

ECON3102-005

CHAPTER 4: CONSUMER AND FIRM  
BEHAVIOR

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- A particular combination  $(c, l)$  of  $c$  and  $l$  is called a consumption bundle.

# THE REPRESENTATIVE CONSUMER'S PREFERENCES

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- In fact, the actual level of utility is irrelevant. What matters is the order of preferences implied by the utility function.



# ASSUMPTIONS ON THE REPRESENTATIVE CONSUMER'S PREFERENCES

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- The consumer likes diversity, i.e. he prefers mixtures to extremes: He would rather have some consumption and some leisure rather than a lot of leisure and no consumption!
- Consumption and leisure are normal goods to the consumer (as opposed to inferior goods!): he consumes more of each as his income goes up.

# INDIFFERENCE CURVES (IC CURVES)

## Definition

An indifference curve connects a set of points that represent bundles among which the consumer is indifferent.

- IC curves are downward sloping (more is preferred to less).

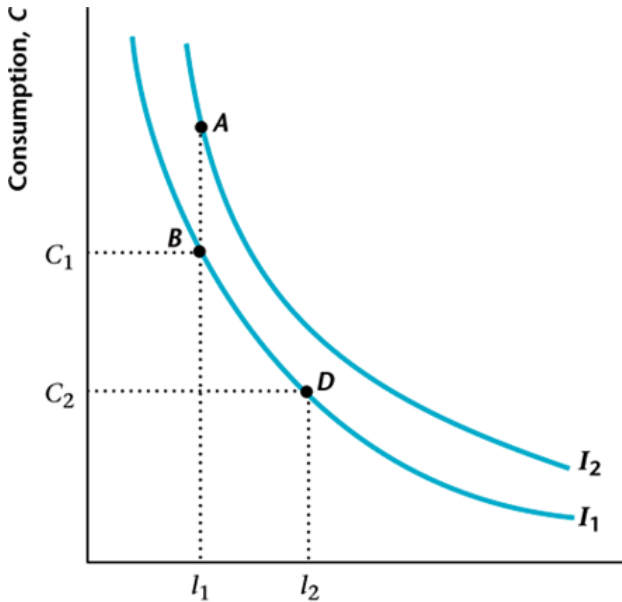
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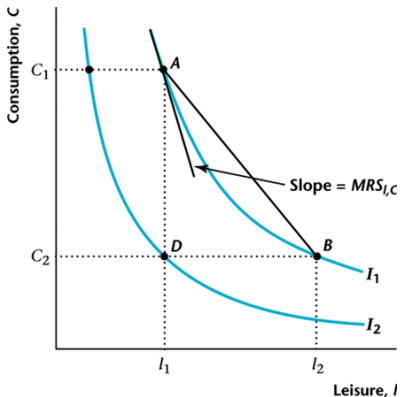
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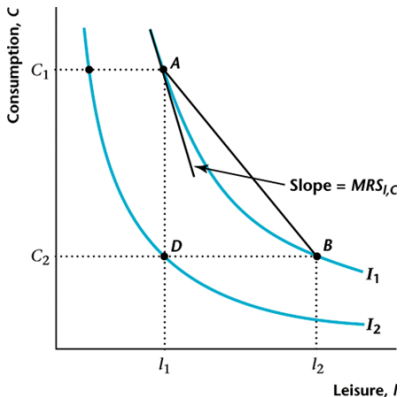


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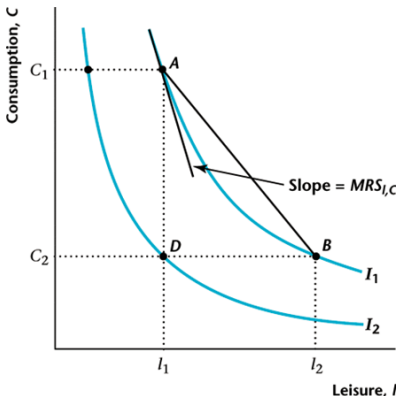




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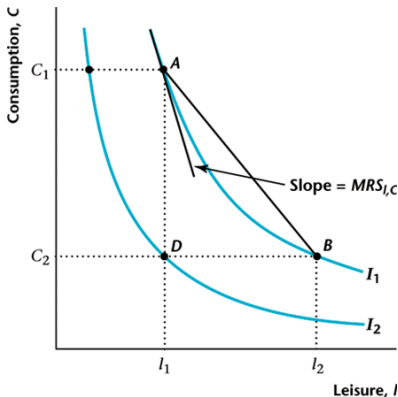


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- As bundle B gets arbitrarily close to bundle A, this rate of substitution becomes  $\frac{\partial c}{\partial l} = -$  the slope of the line tangent to the IC at point A (the derivative of IC at A).

