

Semantic Analysis

Chapter 4



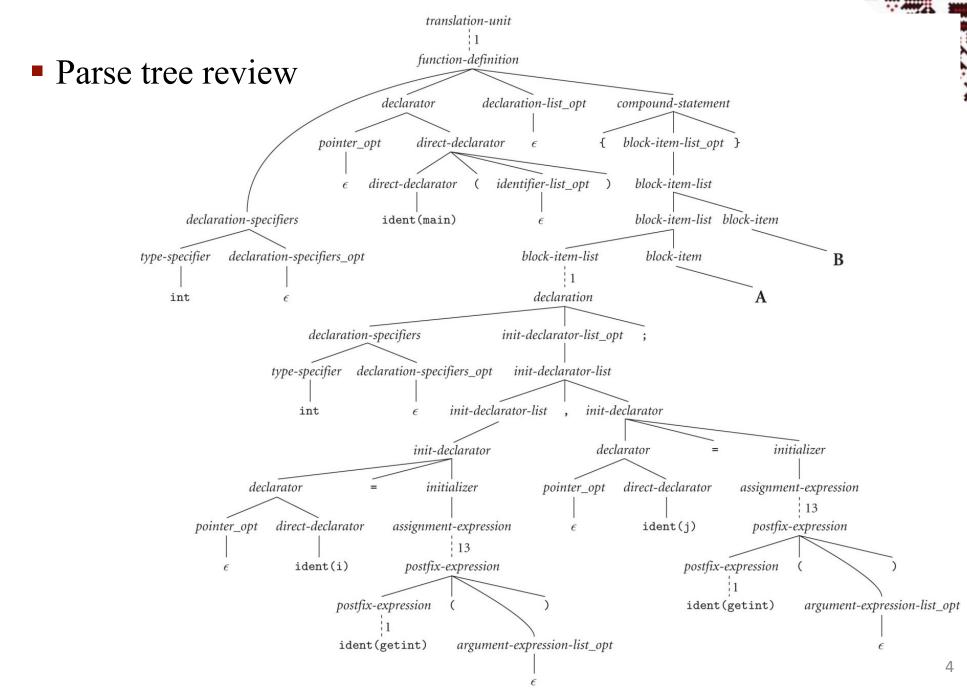
- Syntax
 - "form" of a program
 - "easy": check membership for CFG
 - linear time
- Semantics
 - meaning of a program
 - *impossible*: program correctness **undecidable**!
 - we do whatever we can

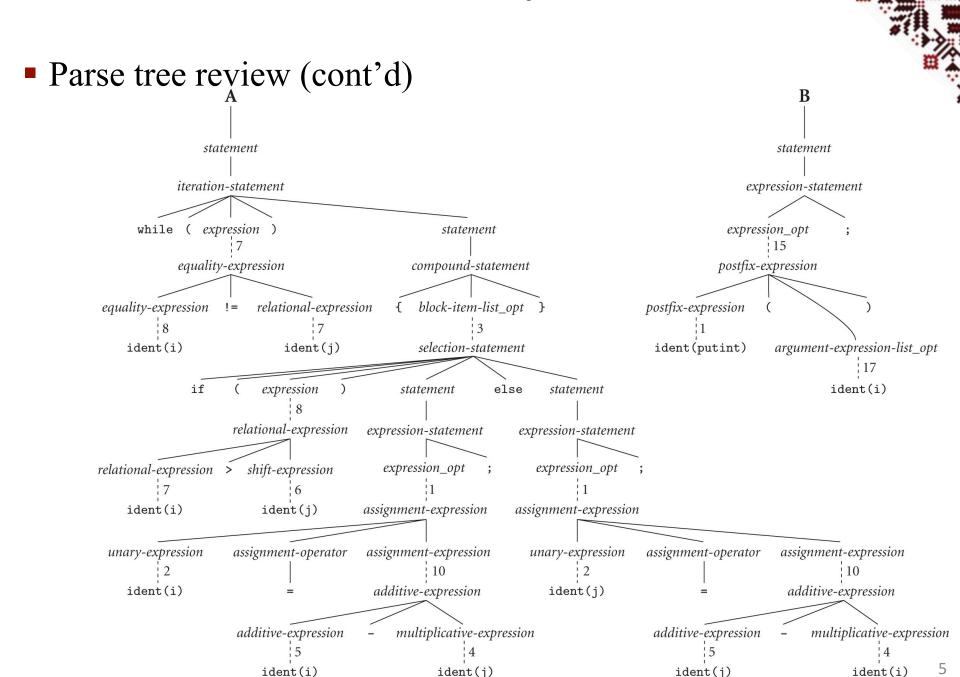


- Cyntax covor and compose time
- Static semantics compile time ≥
 - enforces static semantic rules at compile time
 - generates code to enforce dynamic semantic rules
 - constructs a syntax tree

