Ratsub

A recursive graphics language

Adam Ponting

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1. Ratsub tutorial

Ratsub is a programming language for drawing pictures using recursion and subdivision. A Ratsub program describes an initial shape, how to subdivide it into other shapes, and how long to keep subdividing. The shapes are made of points, which are joined with straight lines. When a shape reaches the maximum recursion level, specified in the shell command, the edge or interior of the shape, or both, are drawn.

Getting started

For writing Ratsub programs you need three things—pen and paper to do sketches, a shell terminal to run commands, and a text editor to enter programs.

Open a text editor to enter Ratsub programs into, like SublimeText, VS Code, TextEdit, NotePad, TextWrangler etc—not a word processor, which may save text as rich text, MS Word or some other format. We want plain text files.

The Ratsub program on the right (yes, that's the whole program!) produces a black square with a white border.

Save it as test.sdv in the subdiv folder. In the shell, cd to the subdiv folder, then running the shell command ratsub test 0 should produce a PNG image in the same folder. In the terminal you should see something like this:

def sq 4

```
$ ratsub test 0
test 0
Making test-0.png...
Done.
```



If nothing happened, the error message should say why not, or at least where in the program the compiler thinks an error is.

Next, type in this program, pressing ENTER after every line, including the last:

The indentation after the first line isn't necessary—it just makes the programs easier to read.

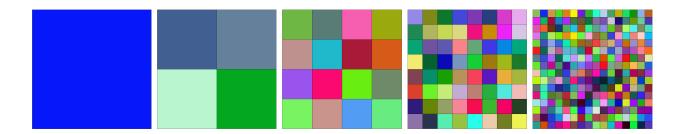
Save it as test.sdv, then on the command line enter:

```
def sq 4
  rand
  p4..7 p0.. 1/2 p1..0
  sq :415c
  sq :c526
  sq :04c7
  sq :7c63
```

\$ ratsub test 0 4

Five .png images, named test-0.png to test-4.png, should appear in the subdiv folder.

The images should look something like this:



Levels

As a Ratsub program runs, shapes are always called with an implicit level parameter, initially 0 for the first shape in the program, and a number of point parameters, which are implicit for the first shape.

A Ratsub program must be called with a level parameter indicating the maximum number of recursion levels to perform. The first shape in the program is level 0 the first time. The shapes it calls (other shapes, or itself, or both) are level 1. The shapes they call are level 2, etc.

When a shape is called at the maximum recursion level, it is drawn with its current colour setting. Nothing is drawn until the maximum level is reached—except using the draw command, which draws a shape immediately.

The shape calls are done *depth-first*, i.e. the first shape called goes all the way to max recursion depth before the second shape is called. And the order shapes are called affects what is on top, what is underneath. That can change the appearance of some programs entirely.

After 10 or 20 levels, the shapes are usually too small too see, and can take a long while to draw if there are millions of them.

The sketch

The first step in writing a Ratsub program is to *make a sketch* of your idea on paper. Draw the initial shape and the shapes it will call or be divided into. Then number the points, preferably in a way that can be efficiently coded.

2. The structure of Ratsub programs

A Ratsub program is made of an optional preamble, followed by one or more shape definitions.

Initial points are defined with x,y coordinates, and other points are affine combinations of them, e.g.

```
p4 p0 .5 p1
```

The 0.5 means p4 will be the average or midpoint of the two, halfway from p0 to p1 — mathematically, $\frac{p0+p1}{2}$. Changing the .5 to various other numbers will get you points on the line between p0 and p1.

```
p4 p0 0 p1 means p4 is at p0.
p4 p0 1 p1 means p4 is at p1.
```

p4 p0 2 p1 means go from p0 to p1, then go the same distance again to reach p4.

You need to use left and right (see p. 14) to make new points off the line between p0 and p1.

Preamble

Defining initial points

Initial points became the parameters of the first shape, the first time through. A square needs 4 initial points, a hexagon 6 etc.

```
A single initial point is set like so: p0 100 100
```

They must be numbered in order, starting from 0.

