Discrete-Event Modeling Using DEVS Assignment 1

SYSC 5104

Player Substitution System (PSS) Model

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PART I - Overview

Real System

For this assignment, I will be modelling the behavior of a player substitution system for a sports team during a game. This system should emulate the decision-making process of a coach when deciding whether to substitute a player in or not; this decision will be based on the player's state and the current game score.

As the game progresses, each player's mental and fatigue level and time metrics (time spent recovering on the bench and total time played) will be monitored. Additionally, the current game score (i.e., team winning, losing, or tied) will be taken into account. The coach will evaluate these factors and then make a decision.

The system's complexity will depend on the substitution logic and the addition of other factors such as hydration level, confidence level, player position, key player, etc. Typically, in sports games, starter players will average more playing time than bench players. However, the scope of this system will focus on two players and not consider the aforementioned factors. If more realism is expected, these factors can still come into play in the future.

Sketch of Model Structure

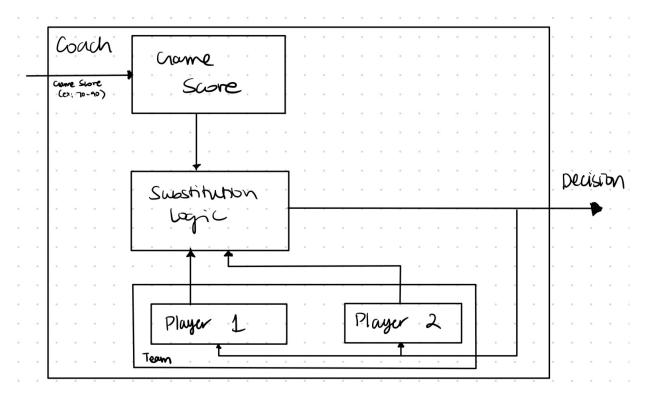


Figure 1: Original Sketch of Coach Model

Behavior of Each Component

• Coach Model:

o Top-level component that contains the submodels below

• Game Score Model:

- Receives inputs of the current game score of team 1 and team 2
- o Output whether team is winning, losing, or tied

• Player Model:

- Monitors player fatigue and mental level
- Records the following time metrics:
 - time spent recovering on the bench
 - total time played
- o Can either be on the field or bench
- Receives input of substitution and game score state and updates metrics accordingly

• Substitution Logic Model:

- o Contains the decision making logic for making a substitution or not
- Receives inputs of player and game score status

• Team Model:

 Coupled model that indicates to the player that he has been subbed (routes substitution logic input to the players)

PART II - Behavior and Formal Specification

The atomic models are Game Score, Substitution Logic, Player (duplicated for two players) The coupled models are Coach (top-level) and Team.

In the following examples, assume 1 time unit is 1 minute (in simulation/code 1 time unit is 1 second)

Player - Behavior

Fatigue

- **Definition:** how tired player is [0, 100]
 - o 0: fully rested
 - o 100: completely exhausted

• How it changes: δ_{int}

- On the field: increases over time (+1.5 per time unit)
- On the bench: decreases over time (-1 per time unit)

Example:

- Player starts on the field
 - Fatigue = 0.0
- After 10 minutes on the field
 - Fatigue = 15
- o After 20 minutes on the field
 - \blacksquare Fatigue = 30
- Player is substituted out (goes to bench)
 - Fatigue = 30 (stays constant)
- After 5 minutes on the bench
 - Fatigue = 25
- **Future improvement:** to replicate real-life performance better, both rates (+/-) should be exponential
 - Get more tired as time goes on
 - Resting becomes worse as time goes (not as effective)

Mental

- **Definition:** player's stress/confidence level [100, 0]
 - o 100: not stressed or high confidence
 - o 0: very stressed or low confidence
- How it changes: δ_{int}
 - o On the field: fluctuates randomly to mimic real-life performance
 - Note that this will be removed for testing purposes to keep things deterministic
 - On the bench: slightly increase over time (+1 per unit of time)
- How it changes: δ_{ext}
 - Team is losing: decrease over time (-2 per unit of time)
 - Team is winning: increase over time (+2 per unit of time)
 - Team is tied: mental stays constant (no change)
- Rules for δ_{int} (uniform random number to discrete variate):
 - Small mistake:
 - Decrease mental by 5 units
 - Probability: 25% per time unit
 - Big mistake:
 - Decrease mental by 10 units
 - Probability: 10% per time unit
 - Score a goal:
 - Increase mental by 15 units
 - Probability: 5% per time unit
 - Assist a goal:
 - Increase mental by 7.5 units

- Probability: 10% per time unit
- O No event:
 - Mental remains constant
 - Probability: 50% per time unit

• Example 1 (with random events)

- o Minute 1 (Team Tied, On Field)
 - Random event: No event
 - Event input: Team Tied \rightarrow no change
 - Mental State $100 \rightarrow 100$
- Minute 2 (Team Losing, On Field)
 - Random event: big mistake mistake (25%, -10)
 - Event input: Team Losing \rightarrow -2 per time unit
 - Total change: -10 2 = -12
 - Mental State: $100 \rightarrow 88$
- Minute 3 (Team Losing, On Field)
 - Random event: Assist a goal (10%, +7.5)
 - Event input: Team Losing \rightarrow -2 per time unit
 - Total change: +7.5 2 = 5.5
 - Mental State: $88 \rightarrow 93.5$
- Minute 4 (Team Winning, On Field)
 - Random event: No event
 - Event input: Team Winning \rightarrow +2 per time unit
 - Mental State: $93.5 \rightarrow 95.5$
- Minute 5 (Team Winning, On Bench)
 - Recovery: +1 per time unit
 - Mental State: $95.5 \rightarrow 96.5$

• Example 2 (no random events):