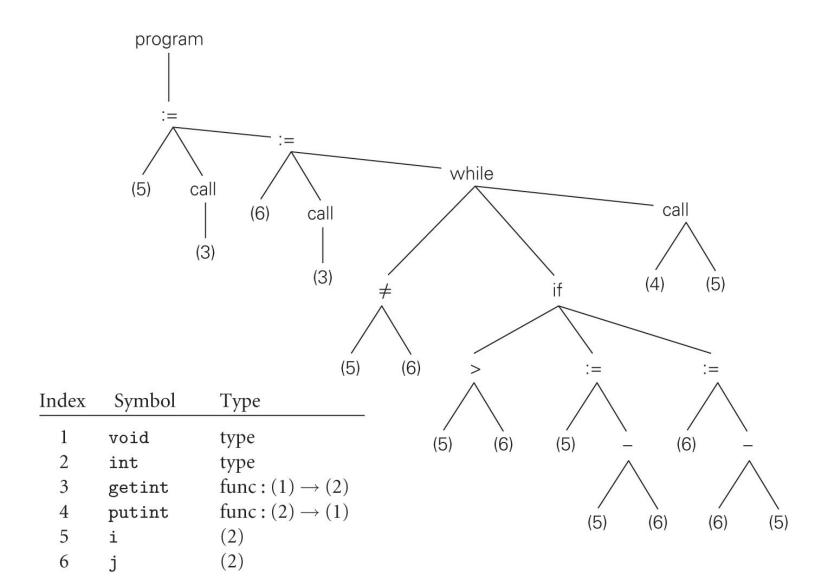
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- information gathered for the code generator
- *Dynamic* semantics run time
 - division by zero
 - index out of bounds
- Semantic analysis (and intermediate code generation) described in terms of annotation (decoration) of parse tree or syntax tree
 - annotations are attributes *attribute grammars*





Parse tree can be replaced by the smaller syntax tree (review)







- Dynamic checks
- compiler generates code for dynamic checking
- can be disabled for increased speed
 - Tony Hoare: "The programmer who disables semantic checks is like a sailing enthusiast who wears a life jacket when training on dry land but removes it when going to sea."
- C almost no checks
- Java as many checks as possible
- trend is towards stricter rules
- Example: 3 + "four"
 - Perl attempts to infer meaning
 - Python run-time error



- Logical Assertions
- Java:

```
assert denominator != 0;
AssertionError - exception thrown if semantic check fails
```

C:

```
assert(denominator != 0);
myprog.c:42: failed assertion 'denominator != 0'
```

Python:

```
assert denominator != 0, "Zero denominator!"
AssertionError: Zero denominator!
```

- Invariants, preconditions, postconditions
 - Euclid, Eiffel, Ada
 - invariant: expected to be true at all check points
 - pre/postconditions: true at beginning/end of subroutines



- Static analysis
 - compile-time algorithms that predict run-time behavior
 - extensive static analysis eliminates the need for some dynamic checks
 - precise type checking
 - enforced initialization of variables



- Attribute grammar:
 - formal framework for decorating the parse or syntax tree
 - for semantic analysis
 - for (intermediate) code generation
- Implementation
 - automatic
 - tools that construct semantic analyzers (attribute evaluator)
 - ad hoc
 - action routines





- Example: LR (bottom-up) grammar
 - arithmetic expr. with constants, precedence, associativity
 - the grammar alone says nothing about the meaning
 - *attributes*: connection with mathematical concept

