```
solutions (Predicate logic)
   for questions 1-5 consider,
               I(21) = 'al is an Integer'
               E(x) = 'x is even'
               O(x) = 'x is odd'
    JX (JCX) NE(X)) N JX (J(X) NO(X))
      Ax (1(x) \rightarrow E(x))
3) \forall x \left( I(x) \rightarrow \left( \neg E(x) \rightarrow O(x) \right) \right)
                                 OR \forall x (I(x) \land \neg E(x) \rightarrow O(x))
((x) A (x)) xE
    \forall x (E(x) \rightarrow I(x))
      Lot
           SCX) = X is a sin
          LOC) = ox is a form of lying
                 AX (Z(x) -> L(x))
```

H(x) = x is happy Define the constant: Jeff H(Jef)

6)

- D(x) = x is a dog

 Define constants Tom, Jerry

 D(Tom) A D(Jerry)
- 9) H(x,y) = x is happier than y S(x,y) = x is sadder than y Define constants Jack, Tim, Bob
 - H (Jack, Tim) A S (Jack, Bob)
- to) T(x) = x is bouble maker

 $D(x, y) = \infty$ dislikes y

Define constants Paul, Ben

D(Ben, Paul) -> T(Paul)

12) Proof

I tote that the PCH) is false if and only if there exists an element in the domain for which PCH is false.

But this holds if and only if there excists an element in the domain for which - PCL) is true

The latter holds if and only if $\exists x \neg P(x)$ is true

 $\therefore \neg \forall x P(x) = \exists x \neg p(x)$

13) Proof:

Giving a counter example to the assertion that they have same truth values is enough to prove that they are not equivalent.

Let us assume the domain D=N (natural numbers)

P(x) = x is even Q(x) = x is odd

 $\frac{L \cdot H \cdot S}{\text{This}} = \frac{1}{2} \text{SC} \left(P(x) \vee Q(x) \right) \qquad \text{Every natural number is even or odd}$

₹.₩\$ = ₹x₽6c) √ ₹x Q6c) (

Every natural number is even or every natural number is odd

This is false.

: 4x(P(x) 1 9(x)) = 4x P(y) 1 4x 6(x)

Giving a counter example to the assertion that they have same touth values is enough to prove that they are not equivalent.

Let us assume the domain D = N

P(x) = 'x is even' P(x) = 'x is odd

R.H.S = $(\exists x ?(x) \land \exists x Q(x))$ (there exists a natural number which is even and there exists a natural number which is odd)

This is True.

LH·S = $\exists x (P(x) \land Q(x))$ (there is a natural number which is even and odd)

this is false.

: $\exists x (P(x) \land Q(x)) \neq (\exists x P(G) \land \exists x Q(x))$