- Minute 1 (Team Tied, On Field)
 - Event input: Team Tied \rightarrow no change
 - Mental State $100 \rightarrow 100$
- Minute 2 (Team Losing, On Field)
 - Event input: Team Losing \rightarrow -2 per time unit
 - Mental State: $100 \rightarrow 98$
- Minute 3 (Team Losing, On Field)
 - Event input: Team Losing \rightarrow -2 per time unit
 - Mental State: $98 \rightarrow 96$
- Minute 4 (Team Winning, On Field)
 - Event input: Team Winning \rightarrow +2 per time unit
 - Mental State: $96 \rightarrow 98$
- Minute 5 (Team Winning, On Bench)

- Recovery: +1 per time unit
- Mental State: $98 \rightarrow 99$
- **Future improvement:** to replicate real-life performance better, implement random mental fluctuations according to the rules above, and mimic Example 1 shown above
 - For implementation and testing purposes, the code will reflect closer to the behavior of Example 2

Time

- **Definition:** two different time metrics
 - Time played: total time the player has been on the field
 - Time on bench: the time a player has spent recovering on the bench
- How it changes: δ_{int}
 - o On the field:
 - Time played: increases over time (+1 per time unit)
 - On the bench
 - Time on bench: increases over time (+1 per time unit)
- How it changes: δ_{ext}
 - Player gets subbed in (goes to field):
 - Time bench: resets to 0
 - Player gets subbed out (goes to bench):
 - Time played: remains constant
- Example:
 - Player starts on the field
 - Time played: 0
 - Time on bench: 0
 - o After 10 minutes on the field
 - Time played: 10
 - Time on bench: 0
 - Player gets substituted out
 - Time played: 10 (remains constant)
 - Time on bench: 0
 - After 5 minutes on the bench
 - Time played: 10
 - Time on bench: 5
 - Player gets substituted in:
 - Time played: 10
 - Time on bench: 0 (resets to 0)
- Future improvement: monitor more time variables, such as the last time played, for better decision making

Full Example with all metrics

- 0 Minute: Player starts on field
 - o Game state: TIED
 - o Fatigue: 0
 - o Mental: 100
 - o Time played: 0
 - Time on bench: 0
- 10 minutes: ON FIELD (10 minutes elapsed)
 - o Game state: TIED
 - o Fatigue: 15
 - o Mental: 100
 - o Time played: 10
 - o Time on bench: 0
- 20 minutes: ON FIELD (10 minutes elapsed)
 - o Game state: TIED
 - o Fatigue: 30
 - o Mental: 100
 - o Time played: 20
 - o Time on bench: 0
- At 20 minutes: Player gets substituted out: ON BENCH
 - o Game state: TIED
 - o Fatigue: 30
 - o Mental: 100
 - o Time played: 20
 - o Time on bench: 0
- 25 minutes: ON BENCH (5 minutes elapsed)
 - o Game state: TIED
 - o Fatigue: 25
 - o Mental: 100
 - o Time played: 20
 - Time on bench: 5
- At 26 minutes Player gets substituted in: ON FIELD
 - o Game state: TIED
 - o Fatigue: 24
 - o Mental: 100
 - o Time played: 20
 - o Time on bench: 0
- 30 minutes: ON FIELD (4 minutes elapsed)

- o Game state: TIED
- o Fatigue: 30
- o Mental: 100
- o Time played: 24
- Time on bench: 0
- At 30 minutes, Game State changes to LOSING
 - o Game state: LOSING
 - o Fatigue: 30
 - o Mental: 100
 - o Time played: 24
 - Time on bench: 0
- 40 minutes: ON FIELD (10 minutes elapsed)
 - o Game state: LOSING
 - o Fatigue: 45
 - o Mental: 80
 - o Time played: 34
 - Time on bench: 0
- 50 minutes: ON_FIELD (10 minutes elapsed)
 - o Game state: LOSING
 - o Fatigue: 60
 - o Mental: 60
 - o Time played: 44
 - Time on bench: 0
- At 50 minutes, Game State changes to WINNING
 - o Game state: WINNING
 - o Fatigue: 60
 - o Mental: 60
 - o Time played: 44
 - o Time on bench: 0
- At 51 minutes, Player gets substituted out: ON BENCH
 - o Game state: WINNING
 - o Fatigue: 61.5
 - o Mental: 62
 - o Time played: 45
 - Time on bench: 0
- 60 minutes: ON BENCH (9 minutes elapsed)
 - o Game state: WINNING
 - o Fatigue: 51.5
 - o Mental: 71
 - o Time played: 45

Player (Atomic) - Formal Specification

```
Player = \langle X, Y, S, \delta_{int}, \delta_{ext}, \lambda, t_a \rangle
X = \{(player\_out\_id \in \mathbb{N}, player\_in\_id \in \mathbb{N}), game\_state \in \{WINNING,LOSING,TIED\}\}
Y = \{\text{player id} \in \mathbb{N}, \text{mental} \in [0,100], \text{ fatigue} \in [0,100], \text{ phase} \in \{\text{ON FIELD}, \text{ phase}\}
ON BENCH, time played \in \mathbb{R}^+, time on bench \in \mathbb{R}^+}
S = \{player \ id \in \mathbb{N}, mental \in [0,100], fatigue \in [0,100], phase \in \{ON \ FIELD, \}\}
ON BENCH, time played \in \mathbb{R}^+, time on bench \in \mathbb{R}^+, game state \in
\{WINNING,LOSING,TIED\}, sigma \in \mathbb{R}^+\}
\delta_{int}(s) = \{
        case phase:
                 ON_FIELD:
                          fatigue = state.fatigue + 1.5 * sigma
                          if game state == WINNING:
                                   mental += 2.0 * sigma
                          elif game state == LOSING:
                                   mental = 2.0 * sigma
                          time played += state.sigma
                 ON BENCH:
                          fatigue = state.fatigue - 1.0 * sigma
                          mental = mental + 1.0 * sigma
                          time on bench += sigma
                          state.sigma = 1.0
        return *this
\delta_{\rm ext}(s, e, x) = \{
        if not empty(x.ids):
                 player out id, player in id = get substitution ids(x.ids)
                 if player out id == player id:
                          phase = ON BENCH
                 elif player in id == player id:
                          phase = ON FIELD
```

```
time on bench = 0
       if not empty(x.game):
               game state = get game state(x.game)
       state.sigma -= e
       return *this
\lambda(s) = \{
       return {
               player id,
               mental,
               fatigue,
               phase,
               time_played,
               time on bench
       }
}
t_a(s): {
       return sigma
}
```

