Before you start:

Homework Files

You can download the starter files for coding as well as this *tex* file (you only need to modify *home-work2.tex*) on canvas and do your homework with latex (recommended). Or you can scan your handwriting, convert to pdf file, and upload it to canvas before the due date. If you choose to write down your answers by hand, you can directly download the pdf file on canvas which provides more blank space for solution box.

Submission Form

For homework 2, you need to upload a pdf file in the following format:

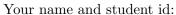
• VE281_HW2_[Your Student ID]_[Your name].pdf

Please strictly follow the format given above!!! Everyone who does not obey the format will get 2 points deduction!!!

Notes: No extra folders (extracting this tar should only give you two files), no space in your name (use underscore(_) instead), no brackets. One example for name of pdf:

VE281_HW2_518370910000_Run_Peng.pdf

Estimated time used for this homework: **3-4 hours.**



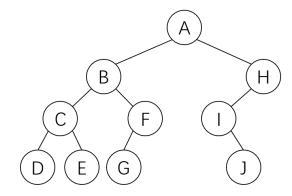
Tour name and student id

Solution:

1 Tree Traversal (26 points)

1.1 Given A Tree (16 points)

Given a binary tree below, please write out the following traversals:



(a) Pre-order depth-first traversal. (4 points)

Solution:

(b) Post-order depth-first traversal. (4 points)

Solution:

(c) In-order depth-first traversal. (4 points)

Solution:

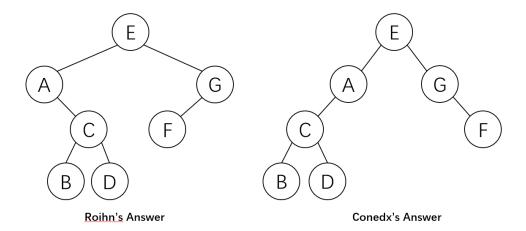
(d) Level-order traversal. (4 points)

Solution:

1.2 Draw The Tree (10 points)

Solution:					
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Roihn and Conedx both provide their plot of the unknown trees.



Their answers are totally different, but seem to be both correct. Can you explain why such a case happens? (2 points)



2 True or False (20 points)

Please judge whether the following statements are **TRUE** or **FALSE**. You can briefly state your reason if you would like to get partial points. Each question takes 2 points.

a) A complete tree is a tree where every node has either 0 or 2 children.

Solution:			

b) A complete tree is a tree where every level except the last is necessarily filled, and in the last level, nodes are filled in from left to right.

i) Proceeding from the bottom of the heap to the top, while repeatedly calling percolateDown()

can initialize a min-heap.

	Solution:
j)	Proceeding from the top of the heap to the bottom, while repeatedly calling percolateUp() can not initialize a min-heap.
	Solution:
3	Hea——p! (23 points)
Сс	onsider a min-heap represented by the following array:
	$\{63, 74, 67, 85, 91, 94, 72, 88\}$
th	rform the following operations using the algorithms for binary heaps discussed in lecture. Ensure at the heap property is restored at the end of every individual operation. r the following operations, please briefly describe what and how you use the given functions:

percolateUp() and percolateDown(), and show the result of the heap after each operation in

either tree form or array form.

b)	Push the value of 79 into this min-heap. (4 points)
	Solution:
	Update element 85 to have a value of 58 (Suppose you have the access to each element). (5 points)
	Solution:
J)	Demons the win element from the beau (5 mainte)
a)	Remove the min element from the heap. (5 points)
	Solution:

) Update element 67 to have a value of 96 (Suppose you have the acces	s to each element) (5 points
Solution:	
Binary Search Tree (30 points)	
.1 Simple simulation (14 points)	
erform the following operations to construct a binary search tree. Ster each operation in either tree form or array form.	Show the result of the BS7
Insert 24, 29, 22, 25, 19, 32, 15, 37 (3 points)	
Solution:	

b)	Delete 22 (3 points)
	Solution:
c)	Delete 29 (3 points)
	Solution:
d)	Insert 22 (3 points)
	Solution:

Solution:							
2 Let's BS	Γ! (16 points)	<u> </u>					
its inorder suc	n a binary search cessor. Given a porder successor if 4 points)	pointer to the	ne node to	be deleted	, what is the	time con	plexity of
Solution:							
	you want to ins				binary search	n tree. H	How man
Solution:							

- c) Consider a tree that satisfies the following conditions:
 - 1. The tree is a binary search tree of integers.
 - 2. The number of elements in the root node's left and right subtrees are the same.
 - 3. There are no duplicate values in the tree.
 - 4. The first element of an inorder traversal of the tree is 11.
 - 5. The last element of an inorder traversal of the tree is 24.
 - 6. The last element of a postorder traversal of the tree is 16.

What is the largest possible integer you can attain by summing up all the values in a tree that satisfies the above constraints? (6 points)

Solution:		

Reference

Assignment 3, VE281, FA2020, UMJI-SJTU.