

Implementation exercises for the course Heuristic Optimization

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Exercise 1.1: Iterative Improvement for the LOP

Goal: Implement perturbative local search algorithms for the LOP

- 1 Linear Ordering Problem (LOP)
- 2 First-improvement and Best-Improvement
- 3 Transpose, exchange and insert neighborhoods
- 4 Random initialization vs. CW heuristic
- 5 Statistical Empirical Analysis

The Linear Ordering Problem (1/3)



- *Ranking in sport tournaments*: establishing the order in which criteria such as wins, losses, draws, points scored, goals scored, or head-to-head results should be considered
- *Archeology*: establishing a chronological sequence of events or cultural phases based on the relative ordering of archaeological artifacts
- *Economics*: triangularization of input-output matrices allow to establish the interdependencies between different sectors of an economy
- etc.

Linear Ordering Problem (2/3)

Given

An $n \times n$ matrix C , where the value of row i and column j is noted c_{ij} .

	1	2	3	4
1	c_{11}	c_{12}	c_{13}	c_{14}
2	c_{21}	c_{22}	c_{23}	c_{24}
3	c_{31}	c_{32}	c_{33}	c_{34}
4	c_{41}	c_{42}	c_{43}	c_{44}

Objective

Find a permutation π of the column and row indices $\{1, \dots, n\}$ such that the value $f(\pi) = \sum_{i=1}^n \sum_{j=i+1}^n c_{\pi(i)\pi(j)}$ is maximized.

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Linear Ordering Problem example (3/3)

$$\pi = (1, 2, 3, 4) \quad C = \begin{array}{c|cccc} & 1 & 2 & 3 & 4 \\ \hline 1 & 1 & 3 & 2 & 4 \\ 2 & 2 & 1 & 1 & 3 \\ 3 & 1 & 2 & 2 & 1 \\ 4 & 4 & 5 & 1 & 4 \end{array}$$

$$f(\pi) = 3 + 2 + 4 + 1 + 3 + 1 = 14$$

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Implement 12 iterative improvements algorithms for the LOP

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- Pivoting rule:
 - ① first-improvement
 - ② best-improvement
- Neighborhood:
 - ① Transpose
 - ② Exchange
 - ③ Insert
- Initial solution:
 - ① Random permutation
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2 pivoting rules \times 3 neighborhoods \times 2 initialization methods =
12 combinations

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Implement 12 iterative improvements algorithms for the LOP

Do not implement 12 programs!

Reuse code and use command-line parameters

```
./lop11 --first --transpose --cw  
./lop11 --best --exchange --random  
etc.
```

Use a parameter to choose the instance file, for instance:

```
./lop11 -i <instance_file>
```

Exercise 1.1: Iterative Improvement for the LOP

Iterative Improvement

```
 $\pi := \text{GenerateInitialSolution}()$ 
```

```
while  $\pi$  is not a local optimum do
```

```
    choose a neighbour  $\pi' \in \mathcal{N}(\pi)$  such that  $F(\pi') < F(\pi)$ 
```

```
     $\pi := \pi'$ 
```

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Iterative Improvement

$\pi := \text{GenerateInitialSolution}()$

while π is not a local optimum **do**

 choose a neighbour $\pi' \in \mathcal{N}(\pi)$ such that $F(\pi') < F(\pi)$

$\pi := \pi'$

Which neighbour to choose? Pivoting rule

- **Best Improvement:** choose best from all neighbours of π
 - ✓ Better quality
 - ✗ Requires evaluation of all neighbours in each step
- **First improvement:** evaluate neighbours in fixed order and choose first improving neighbour.
 - ✓ More efficient
 - ✗ Order of evaluation may impact quality / performance

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Initial solution

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Chenery and Watanabe (CW) heuristic

Construct the solution by inserting **one row at a time**, always selecting the most “attractive” row: the one that maximizes the sum of elements having an influence on objective function.

The “attractiveness” of a row i at step s is: $\sum_{j=s+1}^n c_{\pi(i)j}$

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while π is not a local optimum **do**

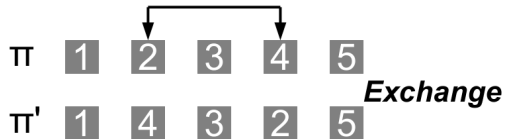
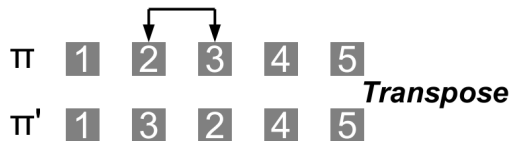
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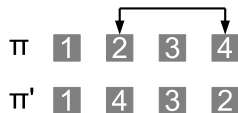
Which neighborhood $\mathcal{N}(\pi)$?