Game Score - Behavior

Game State

- **Definition:** represents the current state of the game based on the scores of two teams (favors team 1)
 - o WINNING: Team 1 is leading
 - o LOSING: Team 1 is trailing
 - TIED: both teams have the same score
- How it changes: δ_{ext}
 - o Team 1 Score > Team 2 Score: WINNING
 - o Team 1 Score < Team 2 Score: LOSING
 - Team 1 Score = Team 2 Score: TIED
- How it changes: δ_{int}
 - No internal event occurs
- Example:
 - o Minute 1(Team 1: 0 | Team 2: 0)
 - TIED

```
    Minute 2 (Team 1: 1 | Team 2: 0)
    WINNING
    Minute 3 (Team 1: 1 | Team 2: 1)
    TIED
    Minute 4 (Team 1: 1 | Team 2: 2)
    LOSING
```

Game Score (Atomic) - Formal Specification

```
Game Score = \langle X, Y, S, \delta_{int}, \delta_{ext}, \lambda, t_a \rangle
X = \{\text{team 1 score} \in \mathbb{N}, \text{team 2 score} \in \mathbb{N}\}\
Y = \{game state \in \{WINNING, LOSING, TIED\}\}\
S = \{\text{team 1 score} \in \mathbb{N}, \text{ team 2 score} \in \mathbb{N}, \text{ game state} \in \{\text{WINNING,LOSING,TIED}\},
sigma \in \mathbb{R}^+
\delta_{int}(s) = \{
         sigma = 1.0
         return *this
}
\delta_{\rm ext}(s, e, x) = \{
         if not empty(x.team 1 score):
                 team 1 score = get_team_1_score(x.team_1_score)
         if not empty(x.team 2 score):
                 team_2_score = get_team_2_score(x.team_2_score)
         if team 1 score > team 2 score:
                  game state = WINNING
         elif team 1 score < team 2 score:
                 game state = LOSING
         else:
                 game state = TIED
         sigma -= e
         return *this
}
\lambda(s) = \{
         return game state
}
```

```
\begin{array}{c} t_a(s) \colon \{ \\ & \text{return sigma} \\ \} \end{array}
```

Substitution Logic - Behavior

Substitution Command

- **Definition:** determines when to substitute players based on their metrics (fatigue, mental, time played, time on bench) and the current game state
 - o player_out_id: id of the player being subbed out (goes to bench)
 - o player in id: id of the player being subbed in (goes to field)
- **How it works:** uses weighted decision making, each metric is normalized and then assigned a weight. Based on the game state (WINNING, LOSING, TIED), the weights and substitution threshold dynamically change
 - Field Players:
 - Metrics and Normalization:
 - Fatigue:
 - o Range: 0 to 100
 - o Normalization: fatigue/100
 - \blacksquare 1 = maximum fatigue
 - Mental:
 - o Range: 0 to 100
 - o Normalization: (mental 100)/100
 - \blacksquare 1 = maximum stress
 - Time played:
 - Range: 0 to ∞
 - Normalization: tanh(time played/scaling factor)
 - Asymptotic to 1 as it increases based on scaling factor
 - Scaling factor changes based on the type of game
 - Ex: soccer (90/45 minutes) or basketball (48/12 minutes)
 - Time on bench:
 - \circ Range: 0 to ∞
 - Normalization: must pass minimum rest period
 - Time on bench > minimum rest → eligible for substitution
 - Dynamic Weights and Thresholds for Field Players:
 - Baseline threshold: 1.5
 - Losing: $1.5 \rightarrow 1.2$

 $\circ \quad \text{Tied: } 1.5 \rightarrow 1.5$

 \circ Winning: $1.5 \rightarrow 1.8$

| Game State | Fatigue Weight | Mental Weight | Time Played Weight | Threshold |
|------------|----------------|---------------|--------------------|----------------------|
| Losing | 1.2x | 1.5x | 1.1x | -20% (easier to sub) |
| Tied | 1x | 1x | 1x | Baseline |
| Winning | 1.2x | 0.7x | 1x | +20% (harder to sub) |

- o Bench Players:
 - **■** Thresholds:
 - Fatigue must be below 40
 - Mental must be at least 60
 - Time on bench must be at least 10
- How it changes: δ_{ext}
 - Updates player metrics/game state when receiving inputs at the state level
- How it changes: δ_{int}
 - No internal event occurs
- Example 1:
 - o Game State: LOSING
 - Weights: 1.2x fatigue, 1.5x mental, 1.1x time played
 - Player 1 Metrics (ON FIELD):
 - Mental: 60
 - Normalized: (100-60)/100 = 0.4
 - Fatigue: 40
 - Normalized: 40/100 = 0.4
 - Time Played: 20
 - Normalized: tanh(20/45) = 0.417
 - Time on Bench: 0
 - Normalized: $N/A \rightarrow field player$
 - Score: 1.2(0.4) + 1.5(0.4) + 1.1(0.417) = 1.5387 > 1.2 (threshold) \rightarrow can be substituted out
 - Player 2 Metrics (ON BENCH):
 - Mental: 80
 - 80 >= 60 (mental threshold for bench player)
 - Fatigue: 10
 - 10 <= 40 (fatigue threshold for bench player)
 - Time Played: 0
 - $N/A \rightarrow bench player$
 - Time on Bench: 20

