

Lecture 15.

e.g. For any integer n , $6|n \iff 2|n \wedge 3|n$.

Proof: Let n be an arbitrary integer. Assuming $6|n$. So

there exist an integer k such that $n = 6k = 2(3k) = 3(2k)$.

e.g. Suppose $A \cap (B \setminus C) = (A \cap B) \setminus C$

Given Goal

$$\text{For } x \in A \cap (B \setminus C) \iff x \in (A \cap B) \setminus C$$

$$\Rightarrow \text{Goal 1: } \rightarrow \quad \text{Goal 2: } \leftarrow$$

For goal 1: $x \in A \cap (x \in B \wedge x \notin C)$ goal 2: $(x \in A \wedge x \in B) \wedge x \notin C$

Proof: Let x be arbitrary, Then

$$\begin{aligned} x \in A \cap (B \setminus C) &\iff x \in A \cap (x \in B \wedge x \notin C) \iff (x \in A \wedge x \in B) \wedge x \notin C \\ &\iff x \in (A \cap B) \setminus C \end{aligned}$$

Since x is arbitrary, -----.

§ 3.5. Proofs involving \setminus

To use a given of form $P \vee Q$, break the proof in two cases: 1) P to the given 2) Q to the given.

Template:

case 1: Assume P - Proof -

case 2: Assume Q - Proof -

- We know $P \vee Q$, these cases are exhaustive. therefore, the goal is true.

$$x^2/4 = k_1 \quad / k_2 \geq 1.$$