

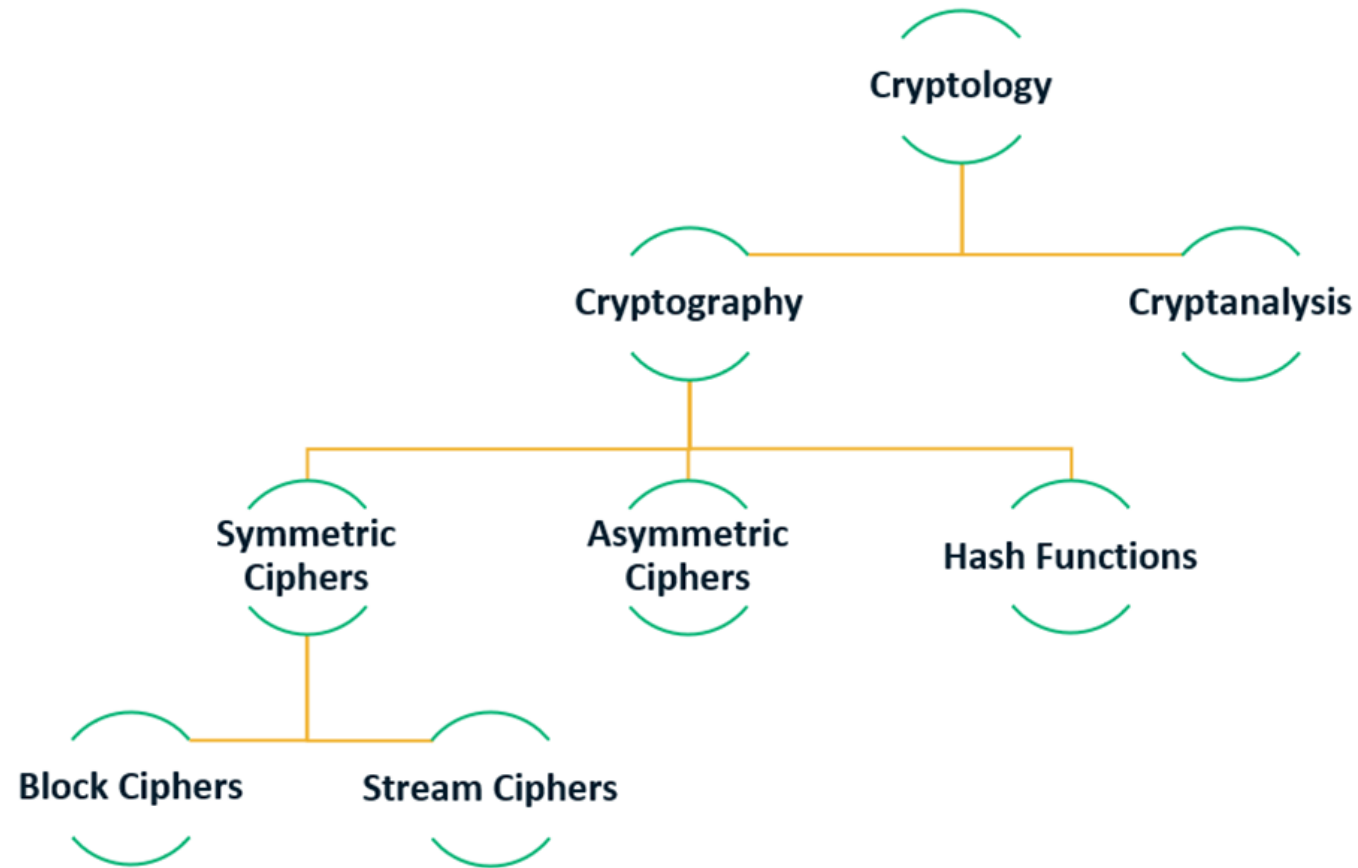
Cryptology

Dr. Ruba Al Omari

EECS 3401 – Applied Cryptography

Topics – Cryptology

- Introduction
- Cryptography
- Cryptanalysis
- The Use of Random Numbers
- Encryption Scheme Security



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Etymology

- Kryptos (Greek) = hidden
 - Cryptology.
 - Ology = Study.
- Sifr (Arabic) = zero
 - cipher, encipher, decipher.
- Steganos (Greek) = covered
 - Steganography.
 - Graphy – Written or Process.

<https://en.wikipedia.org/wiki/Kryptos#>



Kryptos: By Jim Sanborn - Jim Sanborn, CC BY-SA 3.0,
<https://commons.wikimedia.org/w/index.php?curid=8253447>

Definitions 1/2

- **Plaintext**: An original message.
- **Ciphertext**: The coded message.
- **Enciphering/Encryption**: The process of converting from plaintext to ciphertext.
- **Deciphering/Decryption**: Restoring the plaintext from the ciphertext.

Definitions 2/2

- **Cryptography**: The process of making and using codes to secure information.
- **Cryptanalysis**: The process of obtaining the plaintext message from a ciphertext message without knowing the keys used to perform the encryption.
- **Cryptology**: The field of science that encompasses cryptography and cryptanalysis.

CRYPTOLOGY = CRYPTOGRAPHY + CRYPTANALYSIS

History of Cryptography

- 1900 BC: Egypt - first documented use of written cryptography.

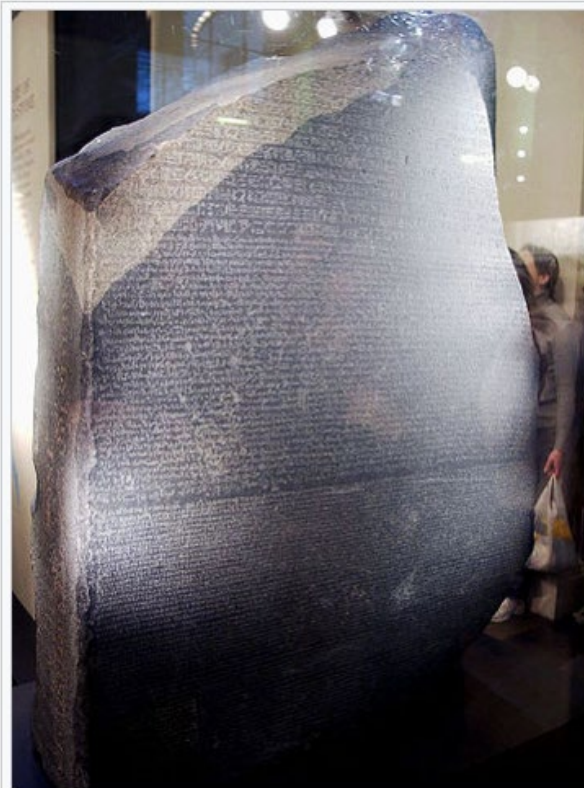
Egyptian hieroglyphs



Hieroglyphs from the tomb of **Seti I (KV17)**, 13th century BC



Hieroglyphs typical of the Graeco-Roman period



The **Rosetta Stone** in the **British Museum**



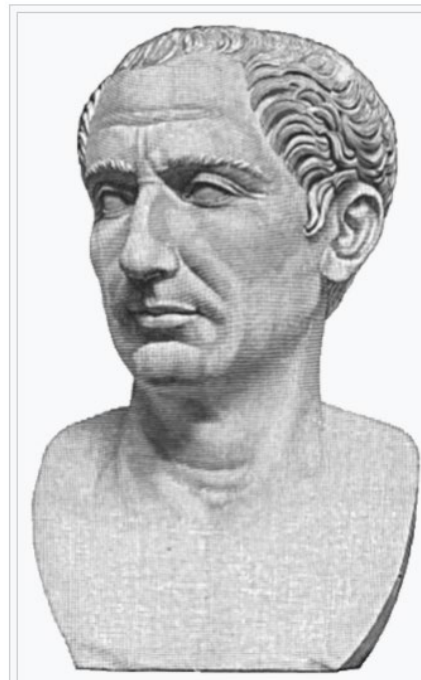
Ibn Wahshiyya's attempt at a translation of a hieroglyphic text

History of Cryptography

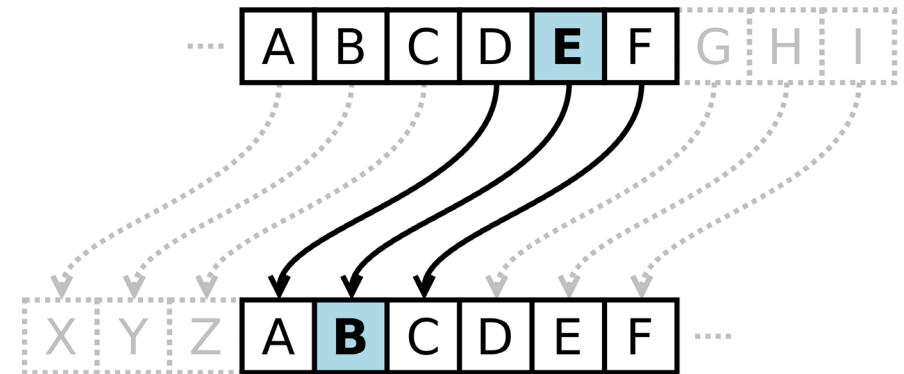
- 487-50 BC: Spartans & Julius Caesar



	I	a	m	h	u	
—	r	t	v	e	r	—
	y	b	a	d	l	
	y	h	e	l	p	



The Caesar cipher is named for **Julius Caesar**, who used an alphabet where decrypting would shift three letters to the left.



<https://en.wikipedia.org/wiki/Scytale>

https://en.wikipedia.org/wiki/Caesar_cipher

History of Cryptography

- 1466: Alberti Polyalphabetic Cipher

Leon Battista Alberti



Presumed self-portrait of Alberti

Born	14 February 1404 Genoa, Republic of Genoa
Died	25 April 1472 (aged 68) Rome, Papal States
Nationality	Italian



The Alberti Cipher disk.

