Assignment midterm-practice1 due 10/27/2022 at 12:09am EDT

1. (1 point)

Midterm Practice Introduction

This problem set is for practice and is **not** worth anything.

You can attempt each problem as many times as you like and you can view the answers to a question by selecting the CorrectAnswers checkbox.

2. (1 point)

Consider the statements:

P: I will go to the library today.

Q: I will go to the gym today.

Which of the following statements is equivalent to the statement "I will go to either the library or the gym today, but I won't g?

- $(P \land Q) \lor \neg (P \land Q)$
- $(P \land Q) \lor (\neg P \land \neg Q)$
- $(P \lor Q) \land (\neg P \land \neg Q)$
- $(P \lor Q) \land \neg (P \land Q)$
- None of the above

Answer(s) submitted:

•

(incorrect)

3. (1 point)

Consider the statements:

P: Billy gets the job.

Q: Bob gets the job.

Which of the following statements is the **negation** of the statement "Either Billy or Bob will get the job, but not both"? (The "negation" of a statement R is $\neg R$.)

- $(P \land \neg Q) \lor (\neg P \land Q)$
- $(\neg P \land Q) \land (P \land \neg Q)$
- $\bullet \ (\neg P \lor Q) \land (P \lor \neg Q)$
- $(P \lor \neg Q) \lor (\neg P \lor Q)$

• None of the above

Answer(s) submitted:

•

(incorrect)

4. (1 point)

Consider the statements:

S: Steve will go to the concert.

K: Kate will go to the concert.

Match the following propositions with the English sentences that they represent.

- A. Either Steve or Kate will go to the concert, and Steve won't go.
- B. Either both Steve and Kate will go to the concert, or both of them won't go.
- C. Either Steve will go to the concert, or neither Steve nor Kate will go.

Answer(s) submitted:

- •
- •

(incorrect)

5. (1 point) Select all the sentences that are logically equivalent to

$$x \in S \rightarrow x \in T$$
.

- A. $x \in S \lor x \notin T$
- B. $x \in S \land x \in T$
- C. $x \notin T \rightarrow x \notin S$
- D. $x \in T \lor x \notin S$
- E. $x \in T \rightarrow x \in S$

Partial credit is given, except when no boxes are marked.

Answer(s) submitted:

(incorrect)

6. (1 point)

Complete the following truth table by filling in the blanks with T or F as appropriate.

$-P \mid Q \mid$	$(P \to Q) \leftrightarrow (Q \to P)$
T T	_
T F	_
F T	_
F F	_

Answer(s) submitted:

- •
- •
- •

(incorrect)

7. (1 point) Complete the following truth table by filling in the blanks with T or F as appropriate.

P	Q	P o Q	$Q \rightarrow P$	$\neg P$	$\neg Q$	$\neg P \rightarrow \neg Q$	$\neg Q \rightarrow \neg P$
Т	T						
T	F						
F	T						
F	F						

Answer(s) submitted:

- •
- •
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(incorrect)

8. (1 point)

Which of the following statements are equivalent to the statement $P \land \neg Q$? Select all correct answers.

- A. $\neg(\neg P \lor Q)$
- B. $\neg Q \land (P \lor Q)$
- C. $\neg (P \lor Q)$
- D. $(P \vee \neg Q) \wedge (Q \vee \neg P)$

Partial credit is given, except when no boxes are marked.

Answer(s) submitted:

•

(incorrect)

9. (1 point)

Which of the statements below has the following truth table?

P	Q	???
—Т	T	T
—Т	F	F
—F	T	T
—F	F	T

- $P \vee \neg Q$
- $Q \vee \neg (P \wedge Q)$
- $\bullet \ P \lor (\neg P \land \neg Q)$
- $(P \land Q) \lor \neg P$
- None of the above

Answer(s) submitted:

•

(incorrect)

10. (1 point)

Determine if each of the following statements is a tautology, a contradiction or neither:

$$(P \land \neg R) \lor \neg (P \lor Q)$$

- ?
- Tautology
- Contradiction
- Neither

$$(P \lor Q) \lor (\neg P \lor \neg Q)$$

- ?
- Tautology
- Contradiction
- Neither

•

(incorrect)

11. (1 point)

Let C(x) be the statement "x has a cat", let D(x) be the statement "x has a dog" and let F(x) be the statement "x has a ferret". Let the universe of discourse consist of all students in your class. Match each logical expression to its equivalent English statement by putting the appropriate letter beside the logical expression.

