ME 552 Lab 01 Report

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Question 1

(a)

We design the circuit as shown below:

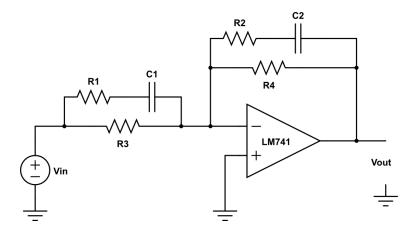


Figure 1: A lead-lag compensator circuit diagram for question 1.

(b)

We can let R_1 , C_1 , R_3 and R_2 , C_2 , R_4 form two different impedance module separately, and let their impedance equal Z_1 and Z_2 , we can get:

$$\begin{split} Z_1 &= \frac{R_3 * (R_1 + (1/sC_1))}{R_3 + (R_1 + (1/sC_1))} = \frac{R_3 (sR_1C_1 + 1)}{s(R_1C_1 + R_3C_1) + 1} \\ Z_2 &= \frac{R_4 * (R_2 + (1/sC_2))}{R_4 + (R_2 + (1/sC_2))} = \frac{R_4 (sR_2C_2 + 1)}{s(R_2C_2 + R_4C_2) + 1} \end{split}$$

The new circuits can be seen as an inverting amplifier:

$$\begin{split} \frac{V_{out}(s)}{V_{in}(s)} &= -\frac{Z_2}{Z_1} = -\frac{R_4(sR_2C_2+1)}{(s(R_2C_2+R_4C_2)+1)} \frac{(s(R_1C_1+R_3C_1)+1)}{R_3(sR_1C_1+1)} \\ &= -\frac{R_4}{R_3} \frac{(sR_2C_2+1)}{(s(R_2C_2+R_4C_2)+1)} \frac{(s(R_1C_1+R_3C_1)+1)}{(sR_1C_1+1)} \end{split}$$

If we assume $R_3 = R_4$, we will gain the standard formula of lead-lag compensator.