History of Cryptography

- World War I: **Substitution** and **Transposition** Ciphers

Hello

Hello

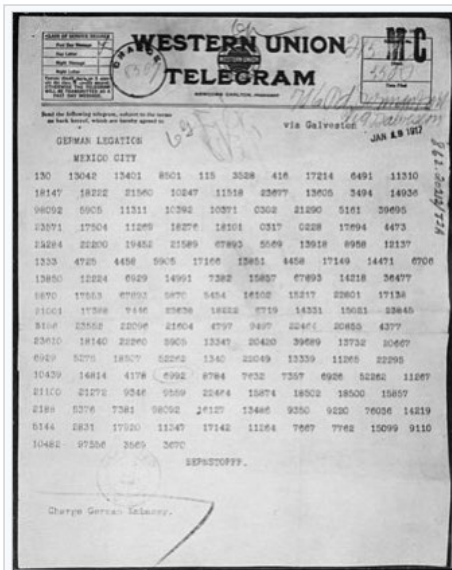
asddf

Holel

History of Cryptography

Vernam, an AT&T employee, invented a polyalphabetic cipher machine that used a nonrepeating random key.

■ World War I: Zimmerman Telegram & OTP (One-Time Pad) – 1914-18



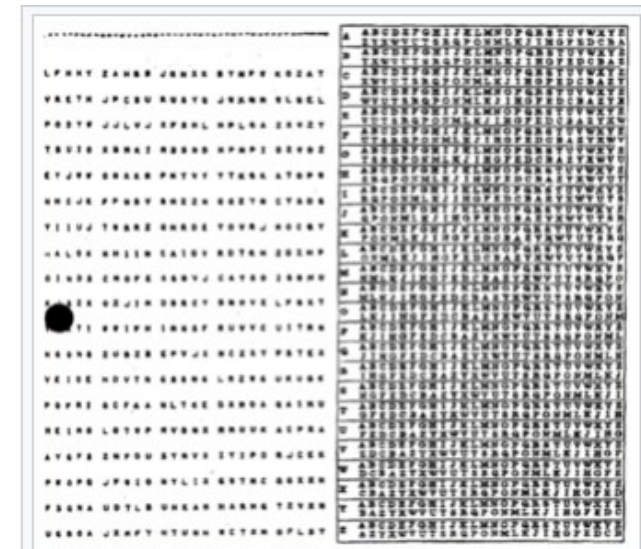
The Zimmermann telegram as it was sent from Washington, DC, to Ambassador Heinrich von Eckardt, the German ambassador to Mexico.

4458 gemessen
17149. Indem schloß.
14471
6706 reichlich
13850 finanziell
12224 unterstutzung
6929 und
14991 einverstanden
7382 ausserorts.
156517 2a/3
67893 Mexico.
14218 in
36477 Texas
5870
17553
67893
5870
5454
16102
15217
22801 A

A portion of the telegram as decrypted by British Naval Intelligence codebreakers. Since the word Arizona was not in the German codebook, it had to be split into phonetic syllables.



Mexico in 1916 (in dark green); territory promised to Mexico in the Zimmermann telegram (in light green); and the pre-1836 original Mexican territory (red line)



A format of one-time pad used by the U.S. National Security Agency, code named DIANA. The table on the right is an aid for converting between plaintext and ciphertext using the characters at left as the key.

History of Cryptography

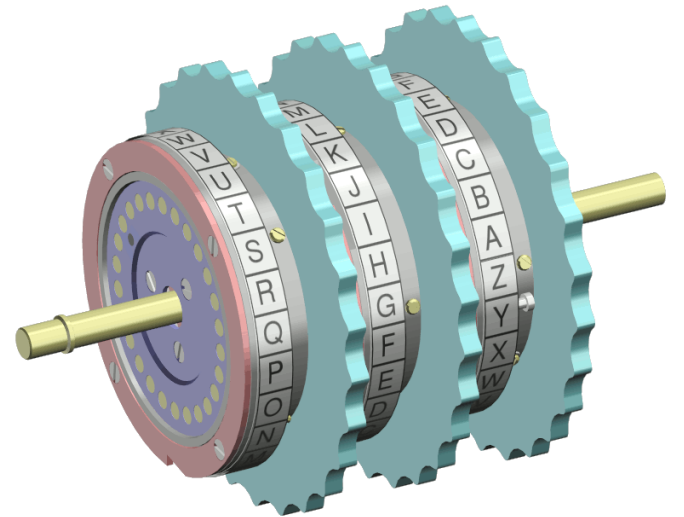
- World War II: Enigma Machine (1939-45)
 - Typing illuminates an alternate letter
 - This is your encoded letter.
 - Which letter lights up depends on the arrangement of the rotors.
 - Each rotor has a possible 26 settings.
 - Adding extra security is a plugboard
 - This swipes letters of any letter of the operator's choosing.



Two Enigma rotors showing electrical contacts, stepping ratchet (on the left) and notch (on the right-hand rotor opposite D).

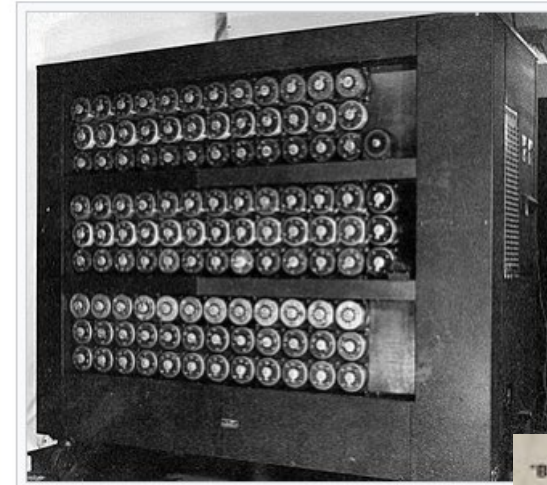
History of Cryptography

- World War II: Enigma Machine
 - To read a message you need to enter the right initial rotor and plugboard settings on your Enigma machine.
 - Without these settings, decoding is almost impossible with over **150 million, million, million** possible combinations.



History of Cryptography

- World War II: Enigma Machine
 - The Allies broke the Enigma machine by exploiting operator errors, captured codebooks, and developing advanced decryption techniques, notably using the **Bombe** machine designed by **Alan Turing** and others at Bletchley Park.
 - This allowed them to reverse-engineer Enigma settings and decode messages.



A wartime picture of a [Bletchley Park](#) Bombe



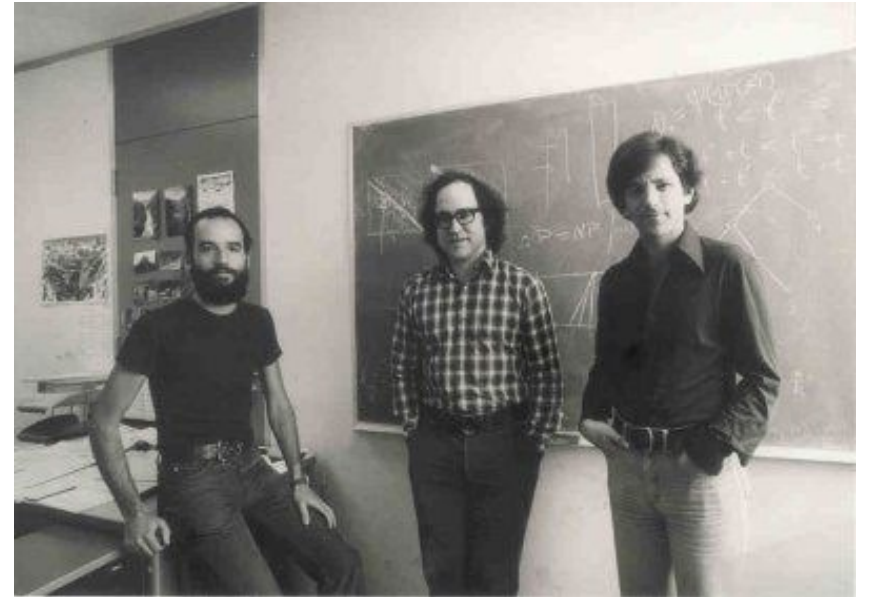
History of Cryptography

■ 1976- : Public Key Cryptography



Whitfield Diffie and Martin Hellman

<https://www.acm.org/articles/bulletins/2016/march/turing-2015-diffie-hellman>



December 197X, left to right: Adi Shamir, Ron Rivest, and Len Adleman Image
<https://people.csail.mit.edu/rivest/photos/photos.html>

History of Cryptography

Date	Event
1900 B.C.	Egyptian scribes used nonstandard hieroglyphs while inscribing clay tablets; this is the first documented use of written cryptography.
487 B.C.	The Spartans of Greece developed the <i>skytale</i> , a system consisting of a strip of papyrus wrapped around a wooden staff. Messages were written down the length of the staff, and the papyrus was unwrapped. The decryption process involved wrapping the papyrus around a shaft of similar diameter.
50 B.C.	Julius Caesar used a simple substitution cipher to secure military and government communications. To form an encrypted text, Caesar shifted the letters of the alphabet three places. In addition to this monoalphabetic substitution cipher, Caesar strengthened his encryption by substituting Greek letters for Latin letters.
1466	Leon Battista Alberti, the father of Western cryptography, worked with polyalphabetic substitution and designed a cipher disk.
1914–17	Throughout World War I, the Germans, British, and French used a series of transposition and substitution ciphers in radio communications. All sides expended considerable effort to try to intercept and decode communications, and thereby created the science of cryptanalysis. British cryptographers broke the Zimmerman Telegram, in which the Germans offered Mexico U.S. territory in return for Mexico's support. This decryption helped to bring the United States into the war.
1917	Gilbert S. Vernam, an AT&T employee, invented a polyalphabetic cipher machine that used a nonrepeating random key.
1919	Hugo Alexander Koch filed a patent in the Netherlands for a rotor-based cipher machine; in 1927, Koch assigned the patent rights to Arthur Scherbius, the inventor of the Enigma machine.
1939–42	The Allies secretly broke the Enigma cipher, undoubtedly shortening World War II.
1976	Whitfield Diffie and Martin Hellman introduced the idea of public-key cryptography.
1977	Ronald Rivest, Adi Shamir, and Leonard Adleman developed a practical public-key cipher both for confidentiality and digital signatures; the RSA family of computer encryption algorithms was born.

