

## \* Training / Validation / Test sets

size	price		
2104	400	} training set 60%	$(x^{(1)}, y^{(1)})$ $\vdots$ $(x^{(m_{\text{train}})}, y^{(m_{\text{train}})})$ $m_{\text{train}} = 6$
1600	330		
$\vdots$	$\vdots$		
1985	300		
1534	315	} validation set 20%	$(x_{\text{cv}}^{(1)}, y_{\text{cv}}^{(1)})$ $\vdots$ $(x_{\text{cv}}^{(m_{\text{cv}})}, y_{\text{cv}}^{(m_{\text{cv}})})$ $m_{\text{cv}} = 2$
1427	199		
1380	212	} test set 20%	$(x_{\text{test}}^{(1)}, y_{\text{test}}^{(1)})$ $\vdots$ $(x_{\text{test}}^{(m_{\text{test}})}, y_{\text{test}}^{(m_{\text{test}})})$ $m_{\text{test}} = 2$
1494	243		

Training error:  $J_{\text{train}}(\vec{w}, b) = \frac{1}{2m_{\text{train}}} \left[ \sum_{i=1}^{m_{\text{train}}} (f_{\vec{w}, b}(\vec{x}^{(i)}) - y^{(i)})^2 \right]$

Validation error:  $J_{\text{cv}}(\vec{w}, b) = \frac{1}{2m_{\text{cv}}} \left[ \sum_{i=1}^{m_{\text{cv}}} (f_{\vec{w}, b}(\vec{x}_{\text{cv}}^{(i)}) - y_{\text{cv}}^{(i)})^2 \right]$

Test error:  $J_{\text{test}}(\vec{w}, b) = \frac{1}{2m_{\text{test}}} \left[ \sum_{i=1}^{m_{\text{test}}} (f_{\vec{w}, b}(\vec{x}_{\text{test}}^{(i)}) - y_{\text{test}}^{(i)})^2 \right]$

$\Downarrow$  then model selection

$$\begin{aligned}
 d=1: f_{\vec{w}, b}(\vec{x}) &= w_1 x_1 + b & \longrightarrow w^{(1)}, b^{(1)} & \longrightarrow J_{\text{cv}}(w^{(1)}, b^{(1)}) \\
 d=2: f_{\vec{w}, b}(\vec{x}) &= w_1 x_1 + w_2 x_2 + b & \longrightarrow w^{(2)}, b^{(2)} & \longrightarrow J_{\text{cv}}(w^{(2)}, b^{(2)}) \\
 d=3: f_{\vec{w}, b}(\vec{x}) &= w_1 x_1 + w_2 x_2 + w_3 x_3 + b & \vdots & \\
 \vdots & & & \\
 d=10: f_{\vec{w}, b}(\vec{x}) &= w_1 x_1 + w_2 x_2 + \dots + w_{10} x_{10} + b & \longrightarrow w^{(10)}, b^{(10)} & \longrightarrow J_{\text{cv}}(w^{(10)}, b^{(10)})
 \end{aligned}$$

Choose  $d=4$

$\Rightarrow$  If  $J_{\text{cv}}(w^{(4)}, b^{(4)})$  is the lowest  $\Rightarrow$  Pick  $w_1 x_1 + \dots + w_4 x_4 + b$

then "estimate generalization error using test set":  $J_{\text{test}}(w^{(4)}, b^{(4)})$