1.
$$E_1 \rightarrow E_2 + T$$

$$2. E_1 \rightarrow E_2 - T$$

3.
$$E \rightarrow T$$

4.
$$T_1 \rightarrow T_2 * F$$

5.
$$T_1 \rightarrow T_2 / F$$

6.
$$T \rightarrow F$$

7.
$$F_1 \rightarrow -F_2$$

8.
$$F \rightarrow (E)$$

9.
$$F \rightarrow \text{const}$$

- Attribute grammar
- S.val: the arithmetic value of the string derived from S
- const.val: provided by the scanner
- copy rules: 3, 6, 8, 9
- semantic functions: sum, diff, prod, quot, add_inv
 - use only attributes of the current production
- 1. $E_1 \rightarrow E_2 + T$ \triangleright $E_1.val := sum(E_2.val, T.val)$ 2. $E_1 \rightarrow E_2 - T$ \triangleright $E_1.val := diff(E_2.val, T.val)$ 3. $E \rightarrow T$ \triangleright E.val := T.val4. $T_1 \rightarrow T_2 * F$ \triangleright $T_1.val := prod(T_2.val, F.val)$ 5. $T_1 \rightarrow T_2 / F$ \triangleright $T_1.val := quot(T_2.val, F.val)$ 6. $T \rightarrow F$ \triangleright $T_1.val := F.val$ 7. $F_1 \rightarrow -F_2$ \triangleright $F_1.val := add_inv(F_2.val)$ 8. $F \rightarrow (E)$ \triangleright F.val := E.val9. $F \rightarrow$ const \triangleright F.val := const.val





- Example: LL (top-down) grammar
 - count the elements of a list
 - "in-line" notation of semantic functions

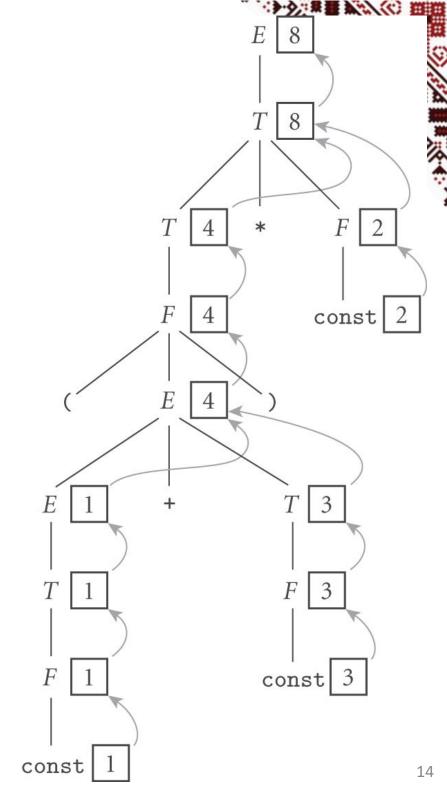
$$L \rightarrow \text{id} LT$$
 $\triangleright \text{L.c} := 1 + 1$
 $LT \rightarrow LT \cdot c := L.c$
 $LT \rightarrow \varepsilon$ $\triangleright \text{LT.c} := 0$

$$L \rightarrow \text{id} LT$$
 $\triangleright \text{L.c} := 1 + \text{LT.c}$

$$>$$
 LT.c := L.c

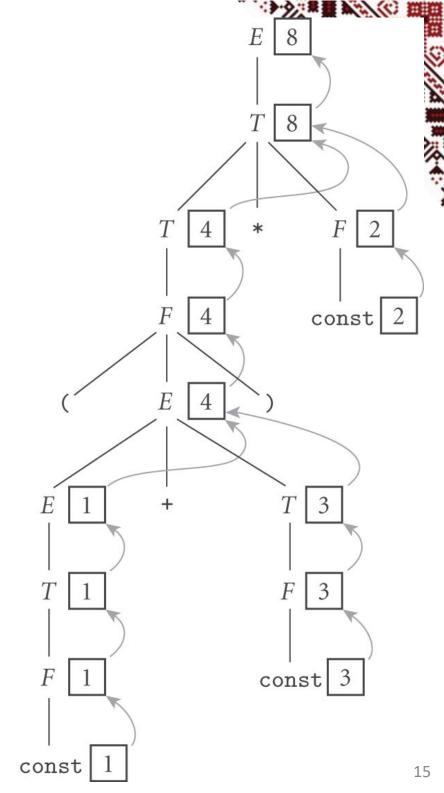


- Annotation of parse tree:
 - evaluation of attributes
 - also called decoration
- Example:
 - LR(1) grammar (arithm. exp.)
 - string: (1+3)*2
 - *val* attribute of root will hold the value of the expression





- Types of attributes:
 - synthesized
 - inherited
- Synthesized attributes:
 - values calculated only in productions where they appear only on the left-hand side
 - attribute flow: bottom-up only
- *S-attributed* grammar: all attributes are synthesized

