

## 1.1 Exercise.

### Chapter 1. Sentential Logic (Propositional Logic).

#### Deductive Reasoning & Logical Connectors.

R: It will rain tomorrow.

P: There exist infinite many nature numbers such that  $n$  and  $n+2$  are prime.

S: It will snow tmr.

R or S: It will rain or snow tomorrow.

Logical Connectors: or  $\Rightarrow \vee$     deny  $\Rightarrow \neg$   
and  $\Rightarrow \wedge$

$R \vee S$ ,  $\neg(R \wedge S) \equiv \neg R \vee \neg S$ .

Translate to Symbols:

Either ... or ...  $\vee$  (same as or, but you know where to add a bracket).

De Morgan's law:

$\neg(R \vee S) \equiv \neg R \wedge \neg S$ .

$3 \leq \pi$  can be says as  $(3 < \pi) \vee (3 = \pi)$

$3 \leq \pi \leq 4$  ----  $[(3 < \pi) \vee (3 = \pi)] \wedge [(4 > \pi) \vee (4 = \pi)]$ .

Well Formed Formula.

e.g.  $\neg \wedge P$  X     $P \wedge \vee Q$  X

$(P \wedge Q)$  X

The truth table

P	Q	$P \vee Q$	$P \wedge Q$	$\neg P$	$\neg Q$	$\neg(P \wedge Q)$	$\neg P \vee \neg Q$
T	T	T	T	F	F	F	F
T	F	T	F	F	T	T	T
F	T	T	F	T	F	T	T
F	F	F	F	T	T	T	T

$$\Rightarrow \neg(P \wedge Q) \equiv \neg P \vee \neg Q.$$

$$P \vee (P \wedge Q)$$

T

T

F

F

$$\Rightarrow P \vee (P \wedge Q) \equiv P.$$

3 boxes, labeled A, O, A mixed O

You know none of these boxes is labeled correctly.

Open one