Complex Analysis I: Problem Set X

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Abstract

This work contains the solutions to the problem set X of Complex Analysis I 2015 at Courant Institute of Mathematical Sciences.

Question 1.

1. Find the fractional linear transformation which sends 1, i, -i to 2, -1, 1 respectively.

Question 2.

2. Find the fractional linear transformation which carries the circle |z|=2 into |z+1|=1, the point -2 into the origin, and the origin into i.

Question 3.

3. Suppose that a fractional linear transformation sends a pair of concentric circle to another pair of concentric circle, show the ratios of the radius must be the same.

Question 4.

4. Find a fractional linear transformation which carries |z|=1 and $|z-\frac{1}{4}|=\frac{1}{4}$ into concentric circles. What is the ratio of radius?

Question 5.

5. Given a circle or line, we call the map sending any point to its symmetric point as a reflection. Reflect the imaginary axis, the line x=y, and the circle |z|=1 into the circle |z-2|=1.