- \bot 1. $\exists x (C(x) \land D(x) \land F(x))$
- $2. \exists x (C(x)) \land (\exists x D(x)) \land (\exists x F(x))$
- $3. \forall x (C(x) \lor D(x) \lor F(x))$
- $__4. \neg \exists x (C(x) \land D(x) \land F(x))$
- $__5$. $\exists x (C(x) \land F(x) \land \neg D(x))$
- A. A student in your class has a cat, a dog, and a ferret.
- B. All students in your class have a cat, a dog, or a ferret.
- C. Some student in your class has a cat and a ferret but not a dog.
- D. No student in this class has a cat, a dog, and a ferret.
- E. For each of the three kinds of animals (cats, dogs, and ferrets), there is a student in your class who has one of these animals.

Answer(s) submitted:

- •
- •
- •
- •

(incorrect)

12. (1 point)

Let F(x) denote the statement x is friendly and H(x) denote the statement x is happy.

Analyze the logical form of the following statement and choose the correct answer.

Everyone is happy only if everyone is friendly.

- $\forall x H(x) \rightarrow \forall x F(x)$
- $\forall x (F(x) \rightarrow H(x))$
- $\forall x (H(x) \rightarrow F(x))$
- $\forall x F(x) \rightarrow \forall x H(x)$
- None of the above

•

(incorrect)

13. (1 point)

Select all the correct answers. There might be more than one right answer.

Which of the following expressions are equivalent to $\exists x \exists y (P(x,y) \rightarrow \neg Q(x,y))$

- A. $\forall x \forall y (P(x,y) \land Q(x,y))$
- B. $\exists x \exists y (\neg P(x,y) \lor \neg Q(x,y))$
- C. $\exists x \exists y (Q(x,y) \rightarrow \neg P(x,y))$
- D. $\neg \forall x \forall y \neg (P(x,y) \rightarrow \neg Q(x,y))$

Partial credit is given, except when no boxes are marked.

Answer(s) submitted:

•

(incorrect)

14. (1 point)

Let P(x, y) stand for the statement "x is the parent of y". Here x and y each denote a human being.

Which of the following is equivalent to the statement $\exists y \neg \exists x P(x,y)$?

- There exists a human who has no human parent.
- Every human is the parent of at least one human.
- There exists a human who is the parent of every human.
- It is not the case that every human is the parent of every human.
- None of the above

•

(incorrect)

15. (1 point)

Select all the correct answers. There might be more than one right answer.

In which of these four universes is the following statement true.

$$\exists x (x \text{ is odd} \rightarrow x > 8)$$

- A. {19}
- B. {10,20}
- C. {1,3,7}
- D. {8}
- E. None of the above

Answer(s) submitted:

•

(incorrect)

16. (1 point)

Let A, B, and C be sets. Which of the following sets is always equal to $A \setminus (B \setminus C)$?

- $(A \cap C) \setminus (B \cap C)$
- $(A \setminus B) \cap (A \setminus C)$
- $(A \setminus C) \cup (B \setminus C)$
- $(A \setminus B) \cup (A \cap C)$
- None of the above

Hint: For this problem it might be useful to draw Venn diagrams.

Answer(s) submitted:

•

(incorrect)

17. (1 point)

Evaluate the following sets:

$$\bigcup \{[-n,n] \mid n \in \mathbb{N}\} = \underline{\hspace{1cm}}$$

$$\{x^2 + 4 \mid x \in \mathbb{R}\} = \underline{\hspace{1cm}}$$

$${3n+1 \mid n \in \{0,1,2,3\}} = \underline{\hspace{1cm}}$$

Enter your answers using set notation or interval notation.

Answer(s) submitted:

- •
- •

(incorrect)

Consider the family of sets $\mathcal{F} = \{\{1,2,3,4,5\}, \{2,3,4,5,6\}, \{3,4,5,6,7\}, \{4,5,6,7,8\}\}$. Evaluate the following sets.

$$\bigcup \mathcal{F} =$$

$$\bigcap \mathcal{F} =$$

Enter your answers using **set notation**.

Answer(s) submitted:

- •
- (incorrect)

The power set of $\{3,7\}$ is _____

Enter your answer using set notation.

Answer(s) submitted:

•

(incorrect)

20. (1 point) Which of the following statements are true? Select all correct answers.

- A. $\emptyset \in \{\emptyset\}$
- B. $\{0\} \subseteq \emptyset$
- C. $\emptyset \subseteq \{\emptyset\}$
- D. $0 \in \emptyset$

• E. $\emptyset \subseteq \{0\}$ Answer(s) submitted:
•
(incorrect)

21. (1 point) Let $A = \{1, 2\}$ and $\mathcal{P}(A)$ be the power set of A.

Which of the following statements are true? Select all correct answers.

- A. $\emptyset \in \mathcal{P}(A)$
- B. ∅ ∈ *A*
- C. $\{\emptyset\} \in \mathcal{P}(A)$
- D. $\emptyset \subseteq A$
- E. $A \subseteq \mathcal{P}(A)$

Partial credit is given, except when no boxes are marked.