- 20 >= 10 (bench time threshold for bench player)
- **Passes all checks** \rightarrow can be substituted in
- \circ **Both players pass** \rightarrow can make the substitution
 - Player 1 OUT
 - Player 2 IN
- Example 2:
 - o Game State: WINNING
 - Weights: 1.2x fatigue, 0.7x mental, 1x time played
 - Player 1 Metrics (ON BENCH):
 - Mental: 80
 - $80 \ge 60$ (mental threshold for bench player)
 - Fatigue: 20
 - 20 <= 40 (fatigue threshold for bench player)
 - Time Played: 20
 - $N/A \rightarrow bench player$
 - Time on Bench: 30
 - 30 >= 10 (bench time threshold for bench player)
 - **Passes all checks** \rightarrow can be substituted in
 - Player 2 Metrics (ON FIELD):
 - Mental: 40
 - Normalized: (100-40)/100 = 0.6
 - Fatigue: 70
 - Normalized: 70/100 = 0.7
 - Time Played: 30
 - Normalized: tanh(30/45) = 0.5827
 - Time on Bench: 0
 - Normalized: $N/A \rightarrow field player$
 - Score: 1.2(0.7) + 0.7(0.6) + 1(0.5827) = 1.8417 > 1.8 (threshold) \rightarrow can be substituted out
 - \circ **Both players pass** \rightarrow can make the substitution
 - Player 1 IN
 - Player 2 OUT

Substitution Logic (Atomic) - Formal Specification

Substitution Logic = $\langle X, Y, S, \delta_{int}, \delta_{ext}, \lambda, t_a \rangle$ $X = \{(player_id \in \mathbb{N}, mental \in [0,100], fatigue \in [0,100], phase \in \{ON_FIELD, ON_BENCH\}, time_played \in \mathbb{R}^+, time_on_bench \in \mathbb{R}^+), (player_id \in \mathbb{N}, mental \in [0,100], fatigue \in [0,100], phase \in \{ON_FIELD, ON_BENCH\}, time_played \in \mathbb{R}^+, time_on_bench \in \mathbb{R}^+), game state \in \{WINNING,LOSING,TIED\}\}$

```
Y = \{(player out id \in \mathbb{N}, player in id \in \mathbb{N})\}\
S = {(player id, mental, fatigue, phase, time played, time on bench), (player id, mental,
fatigue, phase, time played, time on bench), game state ∈ {WINNING,LOSING,TIED},
sigma \in \mathbb{R}^+
\delta_{int}(s) = \{
       sigma = 1.0
       return *this;
\delta_{\rm ext}(s, e, x) = \{
       if not empty(x.players):
               player 1 metrics, state.player 2 metrics = get player metrics(x.players)
       if not empty(x.game state):
               game state = get_game_state(x.game_state)
       state.sigma -= e
       return *this
}
\lambda(s) = \{
       weights = getWeights(game state)
       threshold = getThreshold(game state)
       if player 1 metrics.phase == BENCH:
               bench ready = checkIfBenchPlayerReady(player 1 metrics)
               norm metrics = normalizePlayerMetrics(player 2 metrics)
               score = calculateScore(norm metrics, weights)
               if (score > threshold and bench ready):
                      return {
                              player out id = player 2.id,
                              player in id = player 1.id
       elif player 2.metrics.phase == BENCH:
               bench ready = checkIfBenchPlayerReady(player 2 metrics)
               norm metrics = normalizePlayerMetrics(player 1 metrics)
               score = calculateScore(norm metrics, weights)
               if (score > threshold and bench ready):
                      return {
                              player out id = player 1.id,
```

```
player in id = player 2.id
       return None
}
t_a(s): {
       return sigma
}
Team (Coupled) - Formal Specification
Team = \langle X, Y, M, EIC, EOC, IC, select \rangle
X = \{(player out id \in \mathbb{N}, player in id \in \mathbb{N}), game state \in \{WINNING, LOSING, TIED\}\}
Y = \{(player id \in \mathbb{N}, mental \in [0,100], fatigue \in [0,100], phase \in \{ON FIELD, \}\}
ON BENCH, time played \in \mathbb{R}^+, time on bench \in \mathbb{R}^+), (player id \in \mathbb{N}, mental \in [0,100],
fatigue \in [0,100], phase \in {ON FIELD, ON BENCH}, time played \in \mathbb{R}^+, time on bench \in
\mathbb{R}^+)}
M = \{Player1, Player2\}
EIC = {(self.(player out id, player in id), Player1.(player out id, player in id)),
(self.(player out id, player in id), Player2.(player out id, player in id)), (self.game state,
Player1.game state), (self.game state, Player2.game state)}
EOC = {(Player1.(player id, mental, fatigue, phase, time played, time on bench),
self.(player id, mental, fatigue, phase, time played, time on bench)), (Player2.(player id,
mental, fatigue, phase, time played, time on bench), self.(player id, mental, fatigue, phase,
time played, time on bench))}
IC = \emptyset
Coach (Coupled) - Top Level - Formal Specification
Coach = <X, Y, M, EIC, EOC, IC, select>
X = \emptyset
Y = \emptyset
M = {GameScore, Team, SubstitutionLogic}
EIC = \emptyset
EOC = \emptyset
IC = {(GameScore.game state, SubstitutionLogic.game state), (GameScore.game state,
Team.game state), (Team.Player1.(player id, mental, fatigue, phase, time played,
time on bench), SubstitutionLogic.(player id, mental, fatigue, phase, time played,
time on bench)), (Team.Player2.(player id, mental, fatigue, phase, time played,
time on bench), SubstitutionLogic.(player id, mental, fatigue, phase, time played,
time on bench)), (SubstitutionLogic.(player out id, player in id), Team.(player out id,
player in id))}
```