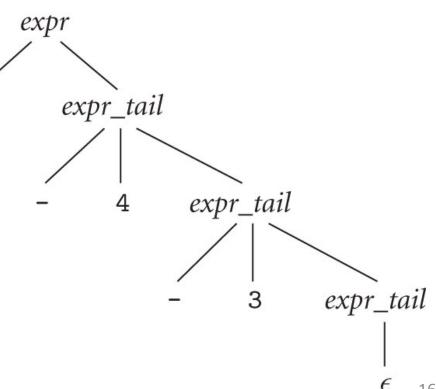


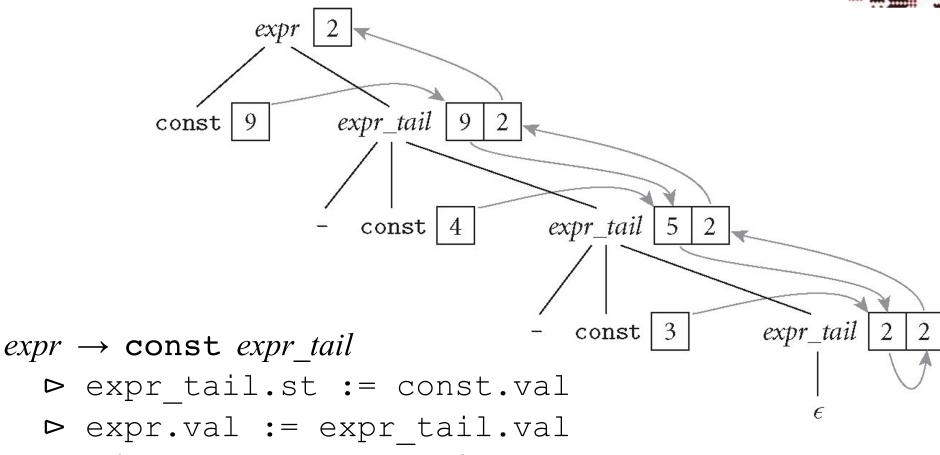


- Inherited attributes:
 - values calculated when their symbol is on RHS of the production
 - Example: LL(1) grammar for subtraction

$$expr \rightarrow const \ expr_tail$$
 $expr_tail \rightarrow - const \ expr_tail$
 $\rightarrow \epsilon$

- string: 9 4 3
- left-associative means cannot have only bottom-up
- need to pass 9 to expr tail to combine with 4





- $expr\ tail_1 \rightarrow const\ expr_tail_2$
 - ▶ expr tail₂.st := expr tail₁.st const.val
- ▶ expr tail₁.val := expr tail₂.val $expr\ tail \rightarrow \varepsilon$
 - ▷ expr tail.val := expr tail.st

- Example: Complete LL(1) grammar for arithmetic expressions
- Complicated because:
 - Operators are left-associative but grammar cannot be left-recursive
 - Left and right operands of an operator are in separate productions

1.
$$E \longrightarrow T TT$$

 $\triangleright TT.st := T.val$ $\triangleright E.val := TT.val$

2.
$$TT_1 \longrightarrow + T TT_2$$

 $\triangleright TT_2.st := TT_1.st + T.val$ $\triangleright TT_1.val := TT_2.val$

3.
$$TT_1 \longrightarrow -T TT_2$$

 $\triangleright TT_2.st := TT_1.st - T.val$ $\triangleright TT_1.val := TT_2.val$

4.
$$TT \longrightarrow \epsilon$$
 \triangleright TT.val := TT.st

5.
$$T \longrightarrow F FT$$
 $\triangleright FT.st := F.val$



Example: LL(1) grammar for arithmetic expressions (cont'd)

6.
$$FT_1 \longrightarrow *F FT_2$$

 $\triangleright FT_2.st := FT_1.st \times F.val$ $\triangleright FT_1.val := FT_2.val$

7.
$$FT_1 \longrightarrow / F FT_2$$

 $\triangleright FT_2.st := FT_1.st \div F.val$ $\triangleright FT_1.val := FT_2.val$

