

Q1:

Let  $x$  be arbitrary and assume  $x \in A \setminus C$ ,

then  $x \in A \cap \neg C$

Given that  $A \subseteq B$ , so  $\forall x (x \in A \rightarrow x \in B)$ ,

Since  $x$  is arbitrary,  $x \in B \cap \neg C$  holds, then  $A \setminus C \subseteq B \setminus C$  is true.  $\square$

Q2:

a)  $x \neq 3$  could not lead to  $x^2 \neq 9$ , because if  $x = -3$ ,  $x \neq 3$  but  $x^2 = 9$ , so  $x^2 - 9 = 0$  and we cannot divide both sides by  $x^2 - 9$ .

b) We can pick  $x = -3$ ,  $y = 1$  for an counter example, then  $x^2 y = 9$ ,  $9y = 9$ ,  $x^2 y = 9y$  and  $y \neq 0$ .

Q3: To proof that  $y \neq 0 \rightarrow x \neq 0$ .

Let  $x = 0$ , given that  $xy = 2x^2 - y$ ,  $y = 0$ .

Therefore, since  $x = 0 \rightarrow y = 0$ ,  $y \neq 0 \rightarrow x \neq 0$  holds.  $\square$