PART III - Testing Strategies and Documentation

Updated Sketch of Model Structure

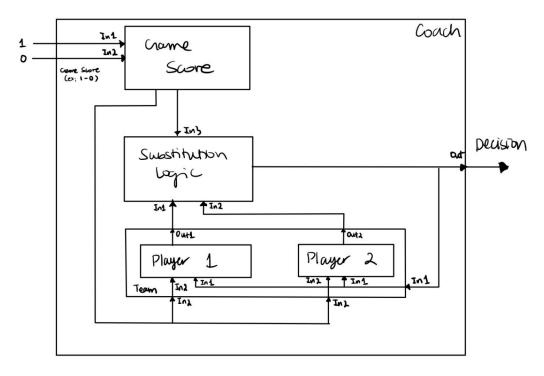


Figure 2: Updated Sketch of Coach Model

Compared to the original sketch of the coach model structure, the team coupled model now has an external output coupling with the **Player** model and receives an additional external input from the **GameScore** model. This was done to ensure that Players receive *game_state* updates, which could play a factor in influencing their mental levels.

Atomic Model Validation

For each of the following atomic models, testing was done by feeding each model's input a .txt file that followed closely the examples proposed in Part II of the report. Each atomic component was treated as a black box, and test cases were created with different inputs to check their correctness. If the observed output matches the expected results, then the atomic model is validated.

GameScore

Given team 1 and team 2's score, this component should output a state accordingly (WINNING, LOSING, or TIED). Note that the model favors team 1.

team_1_score_test.txt

```
0.0 0

1.0 0

2.0 1

3.0 1

4.0 1

team_2_score_test.txt

0.0 0

1.0 0

2.0 0

3.0 1

4.0 2
```

Expected:

- Time 1: TIED
- Time 2: WINNING
- Time 3: TIED
- Time 4: LOSING

Observed:

```
0;3;game_score_model;;{game state: TIED, team 1 score: 0, team 2 score: 0}
1;3;game_score_model;;{game state: TIED, team 1 score: 0, team 2 score: 0}
2;3;game_score_model;;{game state: WINNING, team 1 score: 1, team 2 score: 0}
3;3;game_score_model;;{game state: TIED, team 1 score: 1, team 2 score: 1}
4;3;game_score_model;;{game state: LOSING, team 1 score: 1, team 2 score: 2}
```

The observed matches the expected $\Rightarrow \bigvee$

Player

Given game state and substitution command inputs, player metrics should fluctuate accordingly to the proposed behavior in Part II.

```
game_state_test.txt
0.0 2
30.0 1
50.0 0
substitution_test.txt
20 1 2
26 2 1
51 1 2
```

Expected:

- At minute 0 and onwards:
 - \circ **Fatigue** \rightarrow increases by +1.5 per time unit
 - o **Mental** → unaffected (initial game state, TIED, has no effect)
 - \circ Time played \rightarrow increases by +1 per time unit
 - **Time bench** \rightarrow stays 0
- At minute 20 (player gets substituted out):
 - \circ **Fatigue** \rightarrow decreases by -1. per time unit
 - \circ **Mental** \rightarrow remains constant (max 100)
 - \circ Time played \rightarrow remains constant
 - \circ Time bench \rightarrow increases by +1 per time unit
- At minute 26 (player gets substituted back in):
 - \circ **Fatigue** \rightarrow increases again by +1.5 per time unit
 - \circ **Mental** \rightarrow remains constant
 - \circ Time played \rightarrow increases again by +1 per time unit
 - \circ Time bench \rightarrow resets to 0
- At minute 30 (game state changes from TIED to LOSING):
 - \circ Fatigue \rightarrow keeps increasing by +1.5 per time unit
 - \circ Mental \rightarrow starts decreasing by -2 per time unit
 - \circ Time played \rightarrow keeps increasing by +1 per time unit
 - **Time bench** \rightarrow remains 0
- At minute 50 (game state change from LOSING to WINNING):
 - \circ **Fatigue** \rightarrow keeps increasing by +1.5 per time unit
 - \circ Mental \rightarrow starts increasing by +2 per time unit
 - \circ Time played \rightarrow keeps increasing by +1 per time unit
 - **Time bench** \rightarrow remains 0
- At minute 51, player gets substituted out. Onwards, we should expect:
 - \circ **Fatigue** \rightarrow starts decreasing by -1 per time unit
 - \circ Mental \rightarrow starts increasing by +1 per time unit
 - \circ Time played \rightarrow remains constant
 - \circ Time bench \rightarrow starts increasing by +1 per time unit

Observed:

```
0;3;player_model;;{player_id:1, game state: TIED, mental: 100, fatigue: 0, phase: ON_FIELD, time played: 0, time on bench: 0}
```