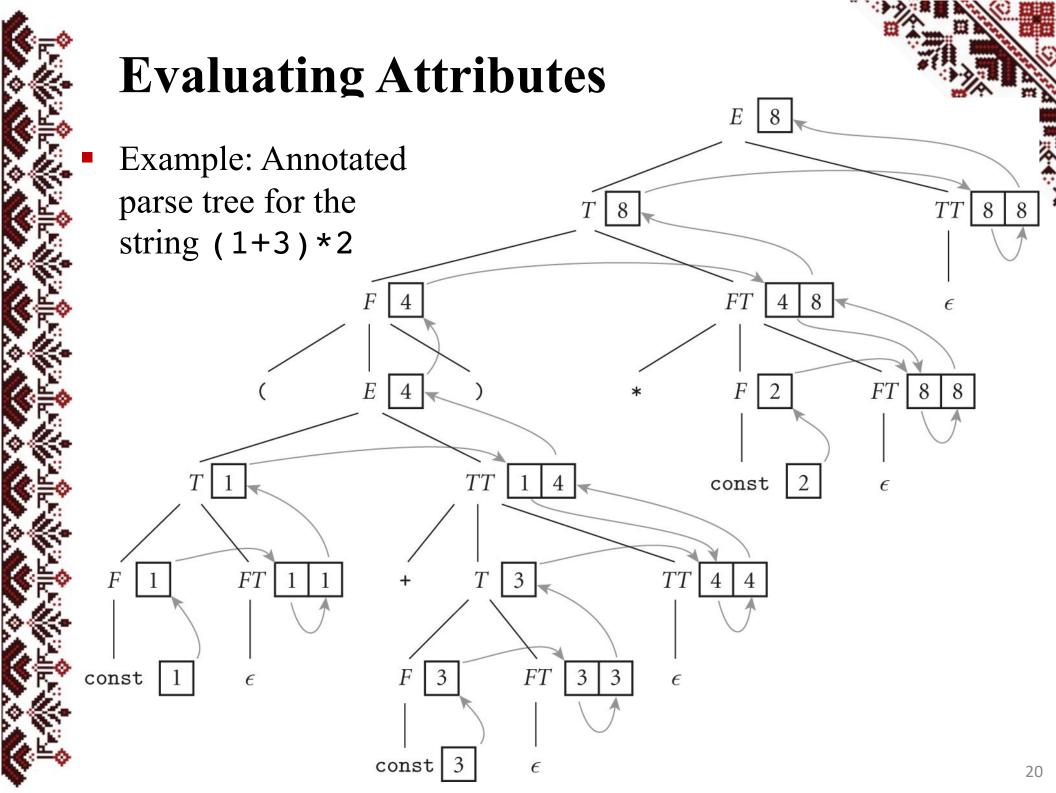
8.
$$FT \longrightarrow \epsilon$$
 \triangleright FT.val := FT.st

9.
$$F_1 \longrightarrow -F_2$$

 $\triangleright F_1.val := -F_2.val$

10.
$$F \longrightarrow (E)$$
 $\triangleright \text{ F.val} := \text{E.val}$

11.
$$F \longrightarrow const$$
 \triangleright F.val := const.val





- Attribute flow
- *Declarative* notation:
 - no evaluation order specified for attributes
- Well-defined grammar:
 - its rules determine unique values for attributes in any parse tree
- Non-circular grammar:
 - no attribute depends on itself in any parse tree
- *Translation scheme*:
 - algorithm that decorates parse tree in agreement with the attribute flow



- Translation scheme:
 - Obvious scheme: repeated passes until no further changes
 - halts only if well defined
 - Dynamic scheme: better performance
 - topologically sort the attribute flow graph
- Static scheme: fastest, O(n)
 - based on the structure of the grammar
- S-attributed grammar simplest static scheme
 - flow is strictly bottom-up; attributes can be evaluated in the same order the nodes are generated by an LR-parser



• Attribute A.s is said to *depend* on attribute B.t if B.t is ever passed to a semantic function that returns a value for A.s

■ *L-attributed grammar*:

- each synthesized attribute of a LHS symbol depends only on that symbol's own inherited attributes or on attributes (synthesized or inherited) of the RHS symbols
- each inherited attribute of a RHS symbol depends only on inherited attributes of the LHS symbol or on attributes (synthesized or inherited) of symbols to its left in the RHS

L-attributed grammar

 attributes can be evaluated by a single left-to-right depth-first traversal



- S-attributed implies L-attributed (but not vice versa)
- S-attributed grammar: the most general class of attribute grammars for which evaluation can be implemented on the fly during an LR parse
- L-attributed grammar: the most general class of attribute grammars for which evaluation can be implemented on the fly during an LL parse
- If semantic analysis interleaved with parsing:
 - bottom-up parser paired with S-attribute translation scheme
 - top-down parser paired with L-attributed translation scheme