Defaults: If p0 is omitted, it's set to 0,0. If no initial points are set at all, they default to the 4 points of pbox, i.e. pbox 0 0 100 100.

pbox

The four points forming a (non-tilted) rectangle can be set with pbox *a b c d* where *a*,*b* is the lower left vertex and *c*,*d* the upper right.

Short form	is short for							
pbox c d	pbox 0 0 c d							
pbox	pbox 0 0 100 100							

pgon

```
pgon n r \theta
```

This sets the vertices of a regular polygon as the initial points. e.g.

```
pgon 5 50 20
```

makes p0 to p4 the 5 vertices of a regular pentagon, centred at (0,0) with radius 50, with p0 at 20° up from the x-axis, and the other points following anti-clockwise.

Defaults: If θ is omitted, it's set to 0, i.e. p0 will be at (r,0).

Shape definitions

Defining new points

New points can defined by saying how far the point is along the line from one existing point to another, e.g.

```
p2 p0 1/2 p1
defines a new point p2, halfway from p0 to p1. This also can be written
p2 p0 0.5 p1 or
p2 p0 .5 p1
```

par

```
p3 par p0 p1 p2
```

New points can also be defined using par, which here makes a new point p3, the same direction and distance from p2 as p1 is from p0. i.e. it draws the 4th point of a parallelogram, given the first 3.

New point numbering

A shape's first new point must be numbered to come immediately after the shape's parameter points (or the initial points, for the first shape). e.g. for

```
def square 4
```

the parameter points—the points the shape is called with—will be named p0, p1, p2 and p3, and the first new point must be p4.

Defining multiple new points

Short form	Equivalent to							
p46 p05 p1	p4 p0 .5 p1							
	p5 p1 .5 p2							
	p6 p2 .5 p3							
p46 p05 p10	p4 p0 .5 p1							
	p5 p1 .5 p2							
	p6 p2 .5 p0							

That second form is handy for creating midpoints on each side of a shape with one command.

Shape calls

shape points options

A shape may have no shape calls. That means *draw it right away*, without waiting for the level to reach the max.

Short forms

Short form	Short for					
<i>shape</i> p15	shape p1,2,3,4,5					
shape :14253	shape p1,4,2,5,3					

N.B. The :14253-type short form can only be used if every point in the list has a single-digit number! p8,9,10 cannot be abbreviated to :8910.

3. Colouring

Colours are represented as *RGB* (red green blue), with the 3 values between 0 (off) and 1 (fully on) inclusive. Colours can be set with R G B values or with a colour name.

Colour can be applied in Ratsub in two different places in a shape definition:

• shape colour - usually in the line below the initial def line.

def sq 4 red tri :012

• shape call colour. This sets the called shape's colour.

def sq 4 tri :012 red

Unless onlyedges is set, every shape is drawn with some colour. A shape's colour is either

- 1. its shape colour, if it has one
- 2. the colour given to it by the shape call it was called with,
- 3. otherwise, the default colour—either black, or mid-grey (0.5,0.5,0.5) if colour-add mode is used.

Colouring syntax examples:

Метнор	Shape colouring	SHAPE CALL COLOURING
basic	red	tri :012 red
initial point shading	ip0 red	
gradient shading	p0 red p1 green	
colour-add mode		tri :012 + 1 2 -1
colour operator		tri :012 not

Basic colouring

Basic shape colouring

r g b c (same as *c c c*) *colourname*

Default: Black.

Basic shape call colouring

If a shape call has a colour, e.g.

sq :0123 red

it will pass that colour, otherwise it will pass its shape's colour, if it has one. Otherwise it will pass the colour its shape was passed when it was called.

Random colouring

rand crand

rand makes a random colour, different each time through the shape/shape call. crand is the same random colour each time.

Random range colouring

```
rand r_{min} r_{max} g_{min} g_{max} b_{min} b_{max} crand r_{min} r_{max} g_{min} g_{max} g_{min} g_{max}
```

These make a random colour with red in the range $r_{min} \dots r_{max}$, etc.

Shape shading

Apart from giving each shape a fixed flat colour, there are two ways to colour shapes with a varying shade.

Initial point shading

ipn r g b
ipn colourname

Initial point shading colours shapes by how close they are to a set of initial points.