# INDIFFERENCE CURVES

$MRS_{l,c} = -$  the slope of the IC passing through bundle  $(c, l)$ :

# CONSUMER'S TIME CONSTRAINT

- Each period, the consumer has  $h$  units of hours of time available, to allocate between  $l$  units of leisure and  $N^s$  units of work.

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- The time constraint is

$$l + N^s = h$$

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- He receives  $\pi$  units of current consumption as in the form of dividend income from the firm.
- Hence, his disposable income is:

$$wN^s + \pi - T$$

# CONSUMER'S BUDGET CONSTRAINT

- The consumer's budget constraint (BC) is:

$$c = wN^s + \pi - T$$

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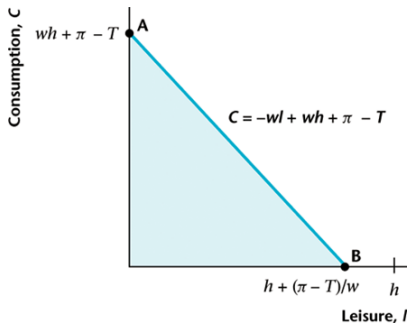
- or,

$$\underbrace{c + wl}_{\text{Implicit expenditure on goods}} = \underbrace{wh + \pi - T}_{\text{Implicit Real Disposable Income}}$$

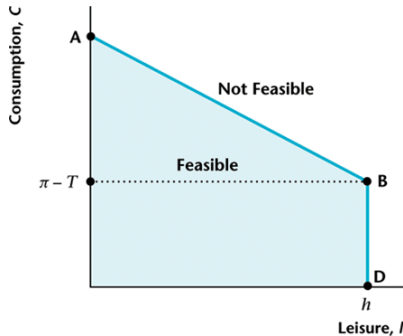
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For convenience, we rewrite the BC as:  $c = -wl + wh + \pi - T$



The Consumer's Budget Constraint  
if  $T > \pi$



The Consumer's Budget Constraint  
if  $T < \pi$

# CONSUMER'S BUDGET CONSTRAINT

Just to show that either case is easy to analyze and that the implications do not change, we will assume in this chapter that  $T < \pi$ . That is, we will be working with the kinked budget constraint.

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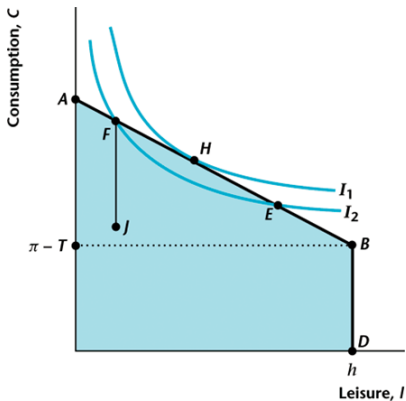
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- We next show that the OCB is the point where the IC is tangent to the budget constraint.



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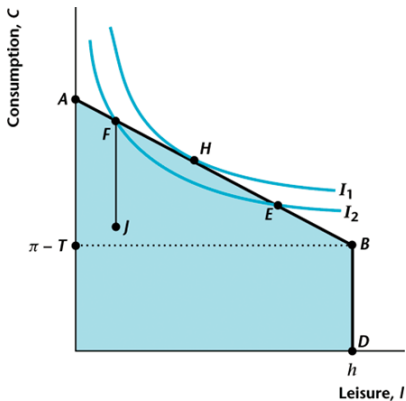
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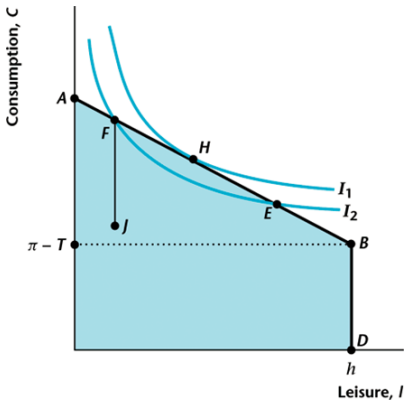
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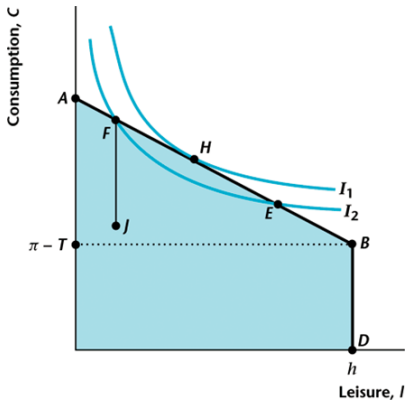


