

Prove that for any integer  $n$ , at least one of the integers  $n, n + 2$  or  $n + 4$  is divisible by 3.

Again this proposition can be proven by a **direct proof**.

**Direct Proof:** First if  $n$  is divisible by there is no need to look at  $n + 2$  or  $n + 4$ , but if  $n$  is not divisible by 3, then it is clear that  $n$  is either of the form  $3m + 1$  or  $3m + 2$  where  $m \in \mathbb{Z}$ .

Then if  $n = 3m + 1$

$$n + 2 = 3m + 3 \text{ which is clearly divisible by 3}$$

Else if  $n = 3m + 2$

$$n + 4 = 3m + 6 \text{ which is clearly divisible by 3}$$

So this statement is true, concluding the proof.