Answer(s) submitted:

•

(incorrect)

22. (1 point) Which of the following sets are subsets of {integers divisible by 2}? Select all correct answers.

- A. {−82, 104, 16}
- B. {prime numbers}
- C. {even natural numbers}
- D. {44,221,90}
- E. {1}

Answer(s) submitted:

•

(incorrect)

23. (1 point)

Let
$$W = \{1, 5, 8, 9, 11\}$$
 and $X = \{0, 3, 5, 8, 9\}$.

Determine the following sets. Express your answers using **set notation**.

$$W \setminus X = \underline{\hspace{1cm}}$$

$$X \setminus W = \underline{\hspace{1cm}}$$

Answer(s) submitted:

•

(incorrect)

24. (1 point)

Let $A = \{1, 2, 3, 5, 10\}$ and $B = \{1, 5, 8, 10\}$.

Determine the following sets. Express your answers using **set notation**.

 $A \cap B = \underline{\hspace{1cm}}$

 $A \cup B = \underline{\hspace{1cm}}$

Answer(s) submitted:

•

(incorrect)

25. (1 point)

Let $A = \{7, 10, 4, 8, 11\}$ and $B = \{x \mid x \text{ is an even positive integer less than } 10\}.$

Determine the following sets. Express your answers using **set notation**.

 $A \cap B = \underline{\hspace{1cm}}$

 $A \cup B =$

Answer(s) submitted:

•

(incorrect)

26. (1 point) Consider the following statement:

$$a-b \notin \{c \in \mathbb{R} \mid c \text{ is odd } \}.$$

Determine whether each variable is free or bound.

a is a:

- A. Free variable
- B. Bound variable

b is a:

- A. Free variable
- B. Bound variable

c is a:

- A. Free variable
- B. Bound variable

Answer(s) submitted:

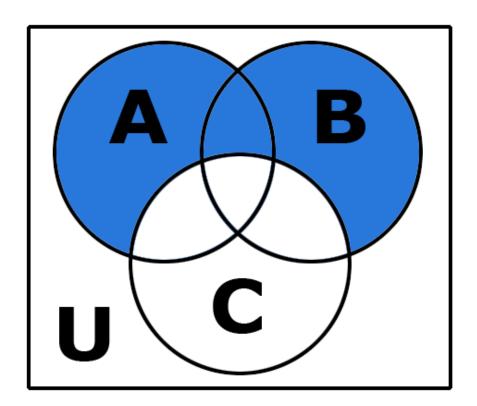
- •
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(incorrect)

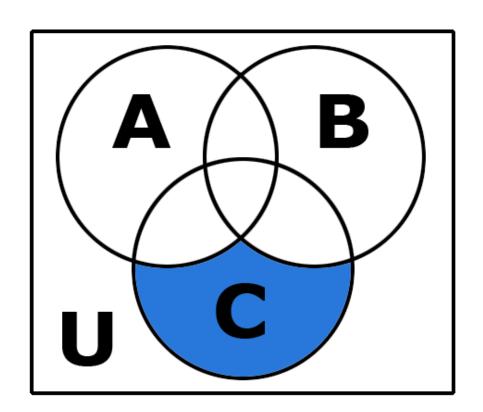
27. (1 point)

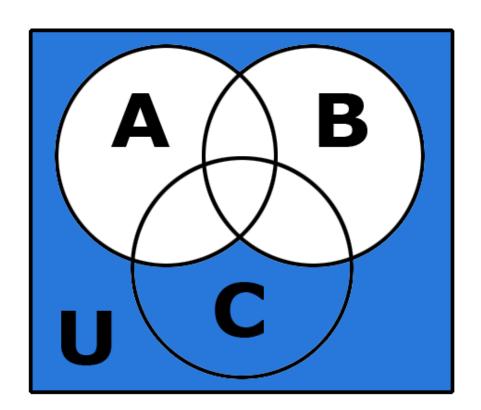
Let A, B, and C be sets in a universe U.

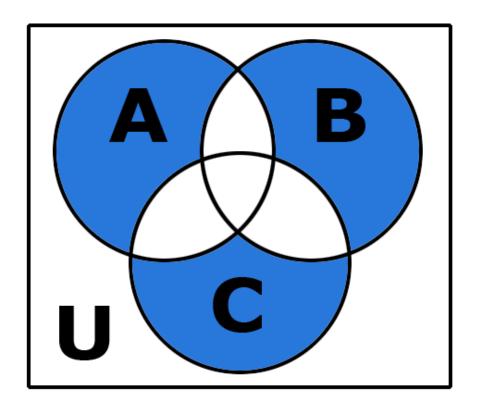
Which of the following Venn diagrams corresponds to $U \setminus (A \cup B)$?



11







(incorrect)

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