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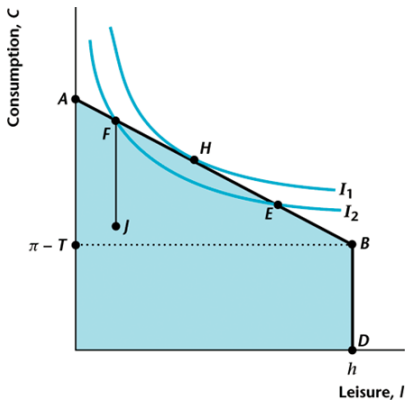
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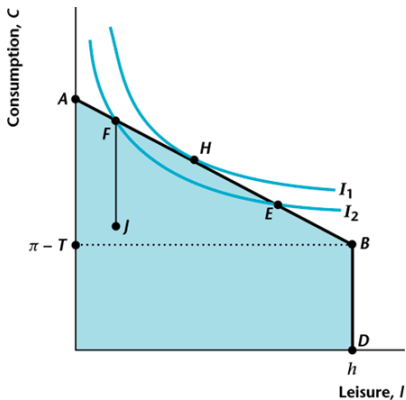
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- the consumer would then be better off if he sacrifices consumption for more leisure.

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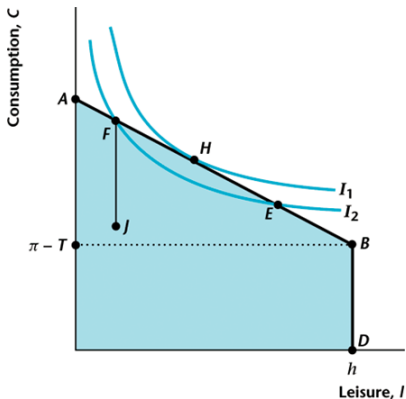


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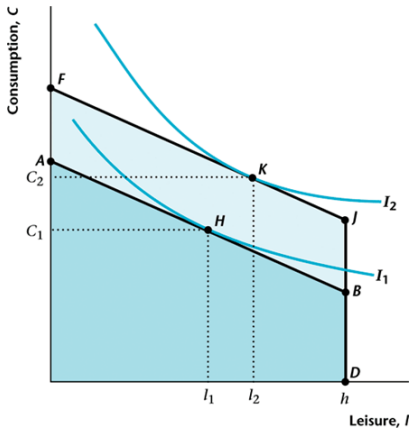
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- Hence, the OCB is the point where:  $MRS_{l,c} = w$ : where the rate at which the consumer would trade consumption for leisure = price of leisure in units of consumption.

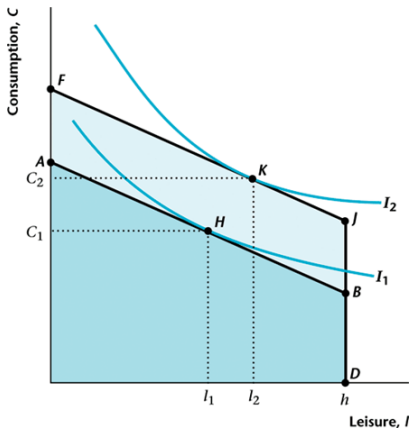
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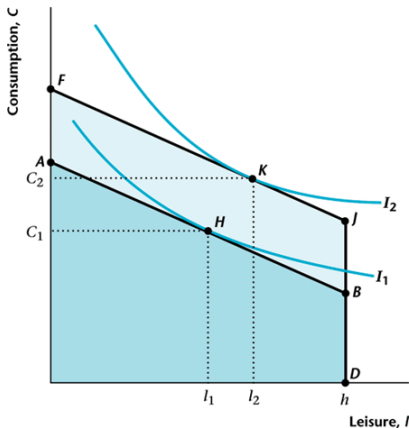


