

According to Ohm:

$$dr = \frac{dv}{di} = \frac{1}{di/dv}$$

Let's find the derivative of the Main Diode Formula (let's temporary name exponential part as  $\varepsilon(v)$ ):

$$\frac{d}{dv} [I_S(\varepsilon(v) + 1)] = \frac{d}{dv} (I_S)(\varepsilon(v) + 1) + I_S \frac{d}{dv} (\varepsilon(v) + 1)$$

First part is zero (derivative from a constant), the second one, due to  $(e^u)' = e^u \cdot u'$  becomes:

$$I_S \frac{d}{dv} \varepsilon(v) = I_S e^{v/\eta V_T} \cdot \frac{1}{\eta V_T}; \quad \frac{1}{di/dv} = \frac{\eta V_T}{I_S e^{v/\eta V_T}}$$

Since we can substitute  $I_S e^{v/\eta V_T}$  with  $i + I_S$ , than finally:

$$r_D = \frac{\eta V_T}{i_D + I_S} \approx \frac{\eta V_T}{i_D}$$

Again, we can easily drop off 1 because we do not deal now with extremely small currents.

The solution for rDs is rd1A = 0.043 Ohm and rd2A = 0.022 Ohm.

Note that if we take a reciprocal of the differential resistance we can observe corresponding angles of the I-V curve:  $\text{atan}(1/0.043) = 87.5\text{deg}$  and  $\text{atan}(1/0.022) = 88.7\text{deg}$ .