# Homework 8 - Graphs

## Problem 1:

What is the big-Oh space complexity of an adjacency list? Justify your answer.

**ANS**

Assume that the number of vertices of a graph is ***n****,* and there are ***e*** edges in it. For an adjacency list, the big-Oh space complexity is *.*

We use the adjacency list to represent a graph, which means each node in the graph are stored in a Double Linked List, and for each node storing a list of its neighbors

First for each node of graph, the big-Oh space complexity is . Then,

for undirected graph every edge is stored in DLL for twice, while for directed graph every edge is stored in DLL for once.

The largest number of edges is *2E, which* *.* Thus, for a graph representing by an adjacency list, the big-Oh space complexity is *.*

## Problem 2:

What is the big-Oh space complexity of an adjacency matrix? Justify your answer.

**ANS**

For each vertex, it takes n blocks of space, and its [adjacency matrix](https://en.wikipedia.org/wiki/Adjacency_matrix" \t "https://northeastern.instructure.com/courses/96512/assignments/_blank) takes blocks of space to represent all of the relationships given.

Therefore, given n nodes, the total space required by the adjacency matrix is

The space complexity in Big-O is *.*

Notice that undirected [adjacency matrix](https://en.wikipedia.org/wiki/Adjacency_matrix" \t "https://northeastern.instructure.com/courses/96512/assignments/_blank) is [symmetrical](E:/Dict/8.9.9.0/resultui/html/index.html" \l "/javascript:;), one of its diagonals from left top to right bottom is always zero, so it takesblocks of space to represent all of the relationships given. The Big-O is also.

## Problem 3:

What is the big-Oh time complexity for searching an entire graph using *depth-first search* (DFS)? Does the representation of the graph make a difference? Justify your answer.

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**ANS**

Assume that the number of vertices of a graph is ***n****,* and there are ***e*** edges in it.

When traversing the graph using DFS, for each node we only invoke the DFS function once. It is because once a node has already been visited and marked, we won’t search from it again. For each node *x,* we consider all other nodes *y* which *x* has directed-edges in to.

If the representation of the graph is *an adjacency list,* the big-Oh time complexity for searching an entire graph is

If the representation of the graph is *an adjacency matrix,*the big-Oh time complexity for searching an entire graph is

## Problem 4:

What is the big-Oh time complexity for searching an entire graph using *breadth-first search* (BFS)? Does the representation of the graph make a difference? Justify your answer.

**ANS**

Assume that the number of vertices of a graph is ***n****,* and there are ***e*** edges in it.

BFS is a procedure that borrows queues for storage, looking up hierarchically. When traversing the graph using BFS, we will only push each node in the queue for once. For each node *x,* we consider all other nodes *y* which *x* has directed-edges in to, once a node has already been visited and marked, we won’t search from it again.

The BFS have a different order for visiting nodes with DFS, it will access to points close to the starting point first. So the big-Oh time complexity is same as DFS.

If the representation of the graph is *an adjacency list,* the big-Oh time complexity for searching an entire graph is

If the representation of the graph is *an adjacency matrix,* the big-Oh time complexity for searching an entire graph is