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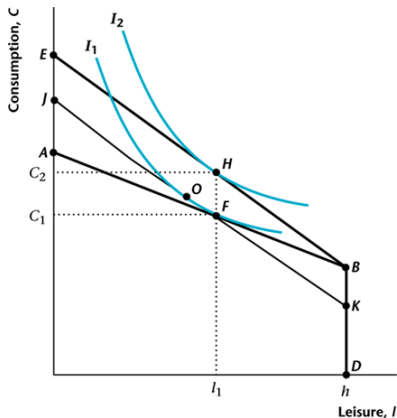
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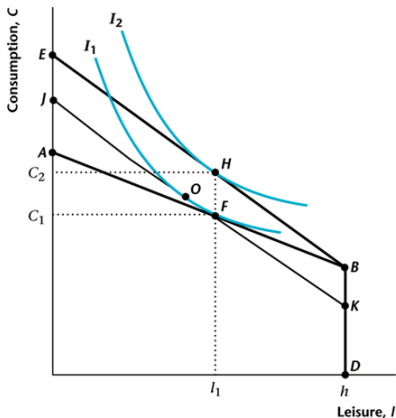
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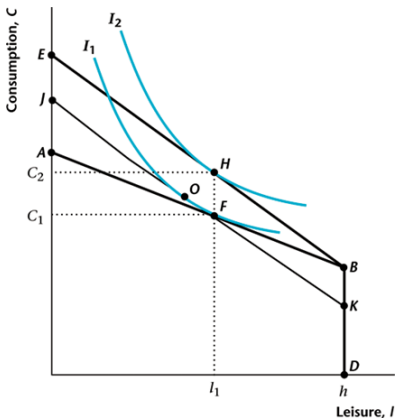


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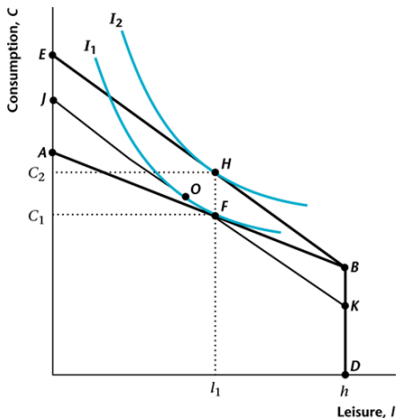


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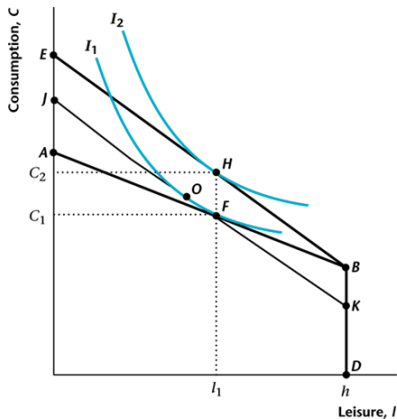
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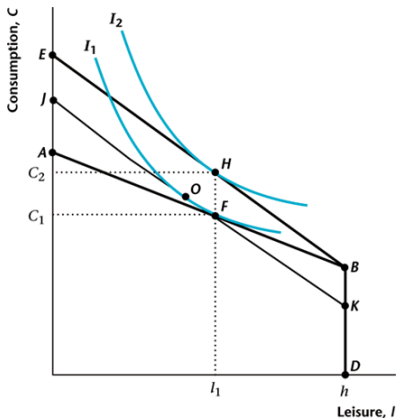
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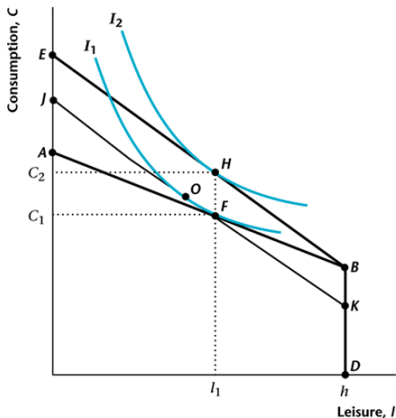
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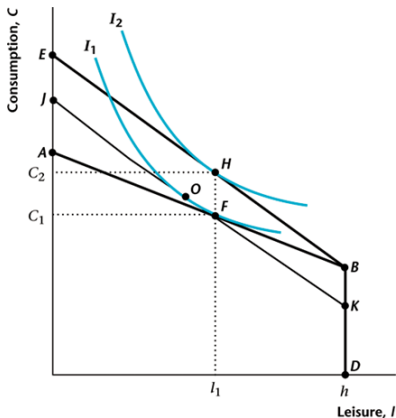
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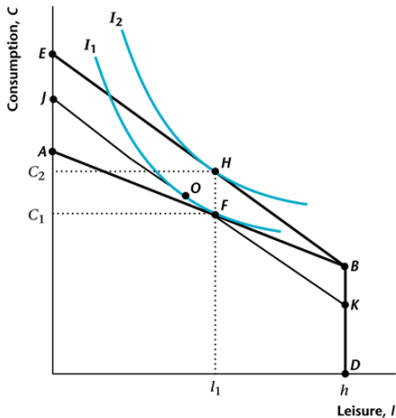


