_d, N)$  (or just  $k_d$ ) is the private key
  - $N$  is the product of two large, randomly chosen prime numbers  $p$  and  $q$  (for example,  $p$  and  $q$  are 512 bits each)
  - Encryption algorithm is  $E(k_e, N)(m) = m^{k_e} \bmod N$ , where  $k_e$  satisfies  $k_e k_d \bmod (p-1)(q-1) = 1$
  - The decryption algorithm is then  $D(k_d, N)(c) = c^{k_d} \bmod N$

# Encryption/Decryption with RSA Asymmetric Cryptography



# Authentication

---

- **Constraining set of potential senders of a message**

- Complementary and sometimes redundant to encryption
- Also can prove message unmodified

- **Algorithm components**

- A set  $K$  of keys
- A set  $M$  of messages
- A set  $A$  of authenticators
- A function  $S : K \rightarrow (M \rightarrow A)$ 
  - That is, for each  $k \in K$ ,  $S(k)$  is a function for generating authenticators from messages
  - Both  $S$  and  $S(k)$  for any  $k$  should be efficiently computable functions
- A function  $V : K \rightarrow (M \times A \rightarrow \{\text{true}, \text{false}\})$ . That is, for each  $k \in K$ ,  $V(k)$  is a function for verifying authenticators on messages
  - Both  $V$  and  $V(k)$  for any  $k$  should be efficiently computable functions

# Authentication – Digital Signature

---

- **Based on asymmetric keys and digital signature algorithm**
- **Authenticators produced are digital signatures**
- **In a digital-signature algorithm, computationally infeasible to derive  $S(k_s)$  from  $V(k_v)$** 
  - $V$  is a one-way function
  - Thus,  $k_v$  is the public key and  $k_s$  is the private key
- **Consider the RSA digital-signature algorithm**
  - Similar to the RSA encryption algorithm, but the key use is reversed
  - Digital signature of message  $S(k_s)(m) = H(m)^{k_s} \bmod N$
  - The key  $k_s$  again is a pair  $d, N$ , where  $N$  is the product of two large, randomly chosen prime numbers  $p$  and  $q$
  - Verification algorithm is  $V(k_v)(m, a) \equiv (a^{k_v} \bmod N = H(m))$ 
    - Where  $k_v$  satisfies  $k_v k_s \bmod (p-1)(q-1) = 1$

# Digital Certificates

---

- **Proof of who or what owns a public key**
- **Public key digitally signed a trusted party**
- **Trusted party receives proof of identification from entity and certifies that public key belongs to entity**
- **Certificate authority are trusted party – their public keys included with web browser distributions**
  - They vouch for other authorities via digitally signing their keys, and so on