

Assume that a students found only oyster mushrooms, b students found only maitake mushrooms, c students found only lion's mane mushrooms, d+g students found both oyster and maitake mushrooms, g+f students found both maitake and lion's mane mushrooms, g+e students found both oyster and lion's mane mushrooms and g students had found all three types of mushrooms, x students found nothing.

Then we could have equations:

$$a+b+c+d+e+f+g+x = 150$$

$$a+d+e+g = 100$$

$$b+d+g+f = 33$$

$$g+e+f+c = 23$$

$$d+g = 23$$

$$g+f = 12$$

$$g+e = 10$$

$$g = 2$$

After calculation we can get that $a = 69$, $b = 0$, $c = 3$ and $x = 37$

1. 69 students found only oyster mushrooms.
2. No student found only maitake mushrooms.
3. 3 students found only lion's mane mushrooms.
4. 37 students found no mushrooms.