

## EXERCISE 4

MAT260, SPRING 2017

**Problem 1.** Exercise 3.5 from the textbook.

**Problem 2.** Exercise 3.6 from the textbook.

**Problem 3.** Exercise 3.8 from the textbook.

**Problem 4.** The damped pendulum equation for a cord of length 1 reads

$$(1) \quad \theta'' + \alpha\theta' + g \sin \theta = 0$$

where  $\alpha > 0$  is the damping constant and  $g$  the gravitational constant.

**a):** Write it as a system of  $2 \times 2$  and find its Jacobian

**b):** Discuss the stiffness of the system. ( $\theta$  is the angle between the cord and the vertical line, and we assume it is in the interval  $[-\pi/2, \pi/2]$ ).