



Types

Chapters 7, 8

Data Types

- Types provide implicit context for operations
- C: `a + b`
 - integer/floating point addition
- Pascal: `new p`
 - allocate right size
- C: `new my_type()`
 - allocate right size
 - call right constructor

Data Types

- Boolean
 - true/false; one byte, sometimes one bit
 - C: integers, true = non-0, false = 0
- Character
 - one byte – ASCII
 - two bytes - Unicode
- Numeric
 - integers, reals
 - complex: C, Fortran, Scheme (pair of floats)
 - rational: Scheme (pair of integers)
- Discrete (or ordinal)
 - integers, Booleans, characters
 - countable, well-define predecessor/successor
- Scalar (or simple): discrete, rational, real, complex

Data Types

- Enumeration

- introduced in Pascal:

```
type weekday = (sun, mon, tue, wed, thu, fri, sat);
```

- ordered: `mon < tue`; can index an array

- Subrange: `type test_score = 0..100`

- Composite (non-scalar)

- Records (struct) – collection of fields
 - Arrays – most common; map from index to elements
 - strings = arrays of characters
 - Sets – powerset of base type
 - Pointers – references to objects; recursive data types
 - Lists – sequence; no map; recursive definition, fundamental in functional programming
 - Files – like arrays but with current position

Type checking

- *Type equivalence*: two types are the same
- *Type compatibility*: a type can be used in a context
- *Type inference*: deduce the type from components
- *Type clash*: violation of type rules

Type Systems

- *Strongly typed* language
 - prohibits any application of an operation to an object that is not intended to support that operation
- *Statically typed* language
 - strongly typed
 - at compile time – good performance
 - C, C++, Java
 - C: more strongly typed with each new version
- *Dynamically typed* language
 - at run time - ease of programming
 - Scheme, Lisp, Smalltalk – strongly typed
 - Scripting: Python, Ruby – strongly typed

Type Checking: Equivalence

- *Structural equivalence*
 - same components put together in the same way
 - C, Algol-68, Modula-3, ML
- *Name equivalence*
 - lexical occurrence
 - each definition is a new type
 - Java, C#, Pascal

Type Checking: Equivalence

- Structural equivalence:
 - format should not matter

```
type R1 = record
  a, b : integer
end;
```

```
type R1 = record
  a : integer;
  b : integer;
end;
```

- What about order? (most languages consider it equivalent)

```
type R3 = record
  b : integer;
  a : integer
end;
```


Type Checking: Equivalence

- Structural equivalence: problem

```
type student = record
  name, address : string
  age : integer
type school = record
  name, address : string
  age : integer
x : student;
y : school;
...
x := y; -- is this an error?
```

- compiler says it's okay
- programmer most likely says it's an error

Type Checking: Equivalence

- Name equivalence
 - Distinct definitions mean distinct types
 - If the programmer takes the time to write two type definitions, then they are different types
 - Aliases

```
type new_type = old_type (* Algol syntax *)  
typedef old_type new_type /* C syntax */
```

- Are aliases the same or different types?
- Different: *strict name equivalence*
- Same: *loose name equivalence*

Type Checking: Equivalence

- Strict name equiv.:
 - `blink` different from `alink`
 - `p, q` – same type; `r, u` – same type
- Loose name equiv.:
 - `blink, alink` – same type
 - `p, q` – same type; `r, s, u` – same type
- Structural equiv.:
 - `p, q, r, s, t, u` – same type

```
type cell = ...           -- whatever
type alink = pointer to cell
type blink = alink        -- alias
p, q : pointer to cell
r : alink
s : blink
t : pointer to cell
u : alink
```

Type Checking: Conversion

- *Type conversion (cast):* **explicit** conversion

```
r = (float) n;
```

- *Type coercion:* **implicit** conversion
 - very useful
 - weakens type security
 - dynamically typed languages: very important
 - statically typed languages: wide variety
 - C: arrays and pointers intermixed
 - C++: programmer-defined coercion to and from existing types to a new type (class)

Type Checking: Compatibility

- *Type compatibility*
 - more important than equivalence
 - most of the time we need compatibility
 - assignment: RHS compatible with LHS
 - operation: operands types compatible with a common type that supports the operation
 - subroutine call: arguments types compatible with formal parameters types

Type Checking: Inference

- *Type inference*

- infer expression type from components
- $\text{int} + \text{int} \Rightarrow \text{int}$
- $\text{float} + \text{float} \Rightarrow \text{float}$
- subranges cause complications

```
type Atype = 0..20; Btype = 10..20;
```

```
var a : Atype; b : Btype;
```

- What is the type of $a + b$?

