$AddBirthday _$ $\Delta Birthday Book$ name?: NAMEdate?: DATEname? ∉ known

 $birthday' = birthday \cup \{name? \mapsto date?\}$