1;3;player_model;;{player_id:1, game state: TIED, mental: 100, fatigue: 1.5, phase: ON_FIELD, time played: 1, time on bench: 0}

```
2;3;player model;;{player id:1, game state: TIED, mental: 100, fatigue: 3, phase: ON FIELD,
time played: 2, time on bench: 0}
3;3;player model;;{player id:1, game state: TIED, mental: 100, fatigue: 4.5, phase: ON FIELD,
time played: 3, time on bench: 0}
4;3;player model;;{player id:1, game state: TIED, mental: 100, fatigue: 6, phase: ON FIELD,
time played: 4, time on bench: 0}
5;3;player model;;{player id:1, game state: TIED, mental: 100, fatigue: 7.5, phase: ON FIELD,
time played: 5, time on bench: 0}
6;3;player model;;{player id:1, game state: TIED, mental: 100, fatigue: 9, phase: ON FIELD,
time played: 6, time on bench: 0}
7;3;player model;;{player id:1, game state: TIED, mental: 100, fatigue: 10.5, phase:
ON FIELD, time played: 7, time on bench: 0}
8;3;player model;;{player id:1, game state: TIED, mental: 100, fatigue: 12, phase: ON FIELD,
time played: 8, time on bench: 0}
9;3;player model;;{player id:1, game state: TIED, mental: 100, fatigue: 13.5, phase:
ON FIELD, time played: 9, time on bench: 0}
10;3;player model;;{player id:1, game state: TIED, mental: 100, fatigue: 15, phase:
ON FIELD, time played: 10, time on bench: 0}
11;3;player model;;{player id:1, game state: TIED, mental: 100, fatigue: 16.5, phase:
ON FIELD, time played: 11, time on bench: 0}
12;3;player model;;{player id:1, game state: TIED, mental: 100, fatigue: 18, phase:
ON FIELD, time played: 12, time on bench: 0}
13;3;player model;;{player id:1, game state: TIED, mental: 100, fatigue: 19.5, phase:
ON FIELD, time played: 13, time on bench: 0}
14;3;player model;;{player id:1, game state: TIED, mental: 100, fatigue: 21, phase:
ON FIELD, time played: 14, time on bench: 0}
15;3;player model;;{player id:1, game state: TIED, mental: 100, fatigue: 22.5, phase:
ON FIELD, time played: 15, time on bench: 0}
16;3;player model;;{player id:1, game state: TIED, mental: 100, fatigue: 24, phase:
ON FIELD, time played: 16, time on bench: 0}
17;3;player model;;{player id:1, game state: TIED, mental: 100, fatigue: 25.5, phase:
ON FIELD, time played: 17, time on bench: 0}
18;3;player model;;{player id:1, game state: TIED, mental: 100, fatigue: 27, phase:
ON FIELD, time played: 18, time on bench: 0}
19;3;player model;;{player id:1, game state: TIED, mental: 100, fatigue: 28.5, phase:
ON FIELD, time played: 19, time on bench: 0}
20;2;substitution file;out;{player out id: 1, player in id: 2}
20;2;substitution file;;6
20;3;player model;;{player id:1, game state: TIED, mental: 100, fatigue: 30, phase:
ON BENCH, time played: 20, time on bench: 0}
```

```
21;3;player model;;{player id:1, game state: TIED, mental: 100, fatigue: 29, phase:
ON BENCH, time played: 20, time on bench: 1}
22;3;player model;:{player id:1, game state: TIED, mental: 100, fatigue: 28, phase:
ON BENCH, time played: 20, time on bench: 2}
23;3;player model;;{player id:1, game state: TIED, mental: 100, fatigue: 27, phase:
ON BENCH, time played: 20, time on bench: 3}
24;3;player model;;{player id:1, game state: TIED, mental: 100, fatigue: 26, phase:
ON BENCH, time played: 20, time on bench: 4}
25;3;player model;;{player id:1, game state: TIED, mental: 100, fatigue: 25, phase:
ON BENCH, time played: 20, time on bench: 5}
26;2;substitution file;out;{player out id: 2, player in id: 1}
26;2;substitution file;;25
26;3;player model;;{player id:1, game state: TIED, mental: 100, fatigue: 24, phase:
ON FIELD, time played: 20, time on bench: 0}
27;3;player model;;{player id:1, game state: TIED, mental: 100, fatigue: 25.5, phase:
ON FIELD, time played: 21, time on bench: 0}
28;3;player model;;{player id:1, game state: TIED, mental: 100, fatigue: 27, phase:
ON FIELD, time played: 22, time on bench: 0}
29;3;player model;;{player id:1, game state: TIED, mental: 100, fatigue: 28.5, phase:
ON_FIELD, time played: 23, time on bench: 0}
30;1;game state file;out;LOSING
30;1;game state file;;20
30;3;player model;;{player id:1, game state: LOSING, mental: 100, fatigue: 30, phase:
ON FIELD, time played: 24, time on bench: 0}