Type Checking: Inference

- Type inference

- declarations: type inferred from the context

- C#: var

```
var i = 123;  
// equiv. to:  
int i = 123;
```

```
var map = new Dictionary<string, int>();  
// equiv. to:  
Dictionary<string, int> map = new  
Dictionary<string, int>();
```

Type Checking: Inference

- C++: auto

```
auto reduce = [](list<int> L, int f(int, int), int s) {  
    for (auto e : L) { s = f(e, s); }  
    return s;  
};
```

...

```
int sum = reduce(my_list, [](int a, int b){return a+b;}, 0);  
int prod = reduce(my_list, [](int a, int b){return a*b;}, 1);
```

- the auto keyword allows to omit the type:

```
int (*reduce) (list<int>, int (*)(int, int), int)  
    = [](list<int> L, int f(int, int), int s) {  
        for (auto e : L) { s = f(e, s); }  
        return s;  
    };
```

Type Checking: Inference

- C++: `decltype`

- match the type of an existing expression
- the type of `sum` depends on the types of `A` and `B` under the coercion rules of C++
- both `int` gives `int`
- one is `double` gives `double`

```
template <typename A, typename B>
...
    A a;
    B b;
    decltype(a + b) sum;
```

Polymorphism

- *Polymorphism* (polymorphous = multiform)
- code works with multiple types
 - must have common characteristics
- *parametric polymorphism*: take a type as parameter
 - explicit parametric polymorphism (*generics*, C++: *templates*) appears in statically typed languages
 - implemented at compile time
- *subtype polymorphism*: code works with subtypes
 - object-oriented languages
- combination (subtype + parametric polymorphism)
 - container classes
 - `List<T>`, `Stack<T>`; T instantiated later

Polymorphism

- *Implicit:*
 - Scheme:

```
(define min (lambda (a b) (if (< a b) a b)))
```
 - applied to arguments of any type to which it can be applied
 - disadvantage: checked dynamically
- *Explicit: generics*
 - C++: *templates*
 - checked statically
- Generics in object-oriented programming
 - parametrize entire class
 - *container*

Polymorphism

- Ada example: overloading (left) vs generics (right)

```
function min(x, y : integer)
  return integer is
begin
  if x < y then return x;
  else return y;
  end if;
end min;

function min(x, y : long_float)
  return long_float is
begin
  if x < y then return x;
  else return y;
  end if;
end min;
```

```
generic
  type T is private;
  with function "<"(x, y : T) return Boolean;
function min(x, y : T) return T;

function min(x, y : T) return T is
begin
  if x < y then return x;
  else return y;
  end if;
end min;

function int_min is new min(integer, "<");
function real_min is new min(long_float, "<");
function string_min is new min(string, "<");
function date_min is new min(date, date_precedes);
```

■ C++ example

```
template<class item, int max_items = 100>
class queue {
    item items[max_items];
    int next_free, next_full, num_items;
public:
    queue() : next_free(0), next_full(0), num_items(0) { }
    bool enqueue(const item& it) {
        if (num_items == max_items) return false;
        ++num_items;  items[next_free] = it;
        next_free = (next_free + 1) % max_items;
        return true;
    }
    bool dequeue(item* it) {
        if (num_items == 0) return false;
        --num_items;  *it = items[next_full];
        next_full = (next_full + 1) % max_items;
        return true;
    }
};

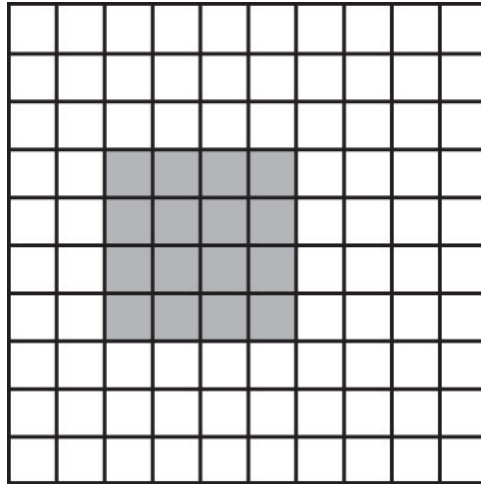
...
queue<process> ready_list;
queue<int, 50> int_queue;
```