Syntax Tree

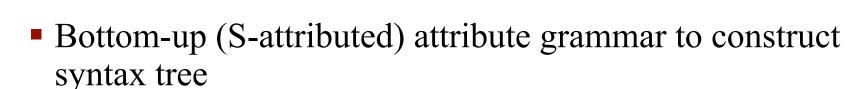
- One-pass compiler
 - interleaved: parsing, semantic analysis, code generation
 - saves space (older computers)
 - no need to build parse tree or syntax tree
- Multi-pass compiler
 - possible due to increases in speed and memory
 - more flexible
 - better code improvement
 - Example: forward references
 - declaration before use no longer necessary



Syntax Tree

- Syntax Tree
 - separate parsing and semantics analysis
 - attribute rules for CFG are used to build the syntax tree
 - semantics easier on syntax tree
 - syntax tree reflects semantic structure better
 - can pass the tree in different order than that of parser





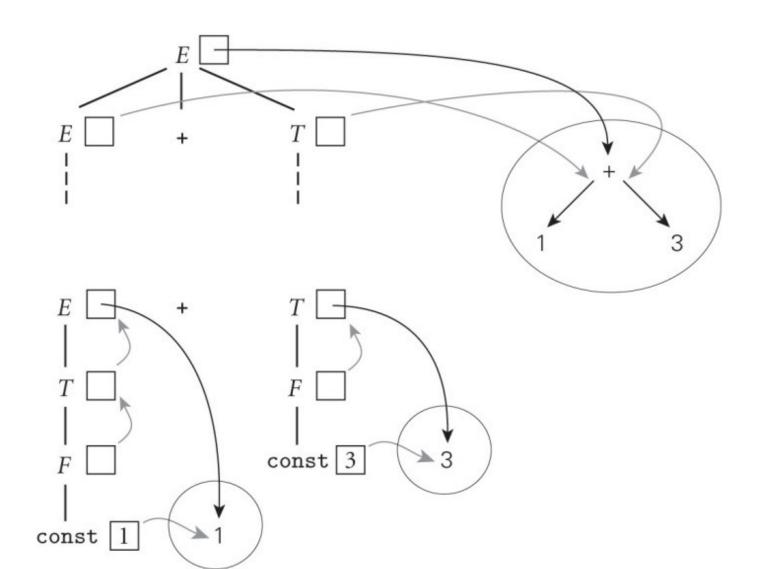
$$E_1 \longrightarrow E_2 + T$$
 $ightharpoonup E_1.ptr := make_bin_op("+", E_2.ptr, T.ptr)$
 $E_1 \longrightarrow E_2 - T$
 $ightharpoonup E_1.ptr := make_bin_op("-", E_2.ptr, T.ptr)$
 $E \longrightarrow T$
 $ightharpoonup E.ptr := T.ptr$
 $T_1 \longrightarrow T_2 * F$
 $ightharpoonup T_1.ptr := make_bin_op("x", T_2.ptr, F.ptr)$
 $T_1 \longrightarrow T_2 / F$
 $ightharpoonup T_1.ptr := make_bin_op("\div ", T_2.ptr, F.ptr)$

 Bottom-up (S-attributed) attribute grammar to construct syntax tree (cont'd)

$$T\longrightarrow F$$
 $ightharpoonup T.ptr := F.ptr$
 $F_1\longrightarrow -F_2$
 $ightharpoonup F_1.ptr := make_un_op("+/_", F_2.ptr)$
 $F\longrightarrow (E)$
 $ightharpoonup F.ptr := E.ptr$
 $F\longrightarrow const$
 $ightharpoonup F.ptr := make_leaf(const.val)$



