

ECE335 Summer 2019 - Lecture 18 Examples

Example 1: Given the following set $A = \{1, 2, 3, 4\}$, define a binary relation as

$$R = \{(1, 1), (2, 1), (3, 1), (4, 4)\}$$

a. Is R *reflexive*? Explain.

No. $(2, 2) \notin R$

b. Is R *symmetric*? Explain.

No. $(2, 1) \in R$ but $(1, 2) \notin R$

c. Is R *transitive*? Explain.

Yes. $(2, 1) \wedge (1, 1) \rightarrow (2, 1) \in R$
 $(3, 1) \wedge (1, 1) \rightarrow (3, 1) \in R$

Example 2: Given the following set $A = \{0, 2, 4, 6, 8, 10\}$, define a binary relation as

$$R = \{(0, 6), (2, 10), (4, 8), (6, 0), (8, 4), (10, 2)\}$$

a. Is R *reflexive*? Explain.

No. $(0, 0) \notin R$

b. Is R *symmetric*? Explain.

Yes. $(0, 6) \wedge (6, 0) \in R$
 $(2, 10) \wedge (10, 2) \in R$
 $(4, 8) \wedge (8, 4) \in R$

c. Is R *transitive*? Explain.

No. $(0, 6) \wedge (6, 0) \in R$ but $(0, 0) \notin R$