Crypto Museum

Welcome at the Crypto Museum website. At present we are a virtual museum in The Netherlands, that can only be visited on the internet 24 hours a day. However, we do have a physical collection, and regularly organise [exhibitions](#), [events](#) and lectures, in cooperation with other organisations.



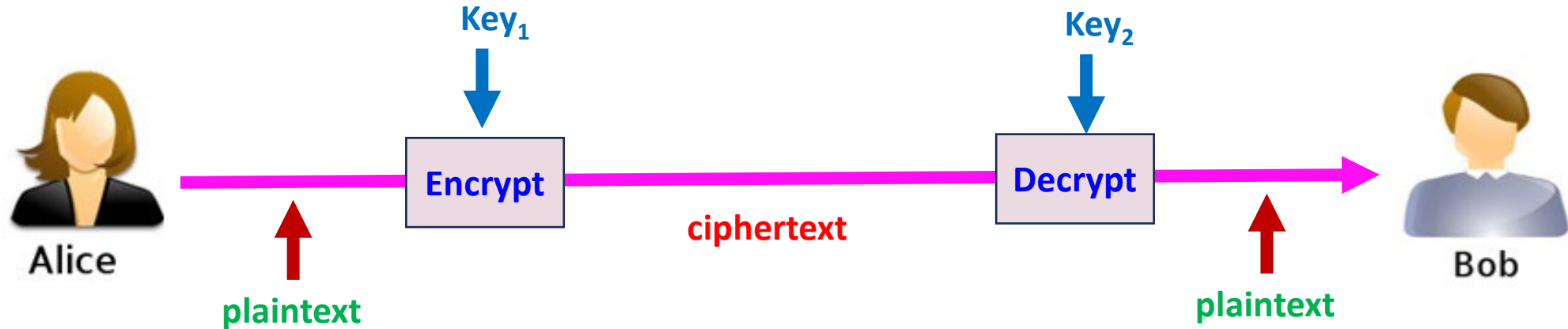
The main goal of Crypto Museum is to preserve history. This is done by collecting, restoring and describing historical [cipher machines](#) – such as the well-known [Enigma machine](#) – [spy radio sets](#), [intercept receivers](#) and other [espionage-related items](#). For a detailed explanation of why we do this, please read our [mission statement](#). Many of the items described on this website are part of the Crypto Museum collection, but some have only crossed our path briefly, or are impossible to obtain. Whenever possible, we have tried to describe the equipment to the best of our abilities.

Source: <https://www.cryptomuseum.com/index.htm>

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The Model



- The **P** and **C** sets

Strings Σ^* over some alphabet Σ , e. g., $\Sigma = \{0, 1\}$ or $\{A - Z\}$

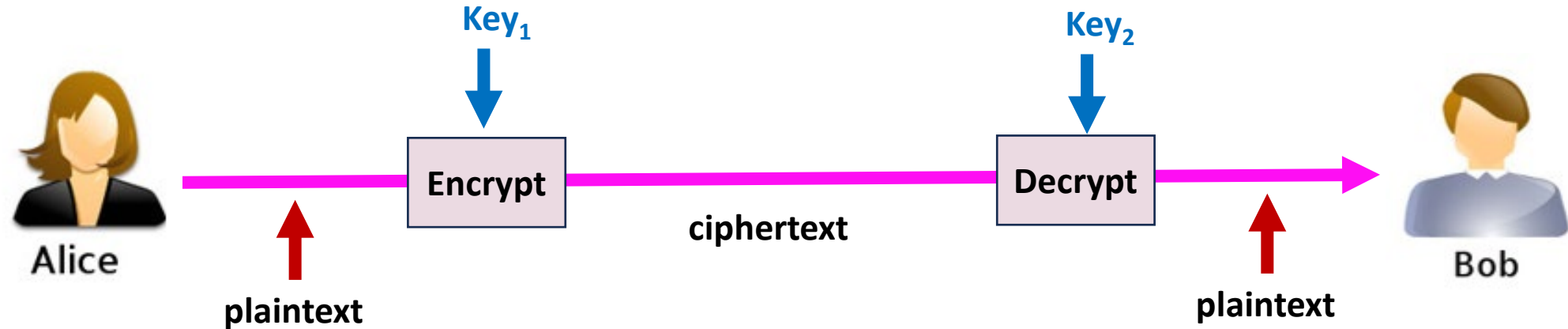
- The **E** and **D** transformations

Keyed functions transforming **P** \leftrightarrow **C**.

- The Cryptosystem

The tuple (**P**, **C**, **K1**, **K2**, **E**, **D**)

Secret vs. Public vs. Private



- **Symmetric** (aka **Secret-Key**) Cryptography.
Key₁=Key₂ and known only to the legitimate parties.
- **Asymmetric** (aka **Public-Key**) Cryptography.
Key₁ is Bob's public, Key₂ is his private key.
- The **Kerckhoff** Principle.
 - Reject Security by Obscurity: E and D are public but not the key.

Alice and Bob

- Do you know how old are Alice and Bob?



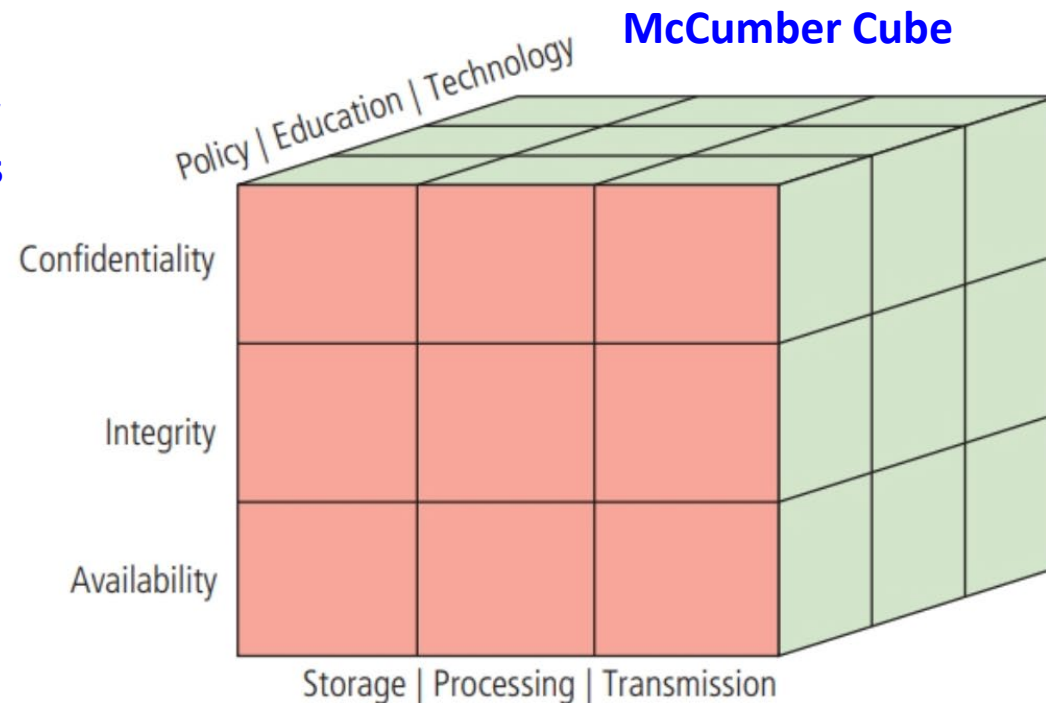
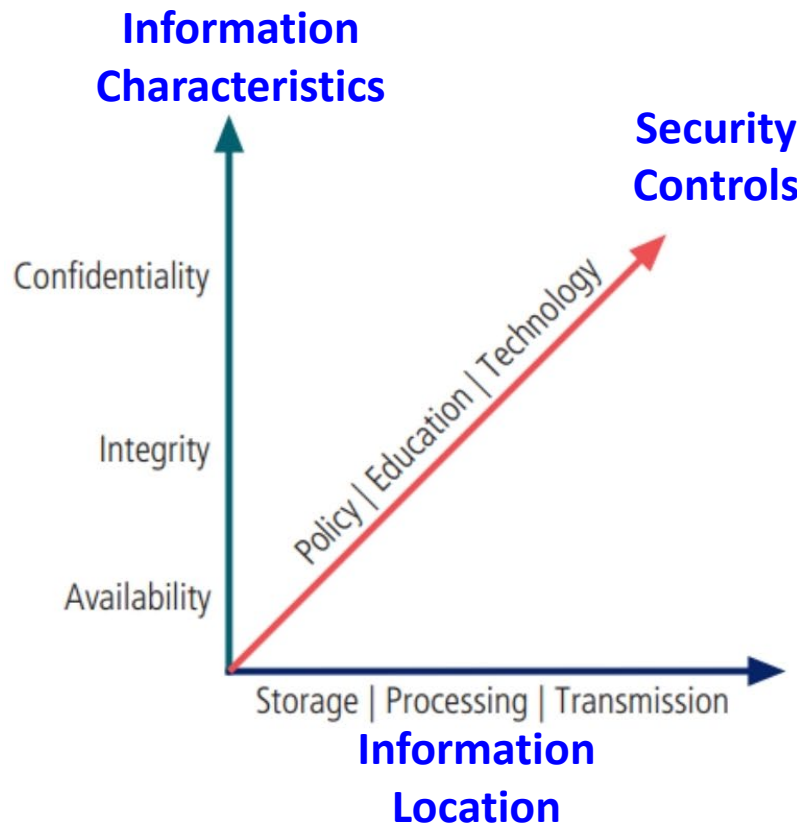
Alice



Bob

The CIA Triad

- **C**onfidentiality, **I**ntegrity, and **A**vailability.
- Which one do you think is the most important?



