From p-values to decision making

Suppose you are testing the hypotheses

$$H_0: p = 0.6$$

 $H_a: p > 0.6$

based on data that have produced

sperific $\Rightarrow p = 0.75$

For this, you calculate the p-value

p-value = P(p > 0.75)

specific value

and compare it with the significance level $\boldsymbol{\vee}$.

p-value

What is the value of "?" that gives the area under the normal curve equal to <a>??
This value of "?" is very important: if the observed is to the right of "?", then we reject the null hypothesis, and we retain it otherwise.

Let's find "?"

Same as
$$P(\hat{p} > ?) = d$$

$$P(\hat{p} - p) = d$$

$$P($$

Then
$$\frac{?-p}{p(a-p)} = 1.64$$
 (see Table 21.1)

and so

$$? = p + 1.64 \sqrt{\frac{p(1-p)}{n}}$$

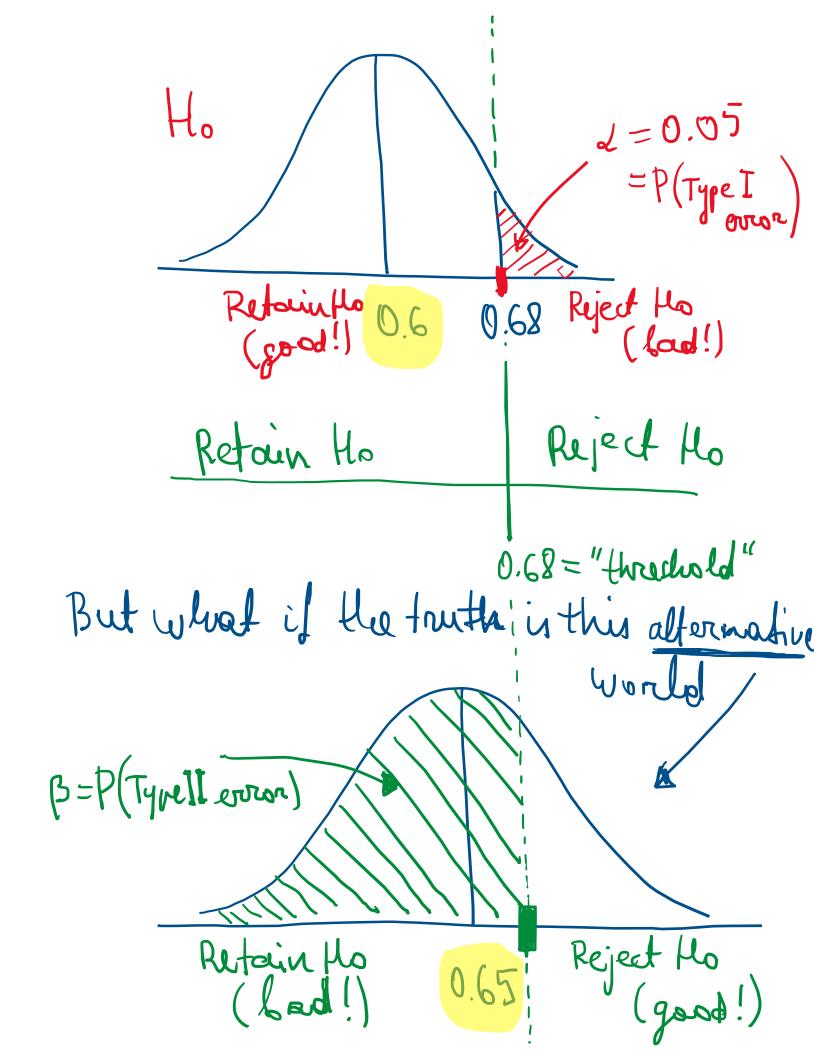
$$= 0.6 + 1.64 \sqrt{\frac{0.6 \times 0.4}{100}}$$

$$= 0.6803433...$$

Consequently, we have the decision rule:

If
$$\beta > 0.68$$
, then reject Ho

If $\beta < 0.68$, then retain Ho



Note what happens when we move the threshold to the right or left:

If we move it to the right, $\sqrt{}$ decreases but $\sqrt{}$ increases

If we move it to the left, dincreases but be decreases

As we see, we can't decrease the two probabilities at the same time. Hence, we have to make a choice: either α is small or β is small.

See the file entitled "Decisions (credit card) type I and II errors" for a visualization. Run the slides quickly to see how the probabilities of type I and type II errors interact.