

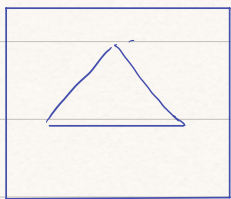
## Normalized Device Coordinates (NDC)

given some immediate mode, vertices in 2D

$$(0, 0.5)$$

$$(0.5, -0.25)$$

$$(0.5, 0.25)$$



← the range of this triangle  $[-1, 1]$  is NDC

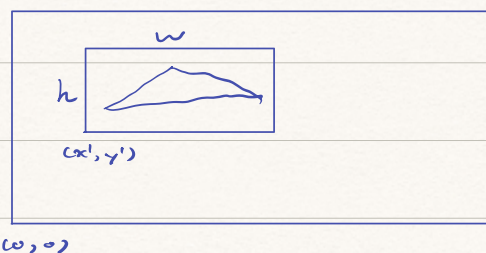
when we're drawing screen, we have to draw to frame buffer, which is the raster image to display, a 2D-grid of picture in memory. Frame buffer exist on screen space and defined in screen space. Viewport defines the transform from normalized coordinate to screen space. i.e.  $(w, 0) \rightarrow (\frac{w}{2}, \frac{h}{2})$

opened drawable window

$$(x, y) \rightarrow (\frac{(x+1)w}{2}, \frac{(y+1)h}{2})$$

To draw on the window which has the offset  $(x', y')$ , we have

$$(x, y) \rightarrow (\frac{(x+1)w}{2} + x', \frac{(y+1)h}{2} + y')$$



Affine Transform.

Affine: 1) Straight lines are preserve

2) Parallelism is preserved i.e. transform is same scale.

Scale: keep ratio, but scale up/down  $\begin{pmatrix} x \\ y \end{pmatrix} \rightarrow \begin{pmatrix} s_x x \\ s_y y \end{pmatrix}$

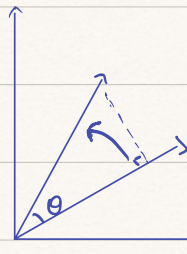
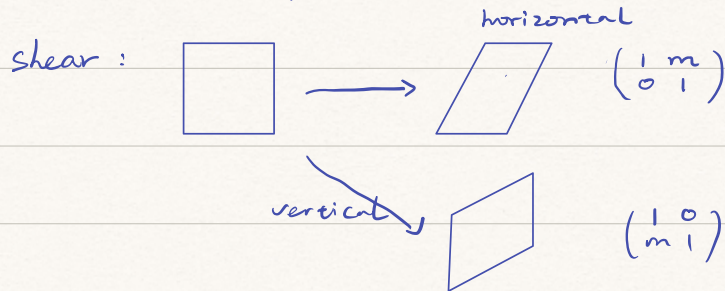
\* we usually transform vertices only, not all objects.

this mapping is achieved via matrix multiplication,

$$\begin{pmatrix} x \\ y \end{pmatrix} \cdot \begin{pmatrix} s_x & 0 \\ 0 & s_y \end{pmatrix} = \begin{pmatrix} s_x x \\ s_y y \end{pmatrix}$$

so,  $x$  only:  $\begin{pmatrix} s_x & 0 \\ 0 & 1 \end{pmatrix}$ ,  $y$  only:  $\begin{pmatrix} 1 & 0 \\ 0 & s_y \end{pmatrix}$ .

scaling is reversible. To get it reversed, multiply by  $\begin{pmatrix} \frac{1}{s_x} & 0 \\ 0 & \frac{1}{s_y} \end{pmatrix}$



$$\begin{pmatrix} x \\ y \end{pmatrix} \begin{pmatrix} \cos \theta & \sin \theta \\ \sin \theta & \cos \theta \end{pmatrix} = \begin{pmatrix} x' \\ y' \end{pmatrix}$$

the inverse of this rotation is to rotate

back (clockwise)

$$\begin{pmatrix} \cos \theta & \sin \theta \\ \sin \theta & \cos \theta \end{pmatrix}^{-1} = \begin{pmatrix} \cos \theta & \sin \theta \\ -\sin \theta & \cos \theta \end{pmatrix}$$

reflection



$$\vec{v} = \begin{pmatrix} v_x \\ v_y \end{pmatrix} \quad \begin{pmatrix} x \\ y \end{pmatrix} \begin{pmatrix} v_x^2 - v_y^2 & 2v_x v_y \\ 2v_x v_y & v_y^2 - v_x^2 \end{pmatrix}$$

the inverse is exactly same

translation



just move it!  $\begin{pmatrix} x+dx \\ y+dy \end{pmatrix}$

Homogeneous coordinates

point:  $\begin{pmatrix} x \\ y \\ 1 \end{pmatrix} \longrightarrow \begin{pmatrix} x \\ y \\ 1 \end{pmatrix}$

direction:  $\begin{pmatrix} dx \\ dy \\ 0 \end{pmatrix} \longrightarrow \begin{pmatrix} dx \\ dy \\ 0 \end{pmatrix}$

$$\begin{pmatrix} x \\ y \\ 1 \end{pmatrix} \cdot \begin{pmatrix} 1 & 0 & dx \\ 0 & 1 & dy \\ 0 & 0 & 1 \end{pmatrix}$$