31;3;player model;;{player id:1, game state: LOSING, mental: 98, fatigue: 31.5, phase:
ON FIELD, time played: 25, time on bench: 0}
32;3;player model;;{player id:1, game state: LOSING, mental: 96, fatigue: 33, phase:
ON FIELD, time played: 26, time on bench: 0}
33;3;player model;;{player id:1, game state: LOSING, mental: 94, fatigue: 34.5, phase:
ON FIELD, time played: 27, time on bench: 0}
34;3;player model;;{player id:1, game state: LOSING, mental: 92, fatigue: 36, phase:
ON FIELD, time played: 28, time on bench: 0}
35;3;player model;;{player id:1, game state: LOSING, mental: 90, fatigue: 37.5, phase:
ON FIELD, time played: 29, time on bench: 0}
36;3;player model;;{player id:1, game state: LOSING, mental: 88, fatigue: 39, phase:
ON FIELD, time played: 30, time on bench: 0}
37;3;player model;;{player id:1, game state: LOSING, mental: 86, fatigue: 40.5, phase:
ON FIELD, time played: 31, time on bench: 0}
38;3;player model;;{player id:1, game state: LOSING, mental: 84, fatigue: 42, phase:
ON FIELD, time played: 32, time on bench: 0}
```

```
39;3;player model;;{player id:1, game state: LOSING, mental: 82, fatigue: 43.5, phase:
ON FIELD, time played: 33, time on bench: 0}
40;3;player model;:{player id:1, game state: LOSING, mental: 80, fatigue: 45, phase:
ON FIELD, time played: 34, time on bench: 0}
41;3;player model;;{player id:1, game state: LOSING, mental: 78, fatigue: 46.5, phase:
ON FIELD, time played: 35, time on bench: 0}
42;3;player model;;{player id:1, game state: LOSING, mental: 76, fatigue: 48, phase:
ON FIELD, time played: 36, time on bench: 0}
43;3;player model;;{player id:1, game state: LOSING, mental: 74, fatigue: 49.5, phase:
ON FIELD, time played: 37, time on bench: 0}
44;3;player model;;{player id:1, game state: LOSING, mental: 72, fatigue: 51, phase:
ON FIELD, time played: 38, time on bench: 0}
45;3;player model;;{player id:1, game state: LOSING, mental: 70, fatigue: 52.5, phase:
ON_FIELD, time played: 39, time on bench: 0}
46;3;player model;;{player id:1, game state: LOSING, mental: 68, fatigue: 54, phase:
ON FIELD, time played: 40, time on bench: 0}
47;3;player model;;{player id:1, game state: LOSING, mental: 66, fatigue: 55.5, phase:
ON FIELD, time played: 41, time on bench: 0}
48;3;player model;;{player id:1, game state: LOSING, mental: 64, fatigue: 57, phase:
ON_FIELD, time played: 42, time on bench: 0}
49;3;player model;;{player id:1, game state: LOSING, mental: 62, fatigue: 58.5, phase:
ON FIELD, time played: 43, time on bench: 0}
50;1;game state file;out;WINNING
50;1;game state file;;inf
50;3;player model;;{player id:1, game state: WINNING, mental: 60, fatigue: 60, phase:
ON FIELD, time played: 44, time on bench: 0}
51;2;substitution file;out;{player out id: 1, player in id: 2}
51;2;substitution file;;inf
51;3;player model;;{player id:1, game state: WINNING, mental: 62, fatigue: 61.5, phase:
ON BENCH, time played: 45, time on bench: 0}
52;3;player model;;{player id:1, game state: WINNING, mental: 63, fatigue: 60.5, phase:
ON BENCH, time played: 45, time on bench: 1}
53;3;player model;;{player id:1, game state: WINNING, mental: 64, fatigue: 59.5, phase:
ON BENCH, time played: 45, time on bench: 2}
54;3;player model;;{player id:1, game state: WINNING, mental: 65, fatigue: 58.5, phase:
ON BENCH, time played: 45, time on bench: 3}
55;3;player model;;{player id:1, game state: WINNING, mental: 66, fatigue: 57.5, phase:
ON BENCH, time played: 45, time on bench: 4}
56;3;player model;;{player id:1, game state: WINNING, mental: 67, fatigue: 56.5, phase:
ON BENCH, time played: 45, time on bench: 5}
```

```
57;3;player_model;;{player_id:1, game state: WINNING, mental: 68, fatigue: 55.5, phase: ON_BENCH, time played: 45, time on bench: 6}
58;3;player_model;;{player_id:1, game state: WINNING, mental: 69, fatigue: 54.5, phase: ON_BENCH, time played: 45, time on bench: 7}
59;3;player_model;;{player_id:1, game state: WINNING, mental: 70, fatigue: 53.5, phase: ON_BENCH, time played: 45, time on bench: 8}
60;3;player_model;;{player_id:1, game state: WINNING, mental: 71, fatigue: 52.5, phase: ON_BENCH, time played: 45, time on bench: 9}
```