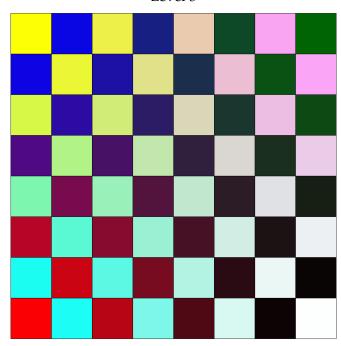
Specify, in a shape's definition, a set of initial points (the fixed points defined in the preamble) and their colours. When the shape is called, it's coloured by these points, proportional to how close it is to them.

Extra initial points to control shading can be added to the preamble, and they will be ignored by the first shape, which only takes as many points as it's defined to need.

Multiple shading colours can be defined on one line.

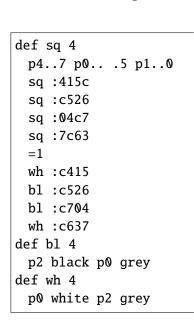
Level 3

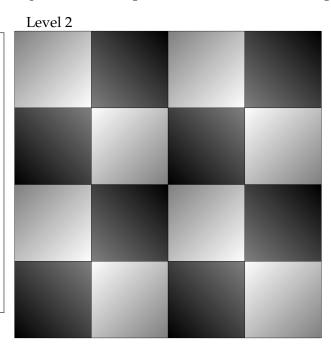
def s1 4
ip0 red ip1 blue
ip2 dark green ip3 black
p47 p05 p10
s2 :415c
s1 :c526
s1 :04c7
s2 :7c63
def s2 4
ip0 cyan ip1 yellow
ip2 violet ip3 white
p47 p05 p10
s2 :415c
s1 :c526
s1 :04c7
s2 :7c63



Gradient shading

Similar to initial point shading, but uses the points from the current shape.





Suggestion: If you need to define new points to use with gradient shading, you can define them in the parent shape and include them as points in the shape call parameters.

Shape call colouring

Colour-add mode

```
shapename points + r g b
shapename points - r g b
shapename points + c
shapename points - c
```

This colours a shape depending on its call path down through the levels—on the add-colours of its ancestor shapes. It's used at the end of shape calls, e.g.

```
sq : 0123 + 123
```

makes the red of the new sq shape 1/10th brighter, the green 2/10ths brighter, and the blue 3/10ths brighter. If the present shape's colour is (R,G,B), this calls sq with the colour (R+r/10,G+g/10,B+g/10). Because the colour adjustments are usually small fractions, the units are 10ths.

```
sq:0123 + 1 means the same as sq:0123 + 1 1 1.
```

N.B. The initial shape takes its shape colour, but after that any shape colours are ignored in favour of the colour passed to it by the shape that called it.

Random

shapename points rand

Colour operators

These are used in shape calls to transform the shape's colour

Operator

```
not/! R G B \Rightarrow 1-R 1-G 1-B.

Black (0 0 1) becomes white (1 1 1), blue (0 0 1) becomes yellow (1 1 0) etc.

rot Rotate colours to the right. R G B \Rightarrow B R G.

rot2 Rotate right twice/rotate left. R G B \Rightarrow G B R.
```

4. Random numbers

Random numbers can be used in shape definitions for setting colours, and with distances, for setting new points. *Random ranges* allow fine control over the desired random numbers.

rand

```
p6 p0 rand p1
```

— this places p6 randomly somewhere on the line between p0 and p1 (including perhaps on those points). This random number is different every time the shape is called.

crand

```
p6 p0 crand p1
```

— this places p6 randomly somewhere on the line between p0 and p1 (including perhaps on those points). This random number is constant - the same every time the shape is called.

srand

srand n

— this seeds the random number generator. With the same n, the random numbers (and thus image) will be the same each time the program's run. For random numbers different each time without having to use srand, use random and crandom instead of rand.

Random range

new points

colours

5. More commands

draw

There are two ways of drawing a shape immediately—regardless of current level:

• Write draw instead of a shape name in a shape call. If a draw call has a colour, e.g. draw :0123 red

it will use that colour, otherwise it will use its shape's colour, if it has one. Otherwise it will use the colour its shape was passed when it was called.

