Graph fragmentation under sparsification