

# Probabilistic Reasoning

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Practice4

# 실습 1. Basic Probability

## ■ Seeing Theory

- <https://students.brown.edu/seeing-theory/index.html>

## ■ Basic Probability

### Example of Random Sampling with Replacement

```
# Probability of drawing spade
printProb(event_probability(deck['spades'], deck['cards']))
printProb(event_probability(deck['spades'], deck['cards']))
printProb(event_probability(deck['spades'], deck['cards']))
# Probability of drawing spade
printProb(event_probability(deck['hearts'], deck['cards']))
printProb(event_probability(deck['hearts'], deck['cards']))
printProb(event_probability(deck['hearts'], deck['cards']))
```

```
25.0%
25.0%
25.0%
25.0%
25.0%
25.0%
```

### Example of Random Sampling without Replacement

```
# returns the probability of drawing the card then draw from the deck
def draw(card, deck):
    #fill the (1)
    (1)
    return prob
```

```
# Print probabilities
printProb(draw('spades', deck))
printProb(draw('spades', deck))
printProb(draw('spades', deck))
printProb(draw('hearts', deck))
printProb(draw('hearts', deck))
printProb(draw('hearts', deck))
```

```
25.0%
23.53%
22.0%
26.53%
25.0%
23.4%
```

## 실습 2. Naïve Bayes (scikit-learn)

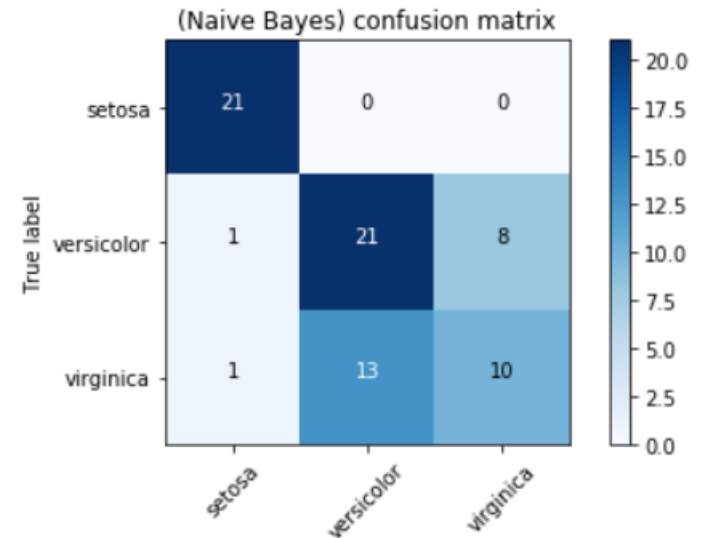
- Iris data set classification

```
Classification Report
      precision    recall  f1-score   support

   setosa      0.91      1.00      0.95        21
  versicolor    0.62      0.70      0.66        30
   virginica    0.56      0.42      0.48        24

 avg / total    0.68      0.69      0.68        75

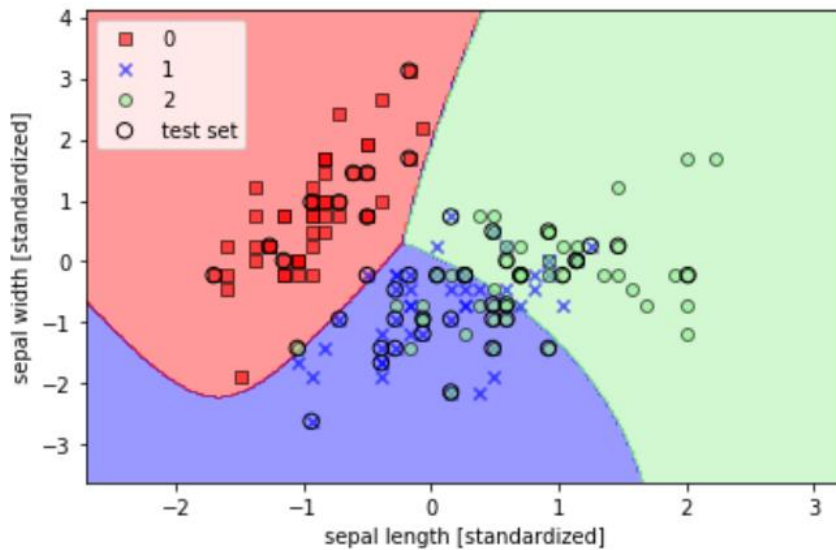
Accuracy
0.693333333333
```