• A shape without any shape calls will be drawn immediately.

Draw is most useful when the child shapes only cover part of the parent, or lie outside it.

grid

 $\operatorname{grid} \theta$

grid transforms the usual square grid into a grid with the y-axis θ degrees from the x-axis. It only affects the initial points. e.g.

Turning left and right

newpointdef left a newpointdef right a

Turning is the only way to make a new point that's not on the line between its 2 defining points. p2 p0 .5 p1 left .25

This travels halfway from p0 to p1, then turns left and travels half that distance—the .25 means 1/4 the distance *between p0 and p1*.

flip

shapecall flip

Used to call a flipped-over version of a shape, especially a line, for example in line fractals like the Koch curve, and IFS.

Flipping a shape only makes a difference if left or right are used in the shape's new point definitions.

Wait shapes and wait

Used at the end of shape calls:

wait makes a wait shape, i.e. wait 1 level then call.

wait n makes n linked wait shapes, i.e. wait n levels then call.

temp

Give example of pics needing 2, 3 wait shapes. Also multiple wait shapes, calls to different numbers in different places.

Conditionals

```
>n =n >-n =-n
```

With > or =, you can do different shape calls depending on the current level.

<pre>def sq 4 tri :012 tri :032 >2</pre>	This does the first two shape calls if the current level<=2, and the second two if it's >2. i.e. :
tri :123 tri :103	If level>2 then do C and D, else do A and B

A negative branch number -n means n levels before the maximum level.

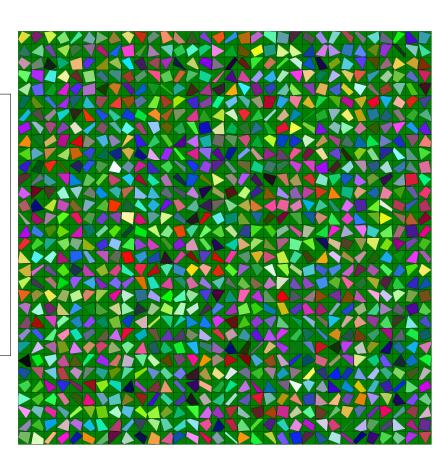
```
def sq 4
tri :012
tri :032
>-2
tri :123
tri :103

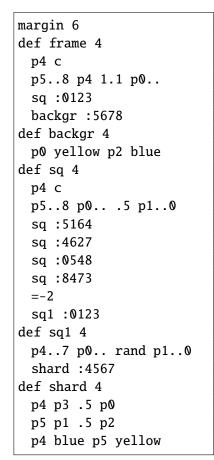
Here the second branch is taken when the current level is more than 2 less than the maximum level. For example, if the program is run with "ratsub myprog 8" then the second branch is taken when the current level >6.
```

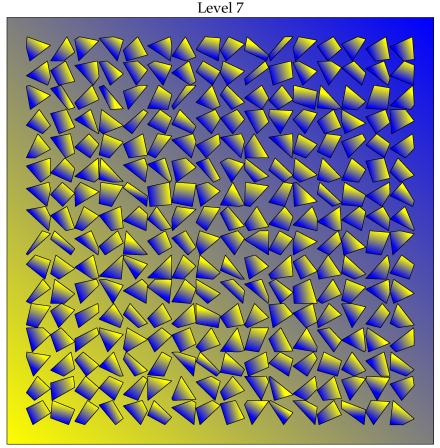
Similarly, =5 means "take this second branch when the current level is 5"; =-5 means "take this second branch when the current level is 5 less than the maximum level".

```
width .02
def sq 4
p4 c
p5..8 p0.. .5 p1..0
sq :5164
sq :4627
sq :0548
sq :8473
=-2
sq1 :0123
draw :0123 green
def sq1 4
p4..7 p0.. rand p1..0
draw :4567 rand
```

Level 7







6. Drawing in 3D with pcube

pcube $r \theta_x \theta_y \theta_z z_{\text{viewpoint}} z_{\text{viewplane}}$

This adds 8 initial points, the vertices of a cube seen in perspective. The image is drawn as if the viewer's eye is at $(0,0,z_{\text{viewpoint}})$ and the viewplane is the plane $z=z_{\text{viewplane}}$.