- Transpose
- Exchange
- Insertion

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Example: Exchange π_i and π_j ($i \neq j$), $\pi' = \text{Exchange}(\pi, i, j)$

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$\pi =$	1	2	3	4
2	5	6	7	8
3	9	10	11	12
4	13	14	15	16

	1	2	3	4
$\pi' =$	1	4	3	2
4	13	16	15	14
3	9	12	11	10
2	5	8	7	6

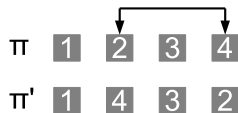
Only a subset of the changes affect the computation of the objective function

Do not recompute the evaluation function from scratch!

Equivalent speed-ups with Transpose and Insertion.

(NOTE: Implementing speed-ups will get you extra points in the exercise)

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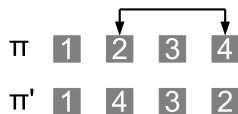
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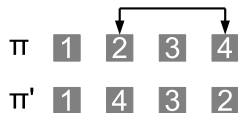
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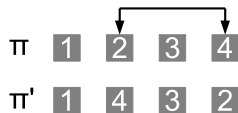
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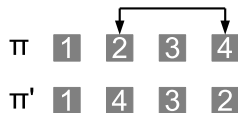
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Exercise 1.1: Iterative Improvement for the LOP

Instances

- LOP instances with sizes 150 and 250.
- A full description is provided in the project document on TEAMS

Experiments

Apply each algorithm k once to each instance i and record its :

- 1 Relative percentage deviation $\Delta_{ki} = 100 \cdot \frac{\text{best-known}_i - \text{cost}_{ki}}{\text{best-known}_i}$
- 2 Computation time (t_{ki})

Note: use constant random seed across algorithms, for each instance

Report for each algorithm k

- Average relative percentage deviation
- Sum of computation time

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Is there a statistically significant difference between the solution quality generated by the different algorithms?

Statistical test

- Paired t-test
- Wilcoxon signed-rank test

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Background: Statistical hypothesis tests (1)

- *Statistical hypothesis tests* are used to assess the validity of statements about properties of or relations between sets of statistical data.
- The statement to be tested (or its negation) is called the *null hypothesis* (H_0) of the test.
Example: For the Wilcoxon signed-rank test, the null hypothesis is that 'the median of the differences is zero'.
- The *significance level* (α) determines the maximum allowable probability of incorrectly rejecting the null hypothesis.
Typical values of α are 0.05 or 0.01.

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Background: Statistical hypothesis tests (2)

- The application of a test to a given data set results in a *p-value*, which represents the probability that the null hypothesis is incorrectly rejected.
- The null hypothesis is rejected iff this p-value is smaller than the previously chosen significance level.
- Most common statistical hypothesis tests are already implemented in statistical software such as the *R software environment* (<http://www.r-project.org/>).

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Example in R

```
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a.cost <- read.table("lop-best-ex-rand.dat")$V1
a.cost <- 100 * (a.cost - best.known) / best.known
b.cost <- read.table("lop-best-ins-rand.dat")$V1
b.cost <- 100 * (b.cost - best.known) / best.known
t.test (a.cost, b.cost, paired=T)$p.value
[1] 0.8819112 // Greater than 0.05!
wilcox.test (a.cost, b.cost, paired=T)$p.value
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Exercise 1.2 VND algorithms for the LOP

Implement 2 VND algorithms for the LOP

- Pivoting rule: first-improvement
- Neighborhood order:
 - ① transpose \rightarrow exchange \rightarrow insert
 - ② transpose \rightarrow insert \rightarrow exchange
- Initial solution:
 - ① CW heuristic

Exercise 1.2 VND algorithms for the LOP

Variable Neighbourhood Descent (VND)

k neighborhoods $\mathcal{N}_1, \dots, \mathcal{N}_k$

$\pi := \text{GenerateInitialSolution}()$

$i := 1$

repeat

 choose the first improving neighbor $\pi' \in \mathcal{N}_i(\pi)$

if $\nexists \pi'$ **then**

$i := i + 1$

else

$\pi := \pi'$

$i := 1$

until $i > k$

Exercise 1.2 VND algorithms for the LOP

Implement 4 VND algorithms for the LOP

- Instances: Same as for exercise 1.1
- Experiments: Same as for exercise 1.1 (i.e., **one run** of each algorithm per instance with constant seeds)
- Report: Same as for exercise 1.1
- Statistical tests: Same as for exercise 1.1

- Instances and “skeleton” code are available on TEAMS
- Some of the deliverables you need to provide in a zip folder with your name via TEAMS are:
 - your implementation in C, C++ or Java. Python is **not** recommended
 - a README file explaining how to run your implementation from the command line on Linux
 - a report no longer than 5 pages describing the implementation of the algorithms and the results you obtained (more detail on TEAMS)
 - see the full description of the deliverables in the pdf on TEAMS
- Deadline is April 7, 2024 (23:59)
- Questions?
Use the Post tab of the implementation channel on TEAMS