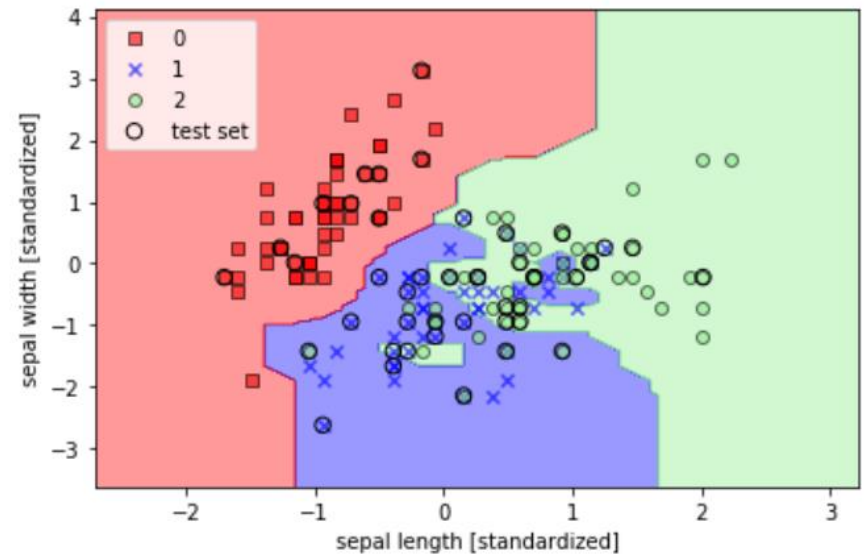
## 실습 2. Naïve Bayes (scikit-learn)

- Plot Decision Regions

### Decision Region of Naive Bayes



### Decision Region of KNN



## 실습 3. Custom Naïve Bayes Implementation

### Bayesian Classifier Example

No.	age	income	student	credit_rating	buys_computer
1	<=30	high	no	fair	no
2	<=30	high	no	excellent	no
3	31...40	high	no	fair	yes
4	>40	medium	no	fair	yes
5	>40	low	yes	fair	yes
6	>40	low	yes	excellent	no
7	31...40	low	yes	excellent	yes
8	<=30	medium	no	fair	no
9	<=30	low	yes	fair	yes
10	>40	medium	yes	fair	yes
11	<=30	medium	yes	excellent	yes
12	31...40	medium	no	excellent	yes
13	31...40	high	yes	fair	yes
14	>40	medium	no	excellent	no

# 실습 3. Custom Naïve Bayes Implementation

```
def getPredictionBayes(dataSet, X):
    classProb = {
        'yes': 1,
        'no': 1
    }
    numberOfData = len(dataSet)

    for classValue in classProb.keys():
        probability = 1

        naiveBayesPrint(classValue)

        # P(Yes) or P(No)
        classCount = countClass(classValue, dataSet)
        # fill the blank (3)
        p = (3)
        probability *= p
        print("%.5f" % p, end=' ')

        for i in range(len(X)):
            value = X[i]
            # ex) P(<30|Yes)

            # fill the blank (4)
            p = (4)
            print(" * %.5f" % p, end=' ')
            probability *= p
            print("\n = %.5f" % probability)

        classProb[classValue] = probability

    bestClass, bestProb = None, -1
    for classValue, probability in classProb.items():
        if bestClass is None or probability > bestProb:
            bestProb = probability
            bestClass = classValue

    return bestClass, bestProb
```

```
# get number of value in i^th column
def count(classValue, i, value, dataSet):
    n = 0
    for instance in dataSet:
        # fill the blank (1) & (2)
        if (1) and (2):
            n += 1

    return n
```

## Classification Results

X: ['<=30', 'medium', 'yes', 'fair']

$P(\text{yes}|X) = P(\text{yes}) * P(X|\text{yes}) =$   
 $P(\text{yes}) * P(\leq 30|\text{yes}) * P(\text{medium}|\text{yes}) * P(\text{yes}|\text{yes}) * P(\text{fair}|\text{yes})$   
 $0.64286 * 0.22222 * 0.44444 * 0.66667 * 0.66667$   
 $= 0.02822$

$P(\text{no}|X) = P(\text{no}) * P(X|\text{no}) =$   
 $P(\text{no}) * P(\leq 30|\text{no}) * P(\text{medium}|\text{no}) * P(\text{yes}|\text{no}) * P(\text{fair}|\text{no})$   
 $0.35714 * 0.60000 * 0.40000 * 0.20000 * 0.40000$   
 $= 0.00686$

```
#####
X is classified to "yes"
probability = 0.02822
#####
```

# 실습 4. Understanding Generative Model