N.B. The algorithm involves dividing by $z - z_{\text{viewpoint}}$, so will make an error if that's 0, i.e. if you get so close that your eye hits a vertex of the cube!

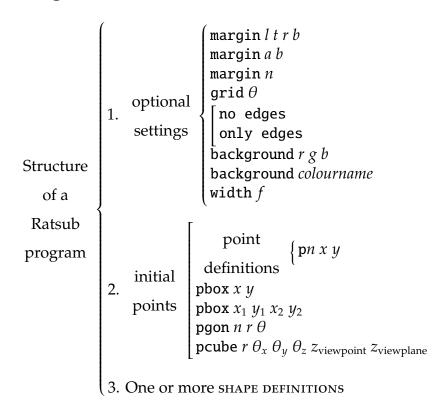
7. Ratsub language reference

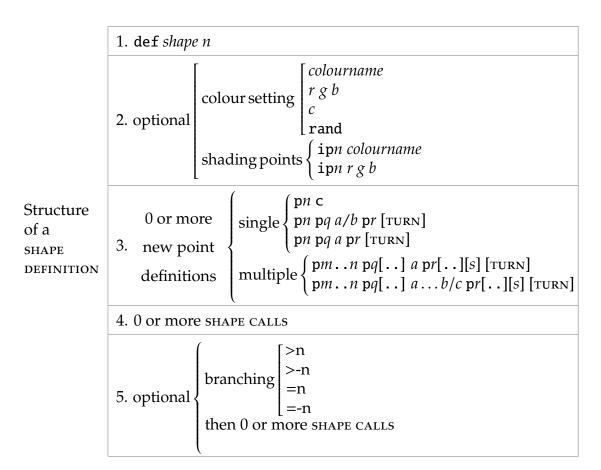
Levels

Each Ratsub program specifies a (theoretically infinite) number of pictures, depending on the level parameter which sets the maximum recursion level/call stack depth. The first shape in a program calls others, they call others etc. When the recursion reaches *N* levels deep, a shape instead draws itself using its parameter points and colour settings.

This can be bypassed with the draw command in a shape's definition—the shape will be drawn immediately.

Program structure





Program structure in detail

Optional settings

grid θ Makes the angle between the x and y axes θ degrees,

for the initial point definitions.

margin *num* set width of the margin around the picture

margin *l t r b* set width of the left, top, right, bottom margin

margin *a b* a is left/right margin, *b* is top/bottom margin.

no edges no shape edges are drawn

only edges only edges are drawn

background *r g b* colour of the background bounding box

width *num* set line width for drawing shape edges.

Initial point definitions

These define the vertices of the initial shape, which are initially passed as parameters to the first shape definition. If grid is set then these points will be affected. Use " to repeat an x- or y-coordinate from the line above.

p3 5.5 2.3 defines point 3 at 5.5,2.3

pbox *a b c d* defines four points, the corners of a rectangle numbered

clockwise from lower left. The new points p0...3 are:

a,b a,d c,d c,b.

 $\operatorname{\mathsf{pbox}} c d$ short for $\operatorname{\mathsf{pbox}} \operatorname{\mathsf{0}} \operatorname{\mathsf{0}} c d$

pbox short for pbox 0 0 100 100

pgon $N r \theta$ Defines the N points of a polygon, with one more point

at the centre 0,0. The point have radius r and p0 is at θ degrees. The N points are numbered anticlockwise.

pcube $r \theta_x \theta_y \theta_z z_{\text{viewpoint}} z_{\text{viewplane}}$ Defines the 8 points of a cube in 3D.

Shape definitions

These define shapes and how they'll be subdivided into other shapes. Shapes can also be subdivided into themselves, as in the example program above.

Initial point definitions and the first shape

Ratsub manual: The first shape defined is drawn with the initial points from the preamble, using as many points as it needs, e.g. "def sq 4" defines a shape "sq" with 4 points, which will

take p0, p1, p2 and p3 of the initial points the first time it's called, and the 4 points it's called with each time after that. So only the first shape defined can take initial points as parameters. After the first shape has been called once, the initial points can only be used by shapes for their shading. "p0" then means, the first parameter in the call to that shape, and not the first initial point.