The CIA Triad

- **Confidentiality**

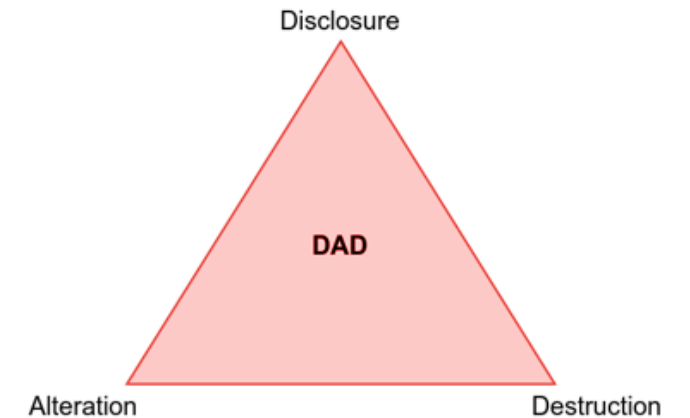
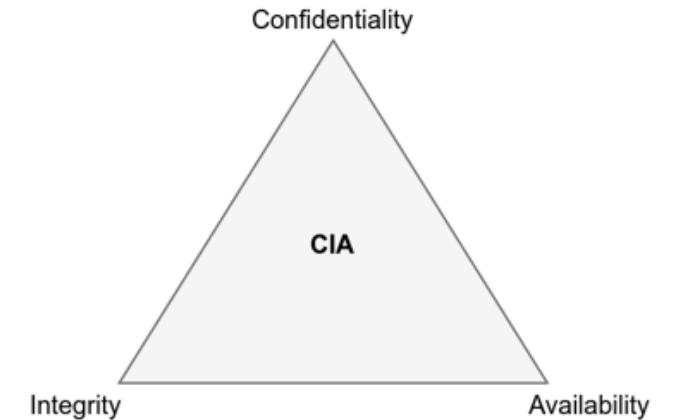
- Based on need-to-know

- **Integrity**

- Of Content integrity
- Of Parties authentication
- Of Time of sending freshness
- Of Act of sending non-repudiation

- **Availability**

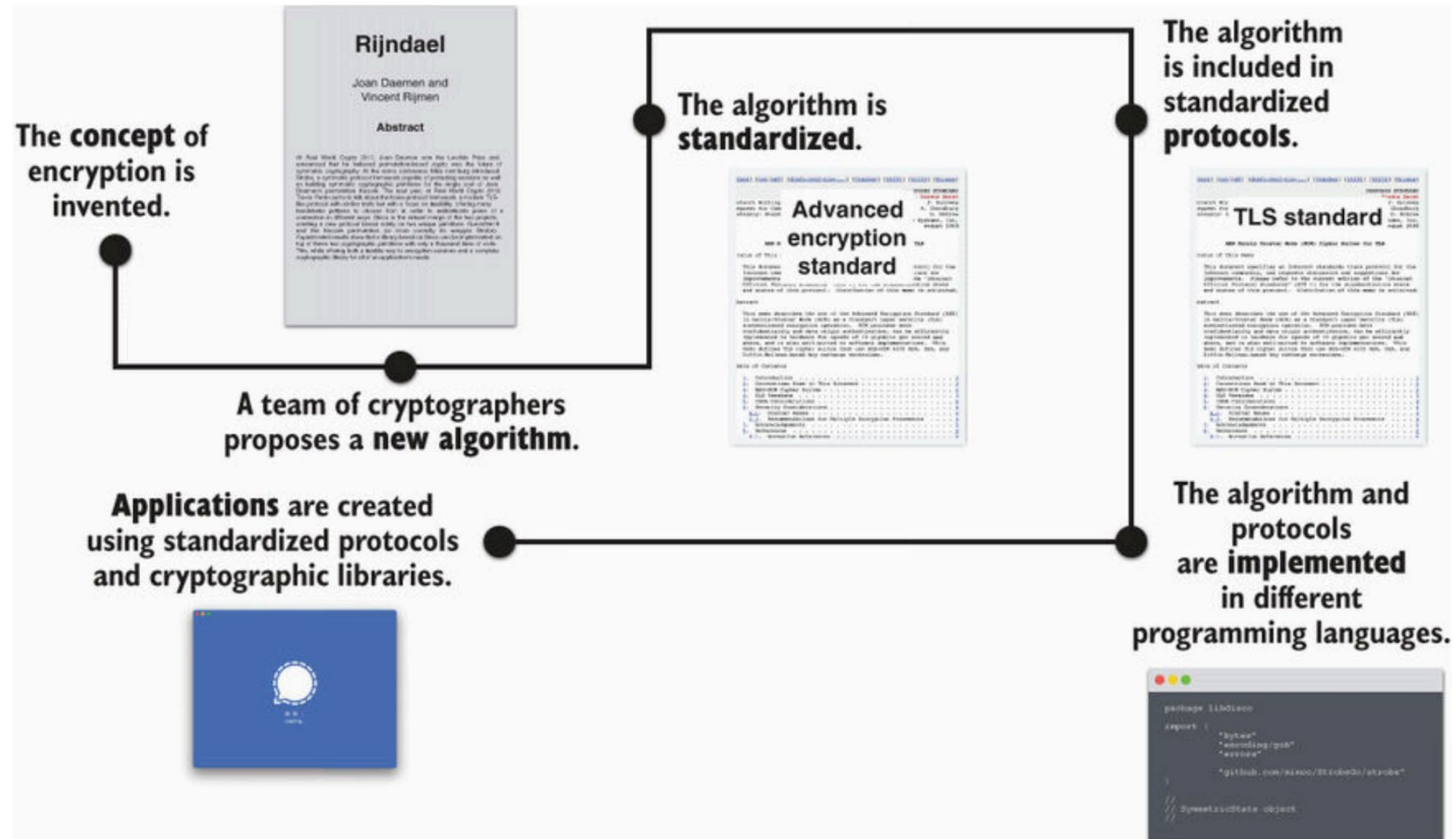
- Anytime from anywhere



The Primitives of Cryptography

1. **Symmetric Ciphers** (*efficient, AES*) - One pre-shared **secret** key per pair of actors
 2. **Asymmetric Ciphers** (*inefficient, RSA*) - One **Public/Private** key pair per actor
 3. **Cryptographic Hash Functions** (*efficient, SHA*) - Maps a message of arbitrary size to a fixed-size **digest**. Any change in the message will almost certainly change the digest!
- Using a mix of these *three* building blocks plus a *random source*, cryptography promises to meet — *any* — security requirement!

Life Cycle for Cryptographic Algorithm

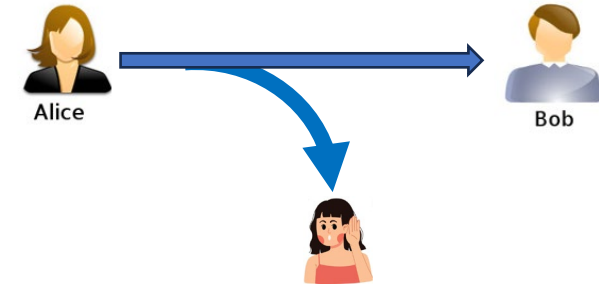
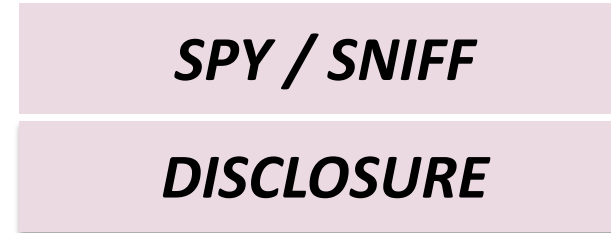


Topics – Cryptology

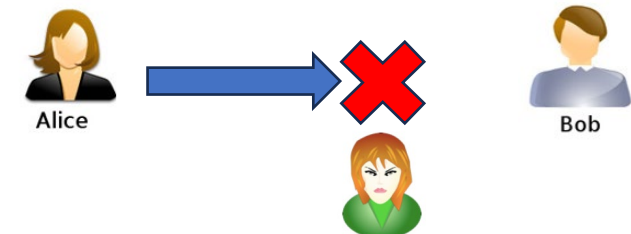
- Introduction
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- **Cryptanalysis**
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Attacks

- Confidentiality
Authentication & Authorization
Based on need-to-know



- Availability
Anytime from anywhere



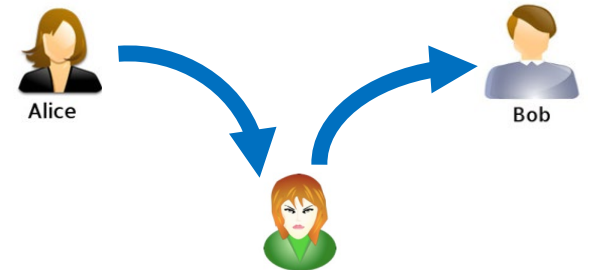
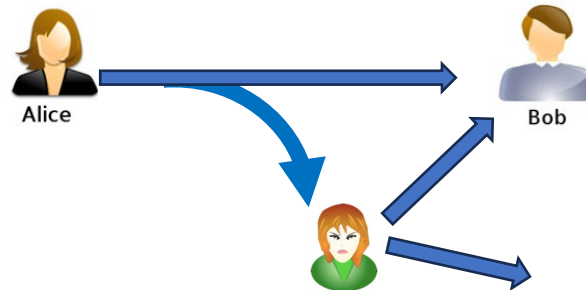
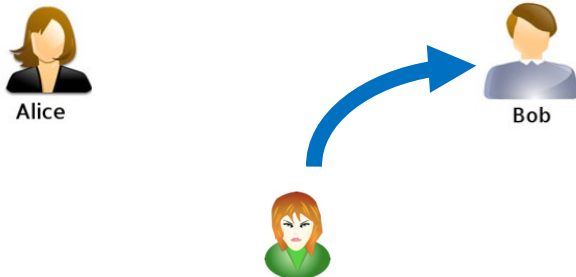
Attacks

