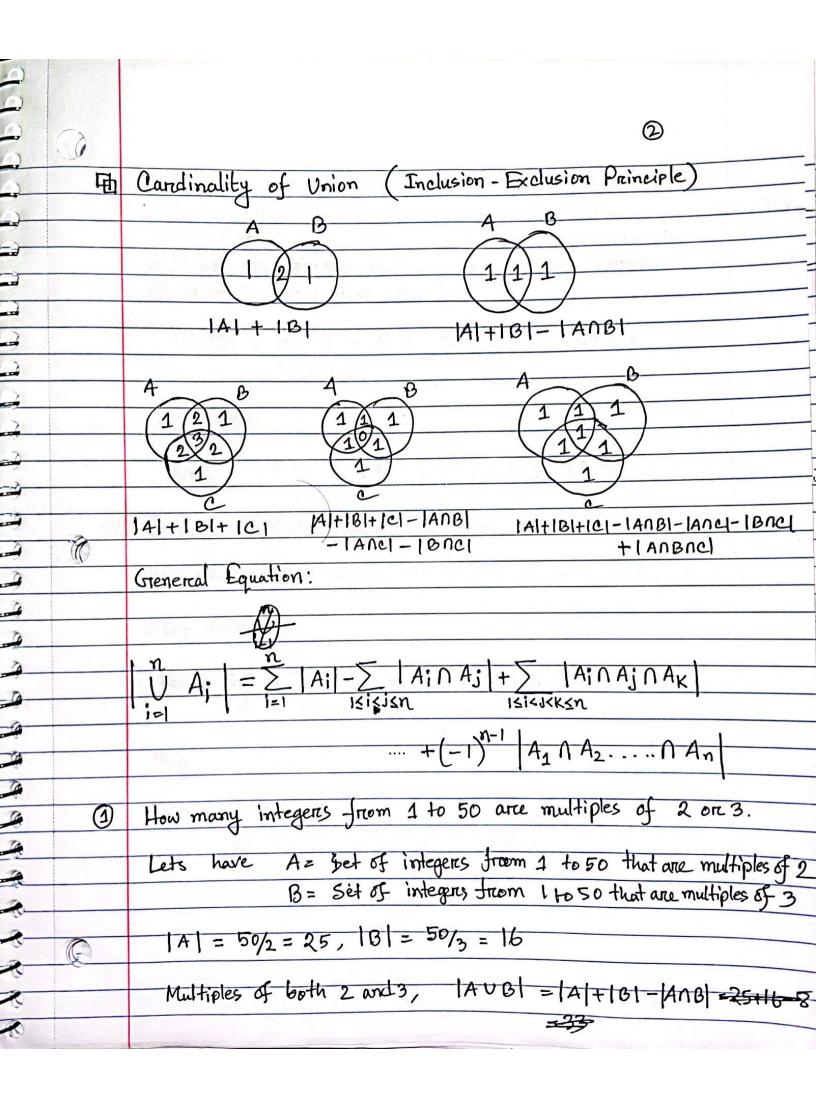
Then AUB= \$1,2,3}, AUC= \$1,2,3}

-



[Note: There are numbers who are multiples of both 2 and 3 like 6,12,18 etc. If we simply sum up then those numbers will be Counted twice. To avoid this, we should make sure those common multiples are counted once. So, we should substract the number of common multiples by once.]

 $|A \cap B|$ = multiples of 2 and 3, that means 6. = 50/6 = 8

SO, |AnB| = 8

likes both?

2

Then, | | AUB| = | A| + | B| - | ANB| = 25+16-8 = 33

In a group of 50 students, 24 like cold drinks and 36 like hot drinks. Each student likes one of the drinks. How many

Let, Set of students who like cold drunks > X >
Set of students who like hot drunks Y

Then | X = 24, | Y = 36, | X UY | = 50

So, |XUY| = |X| + |Y| - |XNY| $\Rightarrow |XNY| = |X| + |Y| - |XUY|$ = 24 + 36 - 50= 60 - 50

= 10

| | | lacktriangle |
|----------|--|---|
| <u>a</u> | <u> </u> | |
| 0 | —————————————————————————————————————— | Cardinality of Power set with proof by induction. |
|)) | | If $ A =n$ then, $ P(A) =2^n$ |
| 9 | | Base case: |
| 3 | | Suppose A={} |
| 9 | | SO, A = 0 |
| 9 | | here, $P(A) = 20$ f Because on empty set is a definite element of power set. |
| 3 | | Then $ P(A) = 1 = 2^{\circ}$ |
| 9 | Ar Carlo | This satisfies the theorem |
| • | | T 1 1' 41 |
| 2 | | Induction Step: |
| <i>9</i> | | If for any IAI=n, IP(A) 1= 2n Induction Hypothesis |
| <u>a</u> | | Then for any B =n+1, P(B) = 2n+1 [we need to prove] |
| | | |
| 3 | | Let $A = \{a_1, a_2, a_3, \dots, a_n\}$ |
| 0 | | and B= {a1, a2, a3, an, anti} |
| | * | Then we can say $B = AV \frac{1}{2}a_{n+1}$? |
| | | For B there two kinds of Subsets: |
| | | (1) Subsets a that donot include ant. These Subsets are |
| 9 | | exactly same as subsets of A. So, there should be 2n Subsets |
| | | Alia 2n subsets. |
| | | 2) For the latter, we can say XU Jantil where VCP(A) |
| • | | As there 2n possible choice for X, There must 2n Subsets - |
| 9 | | That includes anti. |
| 9 | | |

= B-A

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