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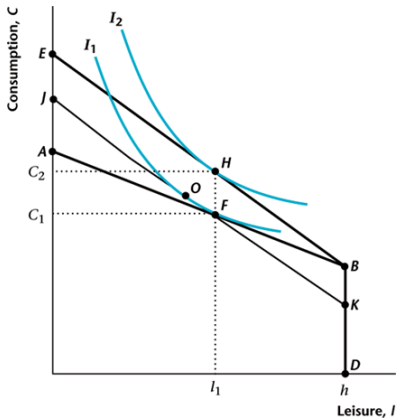


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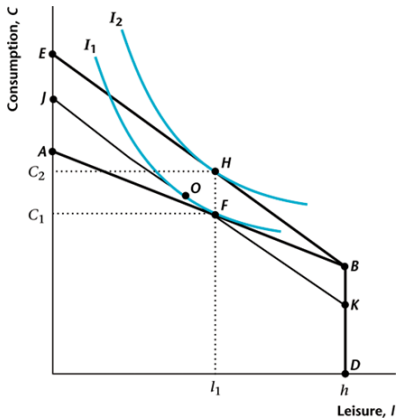
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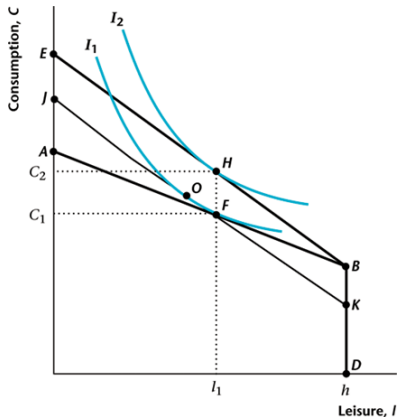
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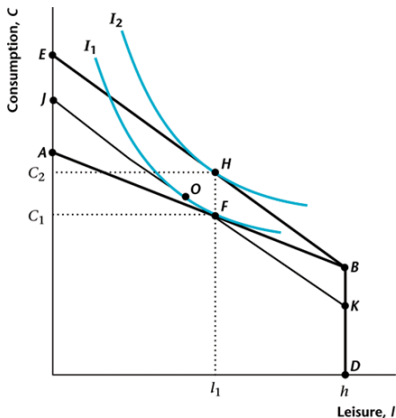
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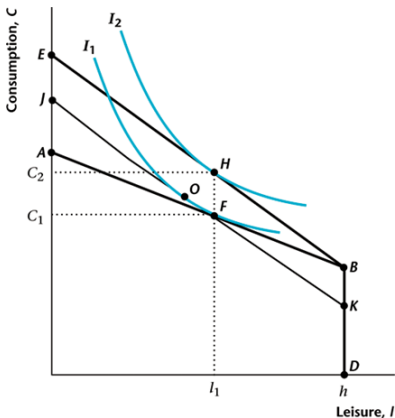


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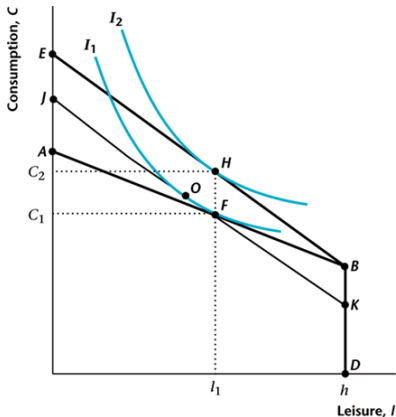
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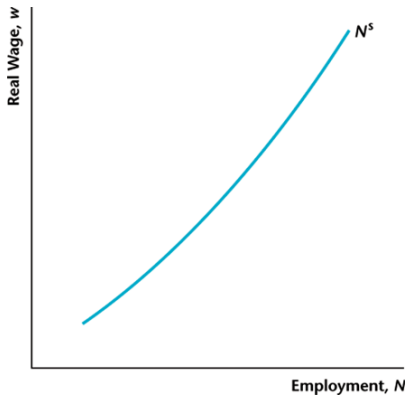


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# LABOR SUPPLY CURVE



- We assume that the substitution effect dominates so that as  $w$  increases, the consumer consumes less leisure and hence works more.

# LABOR SUPPLY CURVE: EFFECT OF AN INCREASE IN DIVIDEND INCOME OR A DECREASE IN TAXES