- Integrity
Of Sender and Sending
Of Time of sending
Of Content

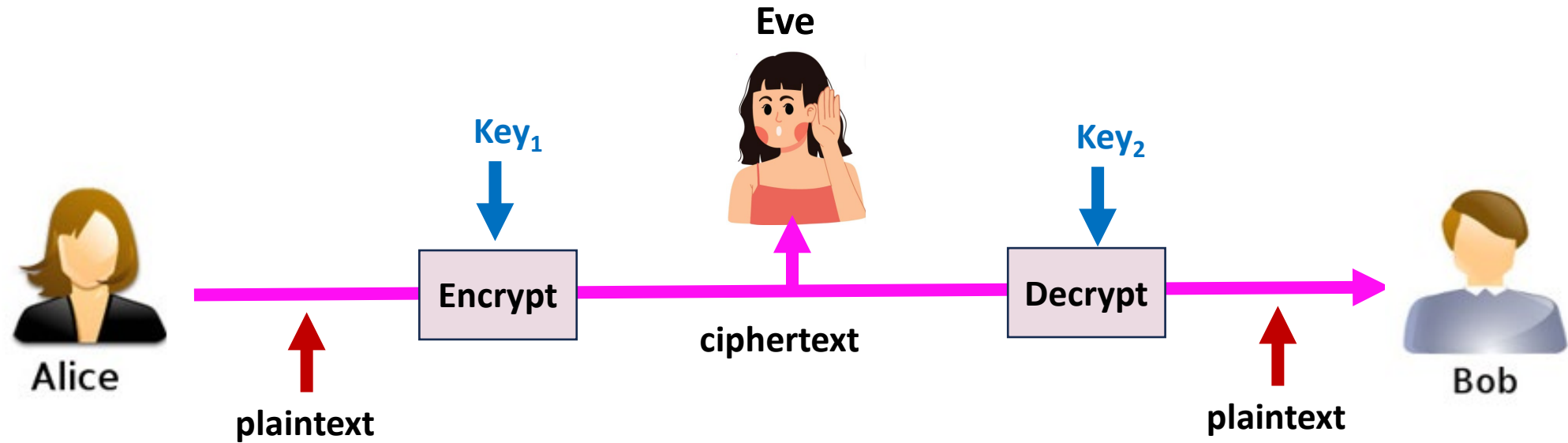
SPOOF / REPUDIATE

REPLAY

FABRICATE

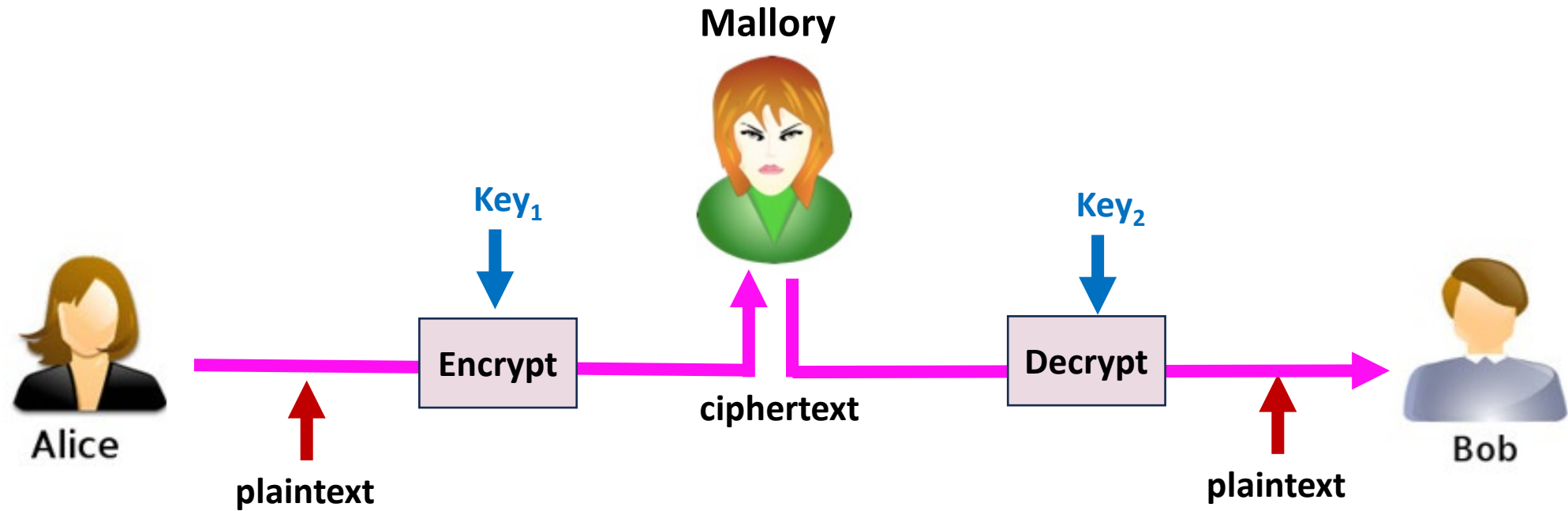


Meet Eve (Eavesdropper)



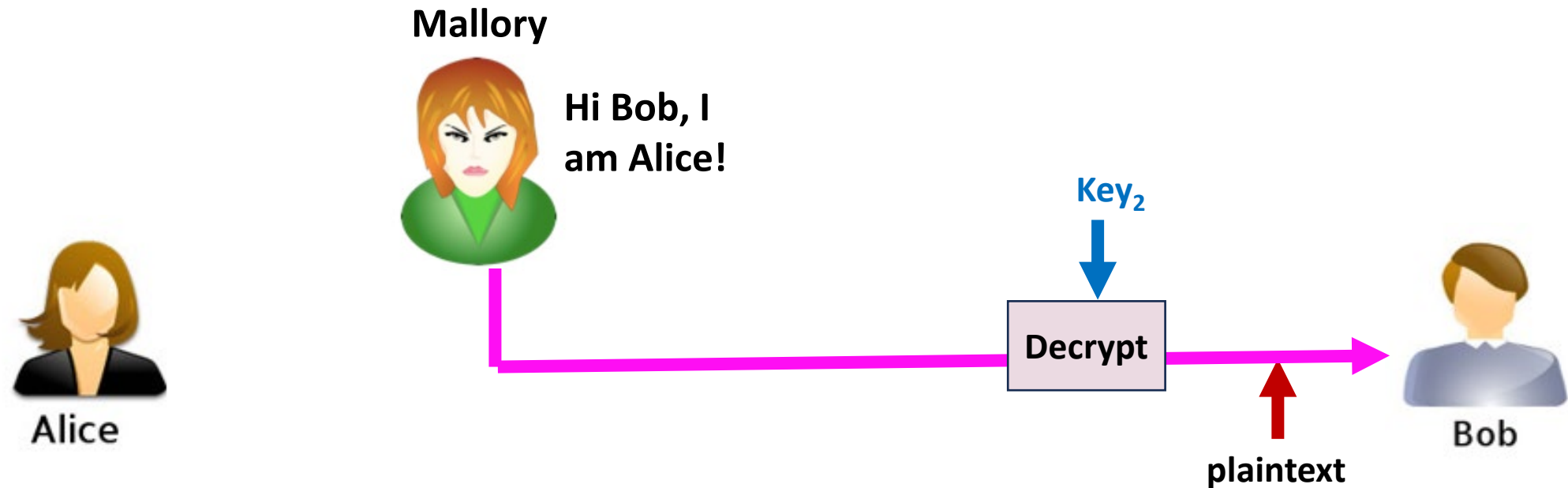
- Eve is a passive intruder: she doesn't affect the message but can gather stats/observe patterns, e.g., metadata; create a codebook via KPA, etc. She therefore violates confidentiality.

Meet Mallory* (Malicious)



* AKA Trudy (Intruder). Mal is an active attacker: she can block or change the message. She can violate all three CIA goals.

Mallory Masquerading as Alice



- Mal is spoofing Bob by masquerading as Alice (perhaps via replay). This causes loss of integrity of message origin.

Attacks

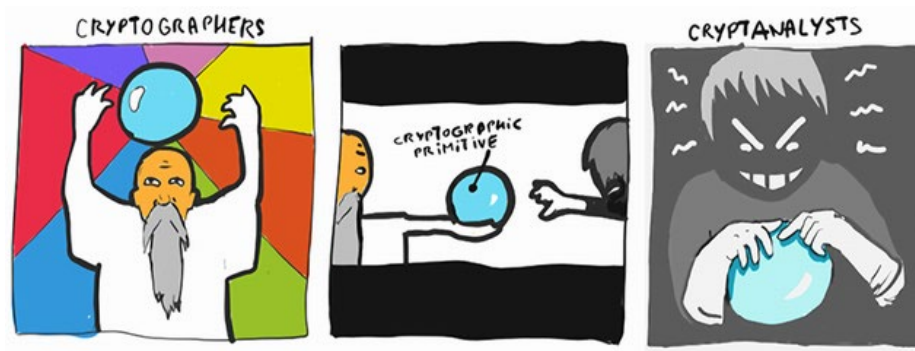
Exhaustive

Scan the Entire Key Space

Does not depend on the specific algorithm, only **depends on key length**.

