

1. **(2 pts)** Determine asymptotic growth rate (Big-O) of the following functions and order them in the ascending order (fastest to slowest).

$7n \log n + 5n$

$2^{\log n}$

$5n + 50 \log n$

2^n

$3n$

2^{12}

$n^2 + 100n$

$15n \log n$

n^3

2. **(2 pts)** Characterize following Python function using Big-O notation.

To get full points, justify your answer.

```
def function(data):  
    value = data[0]  
    for i in range(len(data)):  
        if data[i] < value:  
            value = data[i]  
    return value
```

3. (2 pts) Characterize following Python function using Big-O notation.

To get full points, justify your answer.

```
def sum_of_prefixes(X, Y): # X and Y have the same size
    '''Return number of elements in Y equal to the sum of prefix sums in X'''
    n = len(X)
    counter = 0
    for i in range(n): # loops 0 to n-1
        tot = 0
        for j in range(n): # loops 0 to n-1
            for k in range(1 + j): # loops 0 to j
                tot += X[k]
            if Y[i] == tot:
                counter += 1
    return counter
```

4. (4 pts) Determine computational complexity of the following Python code and prove it using induction. To get full points, justify your answer and describe induction steps.

```
n = 10
for x in range(n):
    print("Outer iteration: {}".format(x))
    for y in range(x + 1, 0, -1):
        print("\tInner iteration: {}".format(y))
    print()
```