Partial Derivatives of the Loss Functions (OLS & LAD)

$$\frac{\partial}{\partial b_o} \left( (y_i - b_o - b_i x_i)^2 \right), \text{ using the chain rule } \frac{\partial}{\partial b_o} \left( (y_i - b_o - b_i x_i)^2 \right) = \frac{\partial u^2}{\partial u} \frac{\partial u}{\partial b_o}, \text{ where } u = y_i - b_o - b_i x_i \text{ and } \frac{\partial}{\partial u} \left( u^2 \right) = 2u : \text{ we get } 2 \left( y_i - b_o - b_i x_i \right) \left( \frac{\partial}{\partial b_o} \left( y_i - b_o - b_i x_i \right) \right)$$

$$D_i \text{ Herefore, } \text{ by term and factor out constants: } 2 \left( y_i - b_o - b_i x_i \right) \left( -1 \right)$$

$$Therefore, \quad \frac{\partial L}{\partial b_o} = -2 \sum_{i=1}^{n} \left( y_i - b_o - b_i x_i \right) = -2 \sum_{i=1}^{n} r_i$$

$$LAD = \sum_{i=1}^{n} |y_{i} - \hat{y}_{i}| \quad \text{where} \quad \hat{y}_{i} = b_{o} + b_{i} \times_{i} = \sum_{i=1}^{n} |y_{i} - b_{o} - b_{i} \times_{i}|$$

$$L = \begin{cases} \sum_{i=1}^{n} (y_{i} - b_{o} - b_{i} \times_{i}) & \text{if} \quad y_{i} \times \hat{y}_{i} \\ \sum_{i=1}^{n} (-y_{i} + b_{o} + b_{i} \times_{i}) & \text{if} \quad y_{i} \times \hat{y}_{i} \end{cases}$$

$$\frac{\partial L}{\partial b_{o}} = \begin{cases} \sum_{i=1}^{n} \frac{\partial (y_{i} - b_{o} - b_{i} \times_{i})}{\partial b_{o}} = 1 & \text{if} \quad y_{i} \times \hat{y}_{i} \end{cases}$$

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