The def line

def shape N

N is the number of points in the shape, the number parameters it takes from the shape that calls it. The first shape, the first time it's run when the program starts, takes the initial points (defined in the preamble) as its parameters.

Shape colour setting (optional)

colourname	set the fill colour.
r g b	set the shape colour to red r , green g , blue b . (colour values are between 0 and 1)
c	set the shape colour to red c , green c , blue c .
rand	random colour
$+ \Delta r \Delta g \Delta b$	
$-\Delta r \Delta g \Delta b$	use colour-add mode

Shading point definitions

ip0 1	gb	Assigns the colour $r g b$ to the initial point 0, the first defined in the preamble (Not the first parameter of the shape!)
in0	3roh	Assign the same colour to initial points 0.1.2.3

ip0...3 rgb Assign the same colour to initial points 0,1,2,3.

New point definitions

	Defines
p2 p0 1/3 p1	a new point p2, 1/3 of the way from p0 to p1.
p2 p0 0.4 p1	a new point p2, 4/10 of the way from p0 to p1.
p2 p0 rand crand random p1	a new random point somewhere on the line between p0 and p1.

New point definition short forms

```
uses the same fraction/number as the previous line.
p3 p1 " p2
p4..6 p0 1..3/4 p1
                       p4 p0 1/4 p1
                       p5 p0 2/4 p1
                       p6 p0 3/4 p1
p4..6 p0 1,2,4/5 p1
                       p4 p0 1/5 p1
                       p5 p0 2/5 p1
                       p6 p0 4/5 p1
p5...7 p1.. .95 p0
                       p5 p1 .95 p0
                       p6 p2 .95 p0
                       p7 p3 .95 p0
p5..7 p0 .95 p1..
                       p5 p0 .95 p1
                       p6 p0 .95 p2
                       p7 p0 .95 p3
p5..7 p0.. .95 p1..
                       p5 p0 .95 p1
                       p6 p1 .95 p2
                       p7 p2 .95 p3
p5..7 p0.. .95 p1..0 p5 p0 .95 p1
                       p6 p1 .95 p2
```

p7 p2 .95 p0

This last form is frequently useful, e.g. for the midpoints of the sides of a pentagon:

```
pgon 5 50 0
def pent 5
p5..9 p0.. 1/2 p1..0
```

as the last side is from p4 back to the first point p0.

8. Colour names

These colour names can be used in Ratsub instead of RGB colour values.

alice blue antique white aqua aquamarine azure beige bisque black blanched almond blue violet blue brown burly wood cadet blue chartreuse chocolate coral corn silk cornflower blue

crimson
cyan
dark blue
dark cyan
dark golden rod
dark gray
dark green
dark grey
dark khaki

dark magenta dark olive green dark orange dark orchid dark red dark salmon dark sea green dark slate blue dark slate gray dark slate grey dark turquoise

dark violet

deep pink

dim gray

deep sky blue

dim grey dodger blue firebrick floral white forest green gainsboro ghost white gold

golden rod gray

green yellow green grey honeydew hot pink indian red indigo ivory khaki

lavender lawn green lemon chiffon light blue light coral light cyan

lavender blush

light golden rod yellow light gray light green light grey light pink light salmon light sea green light sky blue light slate gray

light sky blue
light slate gray
light slate grey
light steel blue
light yellow
lime green
lime
linen
magenta
maroon

medium aquamarine medium blue

medium orchid
medium purple
medium sea green
medium slate blue
medium spring green
medium turquoise
medium violet red
midnight blue
mint cream
misty rose
moccasin

navajo white navy old lace olive drab olive orange red orange orchid

pale golden rod pale green pale turquoise pale violet red papaya whip peach puff peru pink plum powder blue purple red

rosy brown
royal blue
saddle brown
salmon
sandy brown
sea green
sea shell
sienna
silver
sky blue

slate blue slate gray slate grey snow spring green steel blue

tan teal thistle tomato turquoise violet wheat white smoke white yellow green yellow