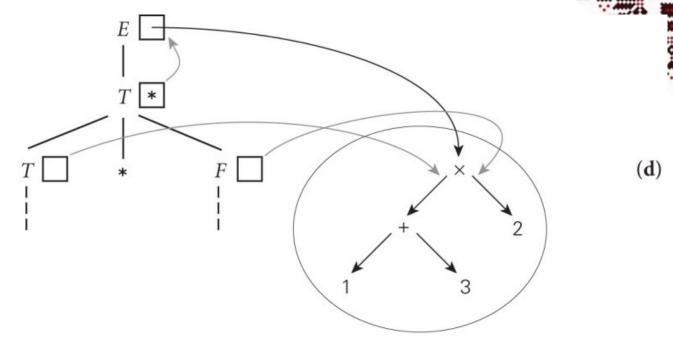
Syntax tree construction for (1+3)*2

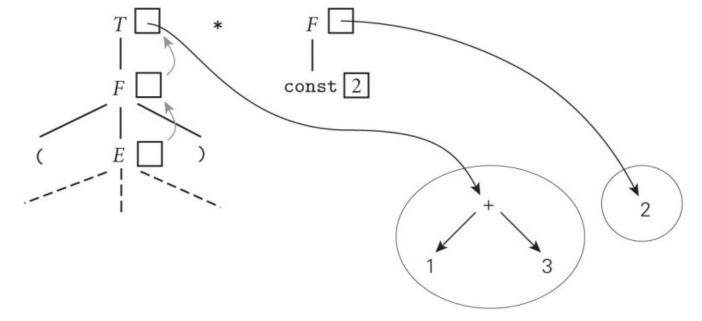




(a)

Syntax tree construction for (1+3)*2 (cont'd)





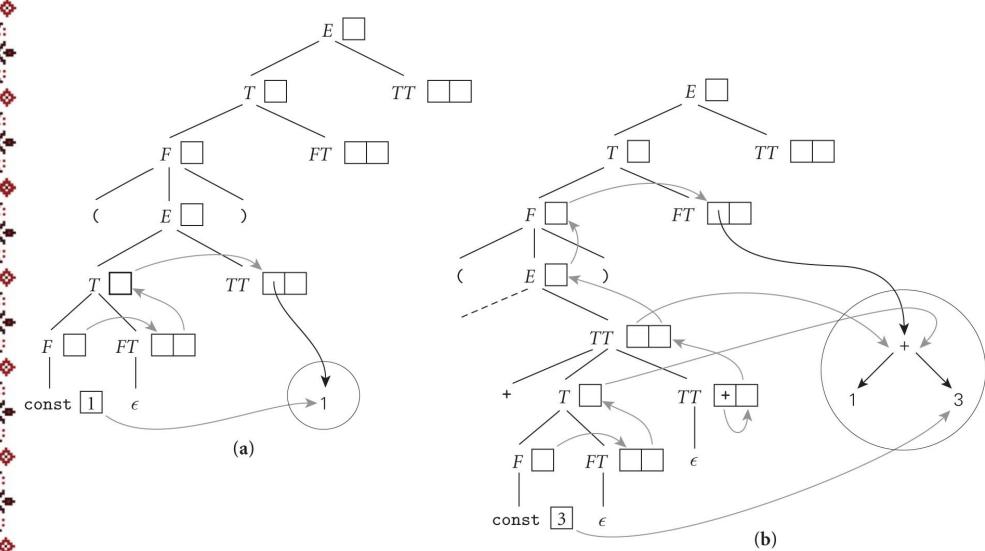
(c)

 Top-down (L-attributed) attribute grammar to construct syntax tree

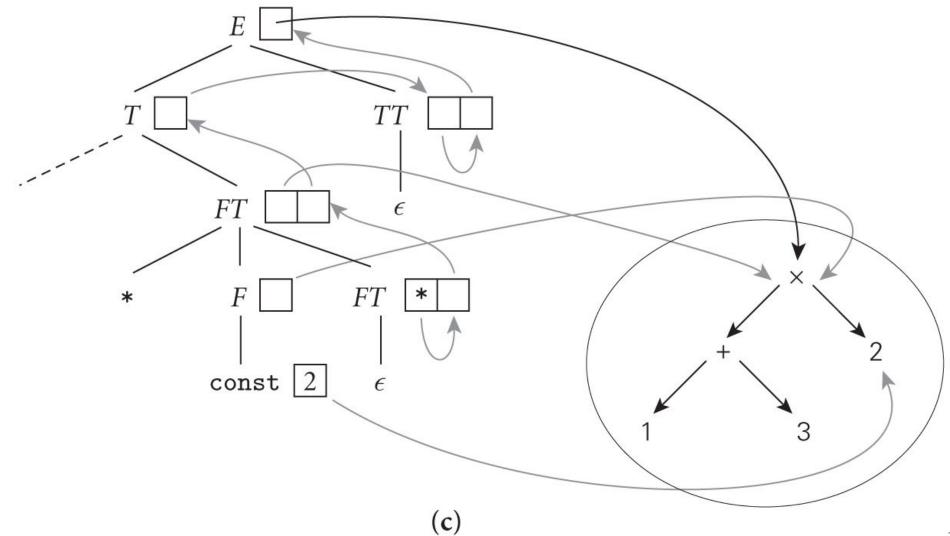
■ Top-down (L-attributed) attribute grammar to construct syntax tree (cont'd)

