Relative risk and odds ratio

Exercise example from the "Seeing Through Statistics" book

Table 12.10

Age and Ghost Sitings

| | Reportedly Has Seen a Ghost | | |
|-----------------|-----------------------------|------|-------|
| | Yes | No | Total |
| Aged 18 to 29 | 212 | 1313 | 1525 |
| Aged 30 or over | 465 | 3912 | 4377 |
| Total | 677 | 5225 | 5902 |

Data Source: The Roper Organization, 1992, p. 35.

The **percentage** of the younger group who reported seeing a ghost:

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Data Source: The Roper Organization, 1992, p. 35.

That's the row corresponding to the younger group: 212 out of 1525 reported yes \rightarrow 212/1525 = 0.139 x 100 = 13.9%

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The **proportion** of the older group who reported seeing a ghost:

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That's the row corresponding to the older group: 465 out of 4377 reported yes \rightarrow 465/4377 = **0.106**

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a. The <u>risk</u> of reportedly seeing a ghost in the younger group:

$$\rightarrow$$
 212/1525 = **0.139**

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What is the *relative risk* of reportedly seeing a ghost for the younger group compared to the older group?

→ Risk for **younger** → Risk for **older**
$$212/1525 = 0.139$$
 $465/4377 = 0.106$

 \rightarrow Relative risk = Risk younger / Risk older = $0.139 \div 0.106 = 1.31$

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Data Source: The Roper Organization, 1992, p. 35.

What is the relative risk of reportedly seeing a ghost for the younger group compared to the older group?

 \rightarrow Relative risk = Risk younger / Risk older = $0.139 \div 0.106 = 1.31$ We would say: *People aged 18 to 29* are 1.31 times as likely to report seeing a ghost as those over 30 8

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What is the <u>odds</u> of reportedly seeing a ghost to not seeing one in the younger group?

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What is the <u>odds</u> of reportedly seeing a ghost to not seeing one in the younger group?

Odds = 212 to
$$1313 = 212/1313 = 0.16$$

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What is the <u>odds ratio</u> of reportedly seeing a ghost to not seeing one in the younger group compared to the older group?

Odds ratio =
$$(212/1313) \div (465/3912) = 1.36$$

Odds of seeing a ghost were 1.36 higher for the younger group.

Summary of Risk, Relative Risk, Odds, and Odds Ratio Computations

Generally, risk and odds are used to compare the responses for a category of interest with the responses for a baseline category. Let's represent the numbers as follows.

| | Response 1 | Response 2 | Total |
|-------------------------|----------------|----------------|------------------|
| Category of Interest | A_1 | A_2 | \mathbf{T}_{A} |
| Baseline | B_1 | \mathbf{B}_2 | T_{B} |

The only difference between risk and odds is whether Response 2 or Total is used for the comparison. *Risk* compares Response 1 to the Total. *Odds* compares Response 1 to Response 2.

- Risk of Response 1 for the Category of Interest = A_1/T_A
- Odds of Response 1 to Response 2 for the Category of Interest = A_1/A_2
- Relative risk = $\frac{A_1/T_A}{B_1/T_B}$
- Odds $ratio = \frac{A_1/A_2}{B_1/B_2}$