Try each value until a collision occurs.

Cryptanalytic



Scan a Subset of the Key Space

Based on **weaknesses** in a particular cryptographic algorithm.

Seek to exploit some property of the algorithm to perform some attack other than an exhaustive search.

Exhaustive (Scan The Entire Key Space)

- Aka *Brute-Force* or *Trial-and-Error*
- Involves trying every possible key until an intelligible translation of the ciphertext into plaintext is obtained
- Lends itself naturally to parallel computations

Key size /b	Number of keys	1 Core	Cluster
32	$2^{32} = 4.3 \times 10^9$	1 hr	2.15 ms
56	$2^{56} = 7.2 \times 10^{16}$	10^3 yr	10 hr
128	$2^{128} = 3.4 \times 10^{38}$	10^{24} yr	10^{18} yr
168	$2^{168} = 3.7 \times 10^{50}$	10^{36} yr	10^{30} yr

The age of the universe is only ~13.6 billion (10^{10}) years

Encryption Key Power – Specific Example

It is estimated that to crack an encryption key using a brute force attack, a computer needs to perform a maximum of 2^k operations (2^k guesses), where k is the number of bits in the key. The average estimated time to crack is approximately half that time.

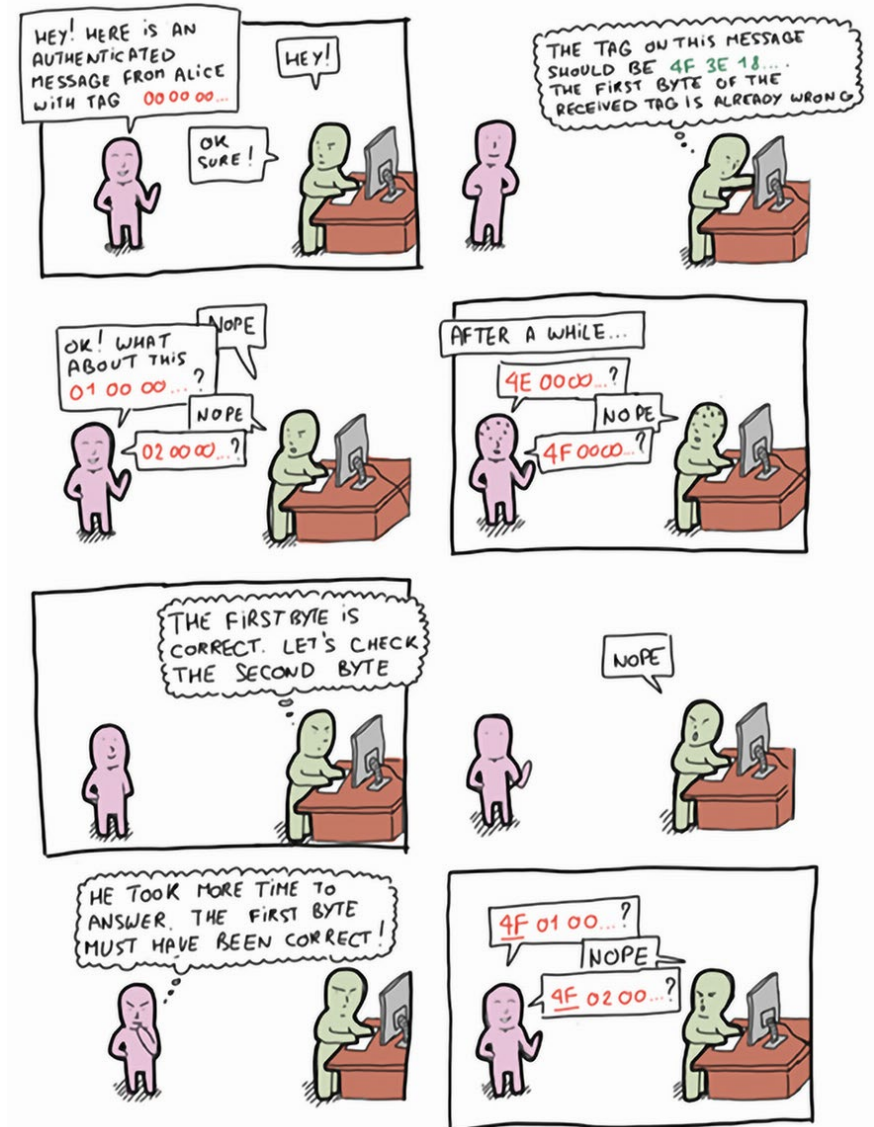
[illegible]

Note: Estimated Time to Crack is based on a 2020-era Intel i9-10900X 10 Core CPU performing 585 Dhrystone GFLOPS (giga/billion floating point operations per second) at 5.2 GHz (overclocked). Modern workstations are capable of using multiple CPUs, further decreasing time to crack, or simply splitting the workload among multiple systems.

Note: The authors acknowledge that this benchmark is based on a very specific application test and that the results are not generalizable. However, these calculations are shown to illustrate the relative difference between key length and resulting strength rather than to accurately depict time to crack.

Cryptanalytic (Scan a Subset of the Key Space)

- Attack Models
 - Known / Chosen Ciphertext (KCA/CCA)
 - Known / Chosen Plaintext (KPA/CPA)
- Methodologies
 - Residual Patterns in CT
 - Pass the Hash
 - Targets authentication protocol.
 - Algorithmic/Implementation Vulnerability
 - Dictionary, Rainbow Table
 - Birthday
 - Meet-in-the-Middle, Man-in-the-Middle



KPA & CPA

- KPA: The attacker **knows some or all of the plaintext** of one or more messages (as well as the ciphertext).
 - “Dear bob”, or any constant header (e.g., Date: or Host: in protocols).
- CPA: The attacker is able to **submit any plaintext** the attacker chooses and obtain the corresponding ciphertext, and hopefully crack the key.

KCA & CCA

- KCA (most difficult): An attacker only has **access to the encrypted traffic** (ciphertext).
 - Some information about the plaintext can be guessed (e.g., language, character probability distribution, format of the message).
- CCA: The attacker is able to **submit any ciphertext** and obtain the corresponding plaintext.
 - **Example:** The attack on SSL 3.0 developed by Bleichenbacher of Bell Labs, which could obtain the RSA private key of a website after trying between 300,000 and 2 million chosen ciphertexts.

Types of Attacks on Encrypted Messages

Summary

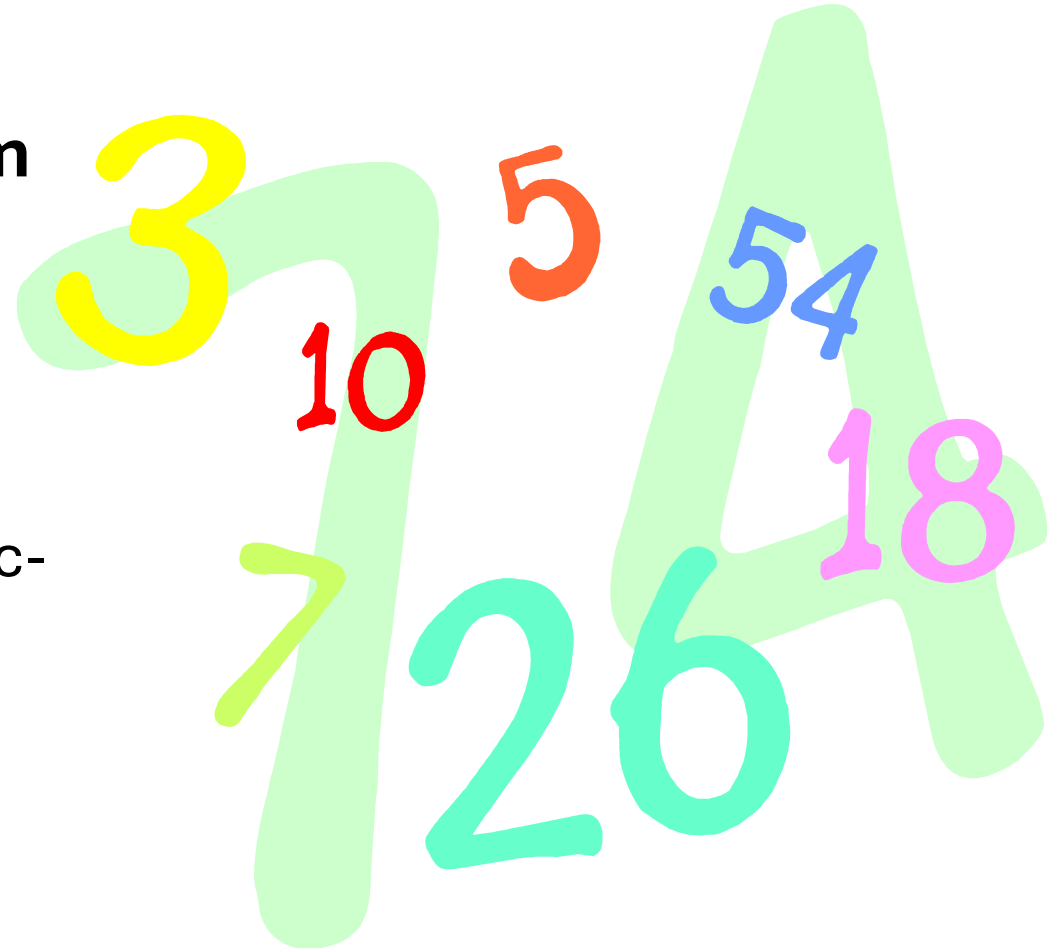
Type of Attack	Known to Cryptanalyst
Ciphertext Only (most difficult)	<ul style="list-style-type: none">• Encryption algorithm• Ciphertext
Known Plaintext	<ul style="list-style-type: none">• Encryption algorithm• Ciphertext• One or more plaintext–ciphertext pairs formed with the secret key
Chosen Plaintext	<ul style="list-style-type: none">• Encryption algorithm• Ciphertext• Plaintext message chosen by cryptanalyst, together with its corresponding ciphertext generated with the secret key
Chosen Ciphertext	<ul style="list-style-type: none">• Encryption algorithm• Ciphertext• Ciphertext chosen by cryptanalyst, together with its corresponding decrypted plaintext generated with the secret key

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The Use of Random Numbers

- Cryptography make use of **random** binary numbers, examples:
 - Nonces are used for handshaking to prevent replay attacks.
 - Session key generation.
 - Generation of keys for the RSA public-key encryption algorithm.
 - Generation of a bit stream for symmetric stream encryption.



