

Nominal GDP = Real GDP * Price Level

	Apples	Oranges
Q_1	50	100
P_1	\$1	\$0.80
Q_2	80	120
P_2	\$1.25	\$1.60

Nominal GDP_1 = $$(50*1 + 100*0.80) = \130

Nominal GDP_2 = $$(80*1.25 + 120*1.60) = \292

The ratio of nominal GDP = $292/130 = 2.25$

Change in nominal GDP = $(292/130-1) = 125\%$

Real GDP Calculation:

- Assume base year = year 1 →

	Apples	Oranges
P_1	\$1	\$0.80

Real GDP_1 = $$(50*1 + 100*0.80) = \130

Real GDP_2 = $$(80*1 + 120*0.80) = \176

The ratio of real GDP, $g_1 = (176/130) = 1.354 \rightarrow$ Change in real GDP = 35.4%

- Assume base year = year 2 →

	Apples	Oranges
P_2	\$1.25	\$1.60

Real GDP_1 = $$(50*1.25 + 100*1.60) = \222.50

Real GDP_2 = $$(80*1.25 + 120*1.60) = \292

The ratio of real GDP, $g_2 = (292/222.50) = 1.312 \rightarrow$ Change in real GDP = 31.2%

- The base year matters in this case because the relative price of apple/orange changes from year 1 to year 2. For instance, $RP_1 = 1/0.80 = 1.25$ versus $RP_2 = 1.25/1.60 = 0.78$.

Chain-Weighted Real GDP:

The chain-weighted ratio = $(g_1 * g_2)^{1/2} = (1.354 * 1.312)^{1/2} = 1.333 \rightarrow$
Change in real GDP = 33.3%

If base year = year 1, then

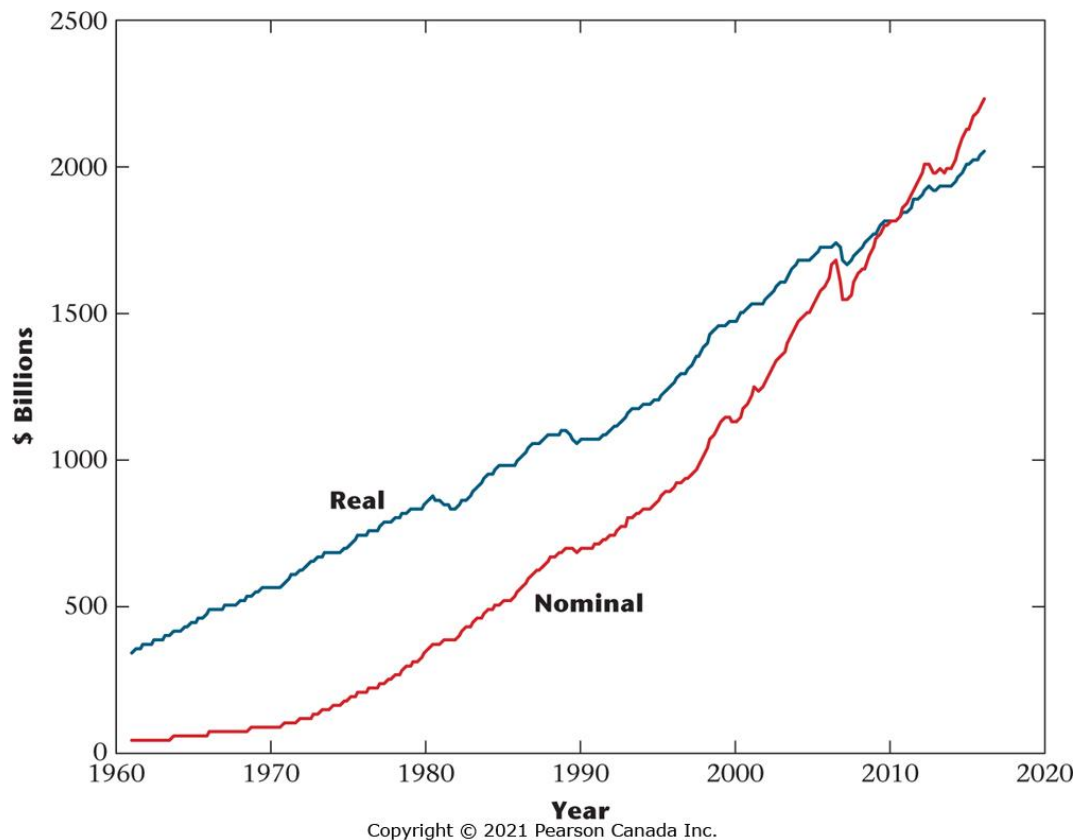
Real GDP₁ = \$130

Real GDP₂ = $\$130 * 1.333 = \173.29

If base year = year 2, then

Real GDP₂ = \$292

Real GDP₁ = $\$292 / 1.333 = \219.05



Measures of the Price Level:

1. Implicit Price Deflator = $\text{Nominal GDP} / \text{Real GDP} * 100$
2. CPI = $\text{Cost of base year quantities at current prices} / \text{Cost of base year quantities at base year prices} * 100$

	Apples	Oranges
Q_1	50	100
P_1	\$1	\$0.80
Q_2	80	120
P_2	\$1.25	\$1.60

Quantity in Year 1:

Year 1 = base year >> P_1 → Nominal GDP_1 = Real GDP_1 = $$(50*1 + 100*0.80) = \130

Year 2 = base year P_2 → Real GDP_1 = $$(50*1.25 + 100*1.60) = \222.50

Quantity in Year 2:

Year 1 = base year >> P_1 → Real GDP_2 = $$(80*1 + 120*0.80) = \176

Year 2 = base year P_2 → Nominal GDP_2 = Real GDP_2 = $$(80*1.25 + 120*1.60) = \292

Implicit Price Deflator = Nominal GDP/Real GDP * 100

	Year 1	Year 2	% Increase
Year 1 = base year	$130/130*100 = 100$	$292/176*100 = 165.9$	$[165.9/100 - 1]*100 = 65.9$
Year 2 = base year	$130/222.50*100 = 58.4$	$292/292*100 = 100$	$[100/58.4 - 1]*100 = 71.2$
Chain-weighting	100	$100*1.685 = 168.5$	$[(1.659*1.712)^{0.50} - 1]*100 = 68.5$

CPI = Cost of base year quantities at current prices/ Cost of base year quantities at base year prices * 100

$$\text{CPI} = 222.5/130 = 171.2 \rightarrow 71.2\%$$

