

Parameter: a number that describe population

Statistic: a number that can be computed from the sample data

$\mu$ : mean of the population

$\sigma$ : standard deviation of the population

$\bar{x}$ : mean of the sample

$s$ : standard deviation of the sample.

Law of Large Numbers: Draw observation at random from any population with finite mean  $\mu$ . As the number of observations drawn increase, the mean  $\bar{x}$  of the observation tend to approach to  $\mu$ .

Sampling distribution: took every one of the possible sample of a certain size, calculated the sample mean for each, and graphed.

Simulation: using softwares to imitate sampling distribution.

the sampling distribution of  $\bar{x}$  has mean  $\mu$  and standard deviation  $\sigma/\sqrt{n}$

$\Rightarrow$  SRS of size  $n$ , mean  $\mu$  and standard deviation  $\sigma$

Since  $\bar{x}$  is always equals to  $\mu$ ,  $\bar{x}$  is an unbiased estimator

\*  $\bar{x}$  must sample all parts of data.

The larger the population is, smaller the standard deviation of the sampling distribution is.  $\bar{x} = \sigma/\sqrt{n}$ . The variable of the average is less.

The shape of the sampling distribution depends on the shape of the population distribution

$\Rightarrow$  the population distribution is Normal, then the sampling distribution is Normal

individual observation:  $N(\mu, \sigma)$   $\Rightarrow$  sample mean  $\bar{x}$  of the SRS:  $(\mu, \sigma/\sqrt{n})$ .

Central Limit Theorem

$n \uparrow$ , the distribution of sample more like Normal distribution, less like population

$\Rightarrow$  when  $n$  is large, the sample distribution is approximately Normal,  $N(\mu, \sigma/\sqrt{n})$