Randomness /1

- A sequence generator is **pseudo-random** if it has this property:
 - **1- It looks random.**
 - It passes all the statistical tests of randomness that we can find (e.g., Diehard tests https://en.wikipedia.org/wiki/Diehard_tests).



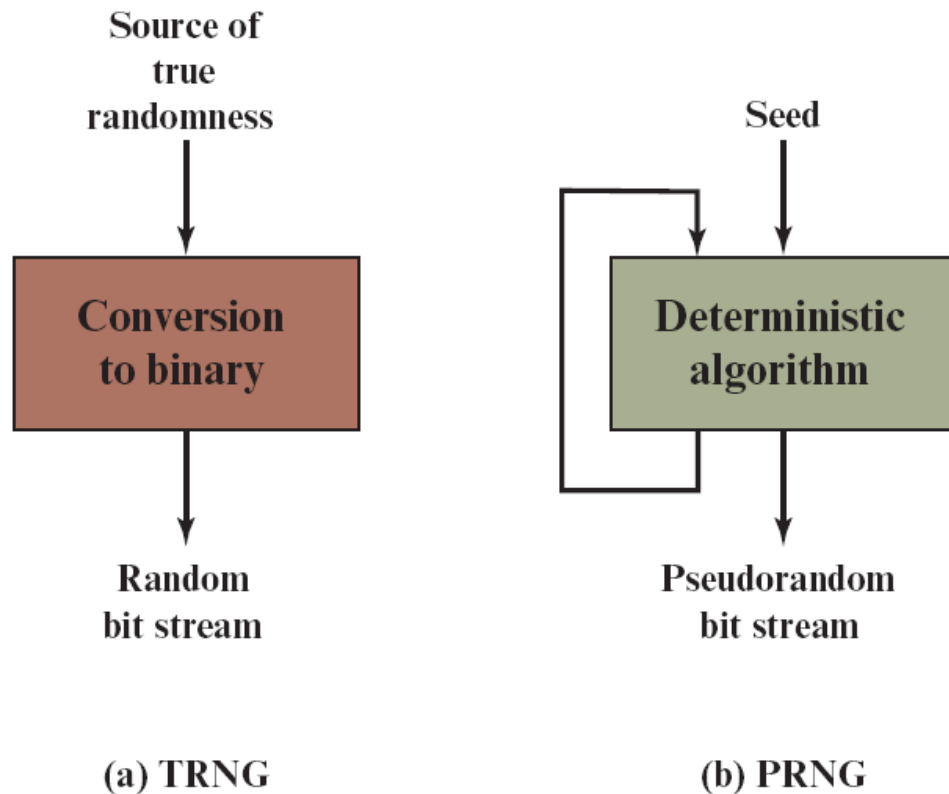
Randomness /2

- For a sequence to be **cryptographically secure pseudo-random**, it must also have this property:
 - **2. It is unpredictable.**
 - It must be computationally infeasible to predict what the next random bit will be, given complete knowledge of the algorithm or hardware generating the sequence and all of the previous bits in the stream.

Randomness /3

- A sequence generator is **true (or real) random** if it has this additional third property:
 - **3- It cannot be reliably reproduced.**
 - If you run the sequence generator twice with the exact same input (at least as exact as humanly possible), you will get two completely unrelated random sequences.

True Random and Pseudorandom Number Generators

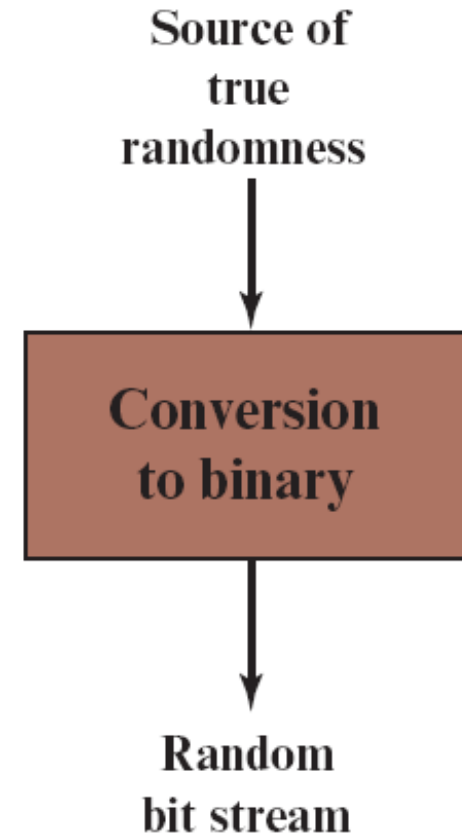


TRNG = true random number generator
PRNG = pseudorandom number generator

	True Random Number Generators	Pseudorandom Number Generators
Efficiency	Generally inefficient	Very efficient
Determinism	Nondeterministic	Deterministic

True Random Number Generator (TRNG)

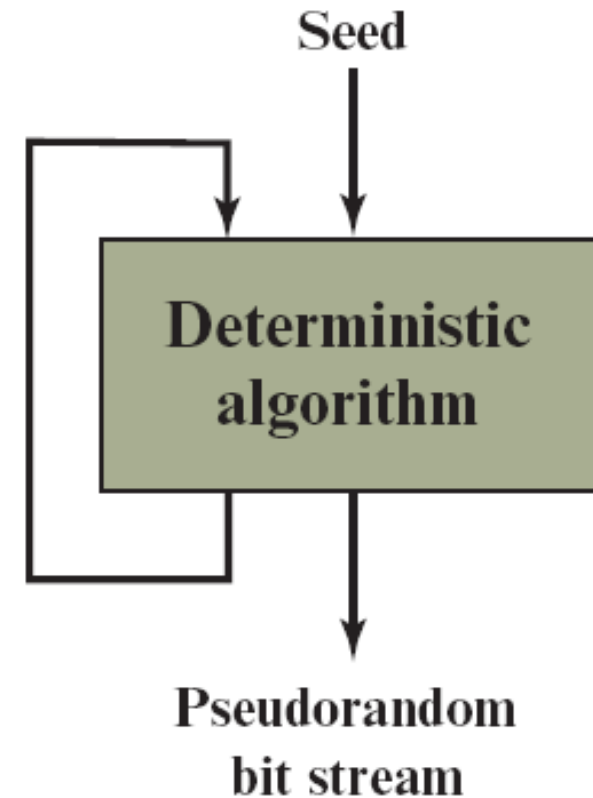
- Takes as input an **entropy source** that is drawn from the physical environment of the computer.
 - e.g., keystroke timing patterns, disk electrical activity, mouse movements, sound/video input.
- The source, or combination of sources, serve as input to an algorithm that produces random binary output.



(a) TRNG

Pseudorandom Number Generator (PRNG)

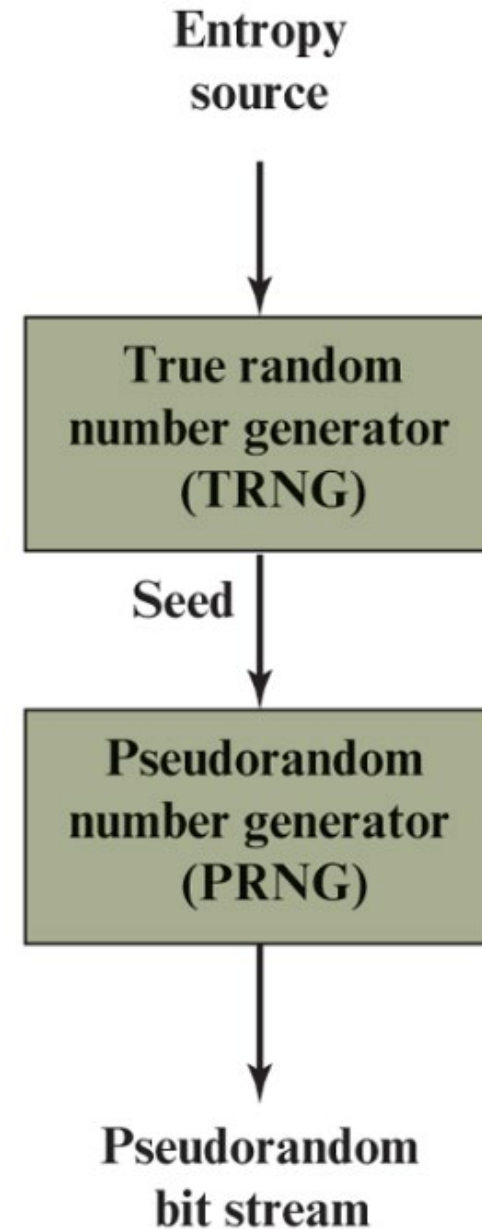
- Takes as input a fixed value, called the **seed**, and produces a sequence of output bits using a deterministic algorithm.
- The output bit stream is determined solely by the input value or values, so **an adversary who knows the algorithm and the seed can reproduce the entire bit stream.**



(b) PRNG

Seed Requirements

- For cryptographic applications, the seed that serves as input to the PRNG must be secure, and is generated by a TRNG.