$$FT_1 \longrightarrow FT_2.st := make_bin_op("x", FT_1.st, F.ptr)$$
 $\triangleright FT_1.ptr := FT_2.ptr$
 $FT_1 \longrightarrow / F FT_2$
 $\triangleright FT_2.st := make_bin_op("\div", FT_1.st, F.ptr)$
 $\triangleright FT_1.ptr := FT_2.ptr$
 $FT \longrightarrow \epsilon$
 $\triangleright FT.ptr := FT.st$
 $FT \longrightarrow FT_2$
 $\triangleright FT.ptr := FT.st$
 $FT \longrightarrow FT_2.ptr \mapsto FT_2.ptr$
 $FT \longrightarrow \epsilon$
 $\vdash FT_2.ptr \mapsto FT_2.ptr$
 $FT \longrightarrow \epsilon$
 $\vdash FT_2.ptr \mapsto FT_2.ptr$
 $FT_3.ptr := FT.st$
 $FT_3.ptr :$

Syntax tree for (1+3)*2



Syntax tree for (1+3)*2 (cont'd)





Action Routines

- There are automatic tools for:
 - Context-free grammar \Rightarrow parser
 - Attribute grammar \Rightarrow semantic analyzer (attrib. eval.)
- Action routines
 - ad-hoc approach; most ordinary compilers use (!)
 - Interleave parsing, syntax tree construction, other aspects of semantic analysis, code generation
 - Action routine: Semantic function that the programmer (grammar writer) instructs the compiler to execute at some point in the parse
 - In an LL grammar, can appear anywhere in the RHS; called as soon as the parser matched the (yield of the) symbol to the left



- LL(1) grammar for expressions
 - with action routines for building the syntax tree
 - only difference from before: actions embedded in RHS

```
E \longrightarrow T \{ TT.st := T.ptr \} TT \{ E.ptr := TT.ptr \}
TT_1 \longrightarrow + T \{ TT_2.st := make\_bin\_op("+", TT_1.st, T.ptr) \} TT_2 \{ TT_1.ptr := TT_2.ptr \}
TT_1 \longrightarrow T  { TT_2.st := make\_bin\_op("-", <math>TT_1.st, T.ptr) } TT_2  { TT_1.ptr := TT_2.ptr }
TT \longrightarrow \epsilon \{ TT.ptr := TT.st \}
T \longrightarrow F \{ FT.st := F.ptr \} FT \{ T.ptr := FT.ptr \}
FT_1 \longrightarrow *F \{ FT_2.st := make\_bin\_op("x", FT_1.st, F.ptr) \} FT_2 \{ FT_1.ptr := FT_2.ptr \}
FT_1 \longrightarrow /F \{ FT_2.st := make\_bin\_op("÷", FT_1.st, F.ptr) \} FT_2 \{ FT_1.ptr := FT_2.ptr \}
FT \longrightarrow \epsilon \{ FT.ptr := FT.st \}
F_1 \longrightarrow -F_2 \{ F_1.ptr := make\_un\_op("+/\_", F_2.ptr) \}
F \longrightarrow (E) \{ F.ptr := E.ptr \}
   --> const { F.ptr := make_leaf(const.ptr) }
```



Action Routines - Example



Recursive descent parsing with embedded action routines:

```
procedure term_tail(lhs : tree_node_ptr)
    case input_token of
    +, -:
        op : string := add_op()
        return term_tail(make_bin_op(op, lhs, term()))
        -- term() is a recursive call with no arguments
    ), id, read, write, $$ : -- epsilon production
        return lhs
    otherwise parse_error
```

• does the same job as productions 2-4:

```
TT_1 \longrightarrow + T \ \{ \ TT_2.st := make\_bin\_op("+", \ TT_1.st, \ T.ptr) \ \} \ TT_2 \ \{ \ TT_1.ptr := TT_2.ptr \ \}  TT_1 \longrightarrow - T \ \{ \ TT_2.st := make\_bin\_op("-", \ TT_1.st, \ T.ptr) \ \} \ TT_2 \ \{ \ TT_1.ptr := TT_2.ptr \ \}  TT \longrightarrow \epsilon \ \{ \ TT.ptr := TT.st \ \}
```



Action Routines - Example

- Bottom-up evaluation
 - In LR-parser action routines cannot be embedded at arbitrary places in the RHS
 - the parser needs to see enough to identify the production, i.e.,
 the RHS suffix that identifies the production uniquely
 - Previous bottom-up examples are identical with the action routine versions