The observed matches the expected $\Rightarrow \bigvee$

SubstitutionLogic

Given two player metrics .txt files, the substitution will use threshold/weighted decision making to evaluate whether a substitution will be made. Weights will vary based on the game state input .txt file. The expected behavior should mimic the logic proposed in Part II.

```
game_state_test.txt
20.0 1
30.0 2
50.0 0

player_1_test.txt
20.0 1 60.0 40.0 0 20.0 0.0
30.0 1 70.0 30.0 1 20.0 10.0
50.0 1 80.0 20.0 1 20.0 30.0

player_2_test.txt
20.0 2 80.0 10.0 1 0.0 20.0
30.0 2 40.0 75.0 0 10.0 0.0
50.0 2 40.0 70.0 0 30.0 0.0
```

Expected:

• Minute 20:

o Game State: LOSING

■ Weights: 1.2x fatigue, 1.5x mental, 1.1x time played

■ Threshold: 1.2

• Player 1 Metrics (ON FIELD):

■ Mental: $60 \rightarrow (100-60)/100 = 0.4$

■ Fatigue: $40 \rightarrow 40/100 = 0.4$

■ Time Played: $20 \rightarrow \tanh(20/45) = 0.417$

- Time on Bench: $0 \rightarrow N/A$ (field player)
- Score: 1.2(0.4) + 1.5(0.4) + 1.1(0.417) = 1.5387 > 1.2 ✓
- Passes threshold \rightarrow can be substituted out
- Player 2 Metrics (ON BENCH):
 - Mental: $80 \rightarrow 80 \ge 60$ ✓
 - Fatigue: $10 \rightarrow 10 \le 40$ ✓
 - Time Played: $0 \rightarrow N/A$ (bench player)
 - Time on Bench: $20 \rightarrow 20 \ge 10$
 - Passes all checks \rightarrow can be substituted in
- \circ **Both players pass** \rightarrow can make the substitution
 - Player 1 OUT
 - Player 2 IN
- **Minute 30:**
 - o Game State: TIED
 - Weights: 1x fatigue, 1x mental, 1x time played
 - Threshold: 1.5
 - Player 1 Metrics (ON BENCH):
 - Mental: $70 \rightarrow 70 >= 60$ ✓
 - Fatigue: $30 \rightarrow 30 \le 40$ ✓
 - Time Played: $20 \rightarrow N/A$ (bench player)
 - Time on Bench: $10 \rightarrow 10 \ge 10$
 - **Passes all checks** \rightarrow can be substituted in
 - Player 2 Metrics (ON FIELD):
 - Mental: $40 \rightarrow (100-40)/100 = 0.6$
 - Fatigue: $75 \rightarrow 75/100 = 0.75$
 - Time Played: $10 \rightarrow \tanh(10/45) = 0.2186$
 - Time on Bench: $0 \rightarrow N/A$ (field player)
 - Score: 1(0.75) + 1(0.6) + 1(0.2186) = 1.5686 > 1.5 ✓
 - Passes threshold \rightarrow can be substituted out
 - \circ Both players pass \rightarrow can make the substitution
 - Player 1 IN
 - Player 2 OUT
- Minute 50:
 - Game State: WINNING
 - Weights: 1.2x fatigue, 0.7x mental, 1x time played
 - Threshold: 1.8
 - Player 1 Metrics (ON BENCH):
 - Mental: $80 \to 80 \ge 60$ ✓
 - Fatigue: $20 \rightarrow 20 \le 40$ ✓
 - Time Played: $20 \rightarrow N/A$ (bench player)

- Time on Bench: $30 \rightarrow 30 \ge 10$
- Passes all checks \rightarrow can be substituted in
- Player 2 Metrics (ON FIELD):
 - Mental: $40 \rightarrow (100-40)/100 = 0.6$
 - Fatigue: $70 \rightarrow 70/100 = 0.7$
 - Time Played: $30 \rightarrow \tanh(30/45) = 0.5827$
 - Time on Bench: $0 \rightarrow N/A$ (field player)
 - **Score:** 1.2(0.7) + 0.7(0.6) + 1(0.5827) = 1.8417 > 1.8
 - Passes threshold \rightarrow can be substituted out
- \circ **Both players pass** \rightarrow can make the substitution
 - Player 1 IN
 - Player 2 OUT

Observed:

```
0;4;substitution logic model;;{game state: TIED, player 1: {player id:0, mental: 100, fatigue: 0,
phase: ON BENCH, time played: 0, time on bench: 0}, player 2: {player id:0, mental: 100,
fatigue: 0, phase: ON BENCH, time played: 0, time on bench: 0}}
1;4;substitution logic model;;{game state: TIED, player 1: {player id:0, mental: 100, fatigue: 0,
phase: ON BENCH, time played: 0, time on bench: 0}, player 2: {player id:0, mental: 100,
fatigue: 0, phase: ON BENCH, time played: 0, time on bench: 0}}
20;1;game state file;out;LOSING
20;2;player 2 file;out;{player id:2, mental: 80, fatigue: 10, phase: ON BENCH, time played: 0,
time on bench: 20}
20;3; player 1 file; out; {player id:1, mental: 60, fatigue: 40, phase: ON FIELD, time played: 20,
time on bench: 0}
20;4; substitution logic model;; {game state: LOSING, player 1: {player id:1, mental: 60,
fatigue: 40, phase: ON FIELD, time played: 20, time on bench: 0}, player 2: {player id:2,
mental: 80, fatigue: 10, phase: ON BENCH, time played: 0, time on bench: 20}}
21;4;substitution logic model;substitution out;{player out id: 1, player in id: 2}
30;1;game state file;out;TIED
30;2;player 2 file;out;{player id:2, mental: 40, fatigue: 75, phase: ON FIELD, time played: 10,
time on bench: 0}
30;3;player 1 file;out;{player id:1, mental: 70, fatigue: 30, phase: ON BENCH, time played:
20, time on bench: 10}
```

```
30;4;substitution_logic_model;;{game state: TIED, player 1: {player_id:1, mental: 70, fatigue: 30, phase: ON_BENCH, time played: 20, time on bench: 10}, player 2: {player_id:2, mental: 40, fatigue: 75, phase: ON_FIELD, time played: 10, time on bench: 0}} 31;4;substitution_logic_model;substitution_out;{player_out_id: 2, player_in_id: 1}} .

50;1;game_state_file;out; {player_id:2, mental: 40, fatigue: 70, phase: ON_FIELD, time played: 30, time on bench: 0} 50;3;player_1_file;out; {player_id:1, mental: 80, fatigue: 20, phase: ON_BENCH, time played: 20, time on bench: 30} 50;4;substitution_logic_model;;{game state: WINNING, player 1: {player_id:1, mental: 80, fatigue: 20, phase: ON_BENCH, time played: 20, time on bench: 30}, player 2: {player_id:2, mental: 40, fatigue: 70, phase: ON_FIELD, time played: 30, time on bench: 0}} 51;4;substitution_logic_model;substitution_out;{player_out_id: 2, player_in_id: 1}}
```

The observed matches the expected $\Rightarrow \bigvee$

Coupled Model Integration Testing

For **Team** and **Coach** coupled models, integration testing was done at the top level to ensure that all atomic components worked together correctly. The focus was on verifying:

- Each atomic component's output matched expected behavior
- State updates between models (internal coupling) as inputs were correctly propagated
- All atomic components received inputs without any unintended overrides or unexpected behavior

One key issue identified was the lack of an atomic component tp generate scores for both teams. To address this, external input .txt files were used for simulation purposes.

```
team_1_score_test.txt
0.0 0
20.0 0
30.0 0
50.0 2
team_2_score_test.txt
0.0 0
20.0 1
30.0 1
50.0 1
```

Verification

To verify the correctness of the Player Substitution System:

- Clone the project from github
- Compile and run the simulation
- Compare the output logs/CSV file against expected behavior outlined above

Link to the repository

https://github.com/yelfaram/Cadmium-Player-Substitution-System