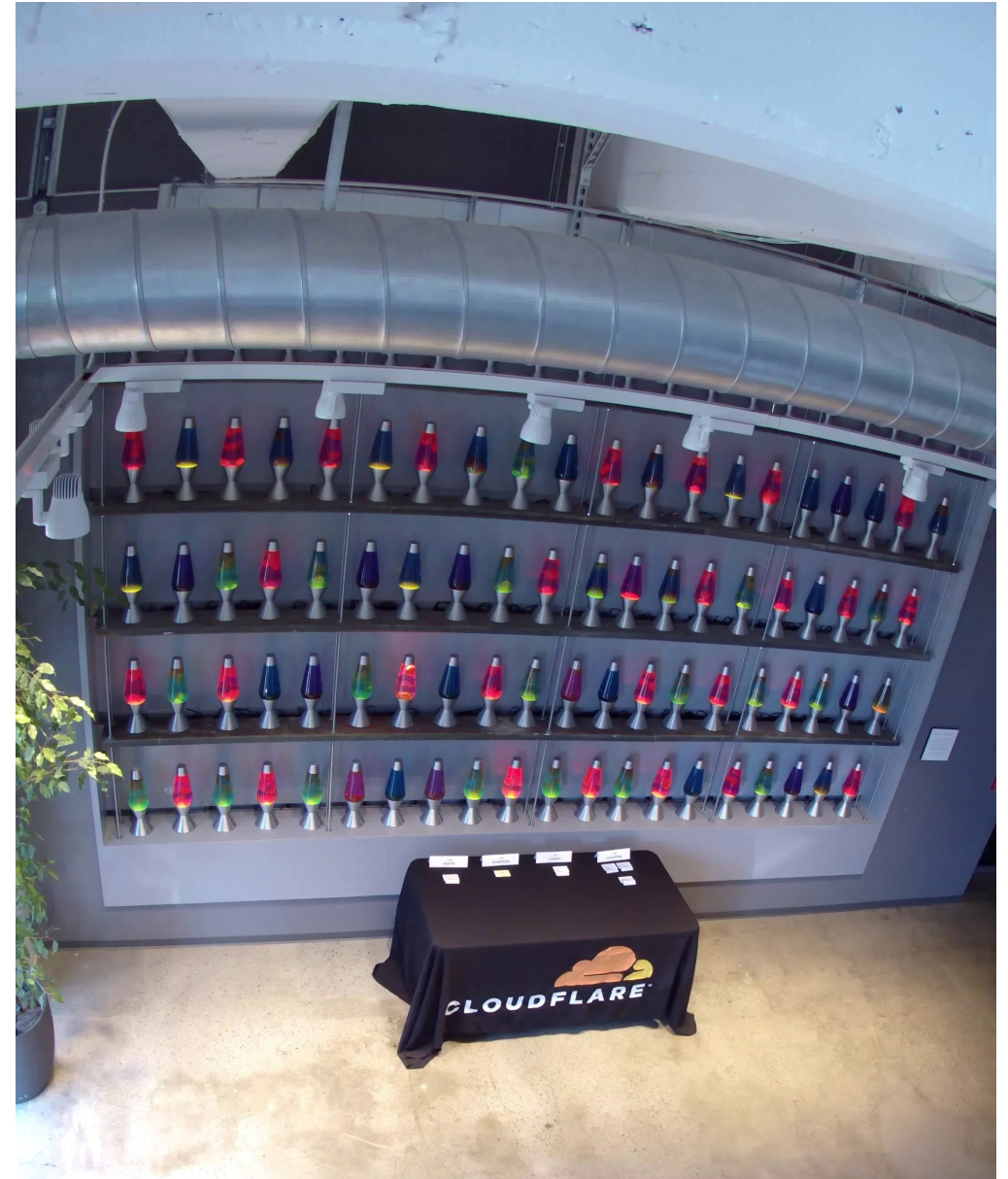


The view from the camera

“A wall of lava lamps in the lobby of our San Francisco office provides an unpredictable input to a camera aimed at the wall.

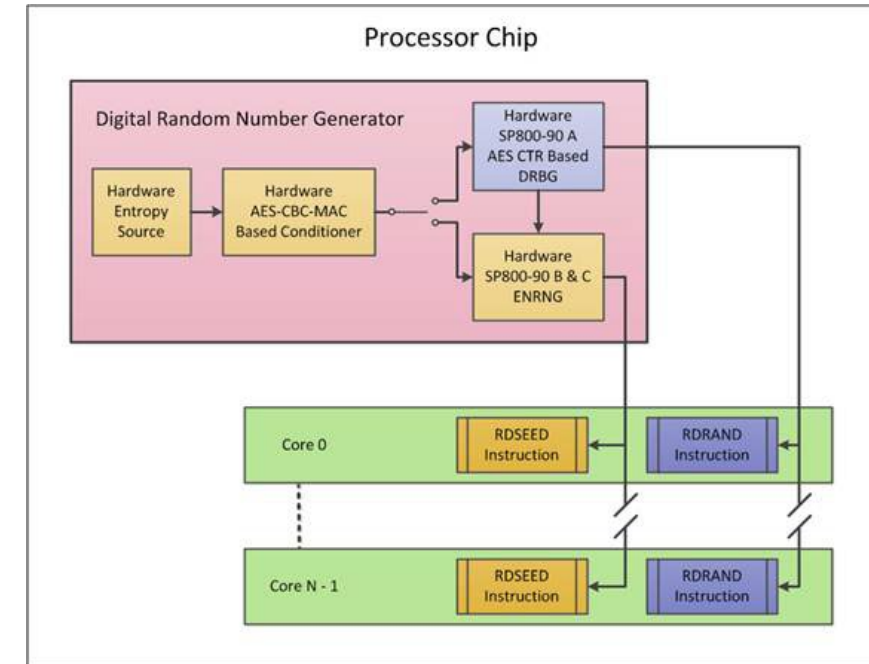
A video feed from the camera is fed into a CSPRNG, and that CSPRNG provides a stream of random values that can be used as an extra source of randomness by our production servers.

Since the flow of the “lava” in a lava lamp is very unpredictable, “measuring” the lamps by taking footage of them is a good way to obtain unpredictable randomness.”



Intel Digital Random Number Generator

- The Entropy Source runs on a self-timed circuit and uses **thermal noise** within the silicon to output a random stream of bits at the rate of 3 GHz.
- Thermal noise generated by **random motion of free electrons in a conductor** resulting from thermal agitation.



Intel Processor Chip with Random Number Generator

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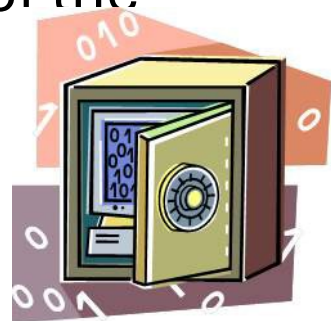
Encryption Scheme Security

- **Unconditionally secure**

- No matter how much time an opponent has, it is impossible for him or her to decrypt the ciphertext simply because the required information is not there.

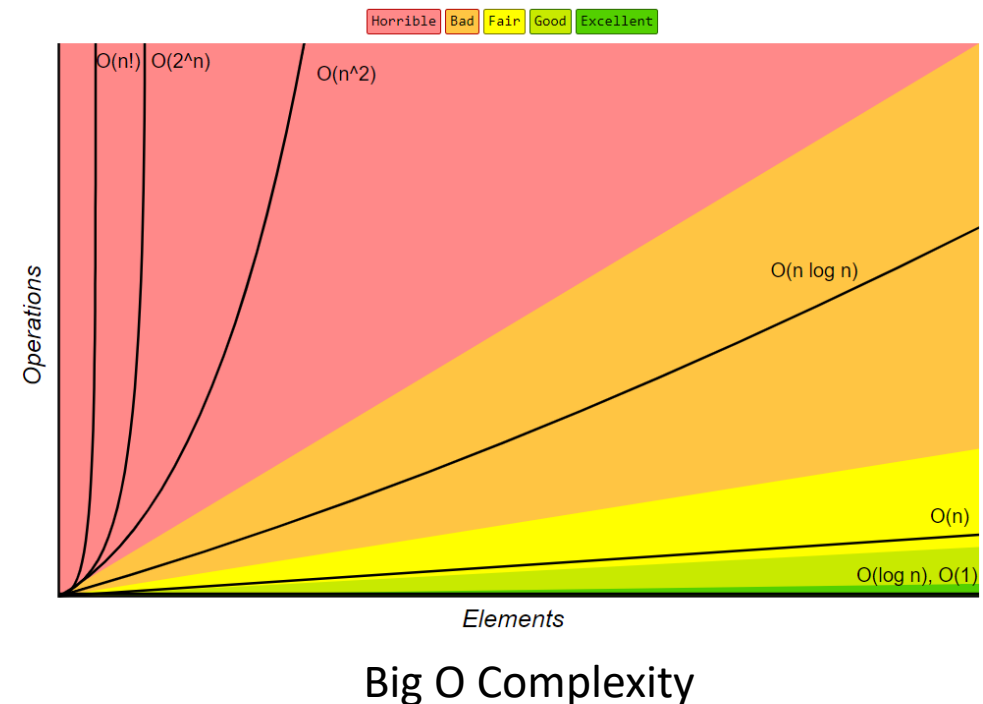
- **Computationally secure**

- The **cost** of breaking the cipher **exceeds the value** of the encrypted information.
- The **time** required to break the cipher **exceeds the useful lifetime** of the information.



Cost of Computation

- Big O notation is used to describe the complexity of a function or algorithm.
- It models the number of operations required as the input size increases.
- In a polynomial, the variable is raised to a power: n^a , where a is a fixed constant.
- In an exponential function, the variable **is** the exponent: 2^n



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