Arrays

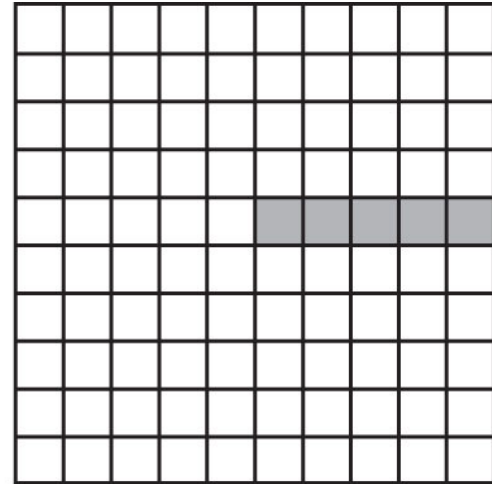
- Arrays
 - the most important composite data type
 - semantically, map: index type \rightarrow element type
- Homogenous data
- Index type
 - usually discrete type: int, char, enum, subranges of those
 - non-discrete type: *associative array*, *dictionary*, *map*
 - implemented using hash tables or search trees
- Dense – most positions non-zero
 - sparse arrays – stored using linked structures

Arrays

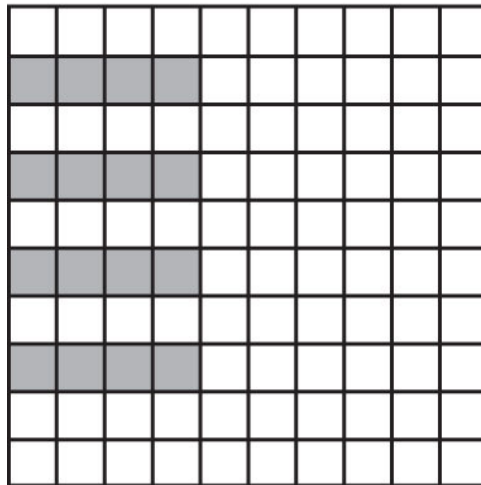
- Slices



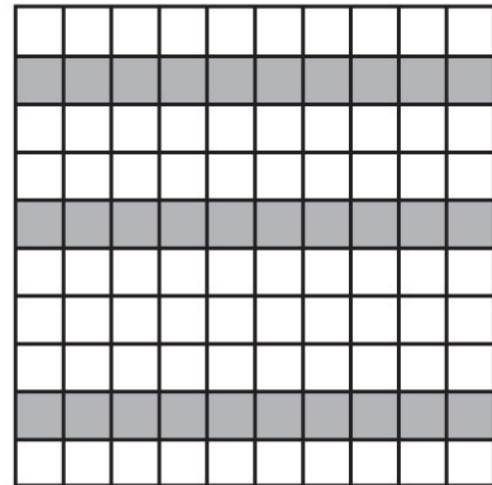
`matrix(3:6, 4:7)`



`matrix(6:, 5)`



`matrix(:4, 2:8:2)`



`matrix(:, (/2, 5, 9/))`

Arrays: Dimensions, Bounds, Allocation

- Static allocation:
 - array with lifetime the entire program
 - shape known at compile time
- Stack allocation:
 - array with lifetime inside subroutine
 - shape known at compile time
- Heap / stack allocation
 - dynamically allocated arrays
 - *dope vector*: holds shape information at run time
 - compiled languages need the number of dimensions
 - shape known at elaboration time – can allocate on stack
 - shape changes during execution: allocated on heap

Arrays

- Example: C dynamic local array

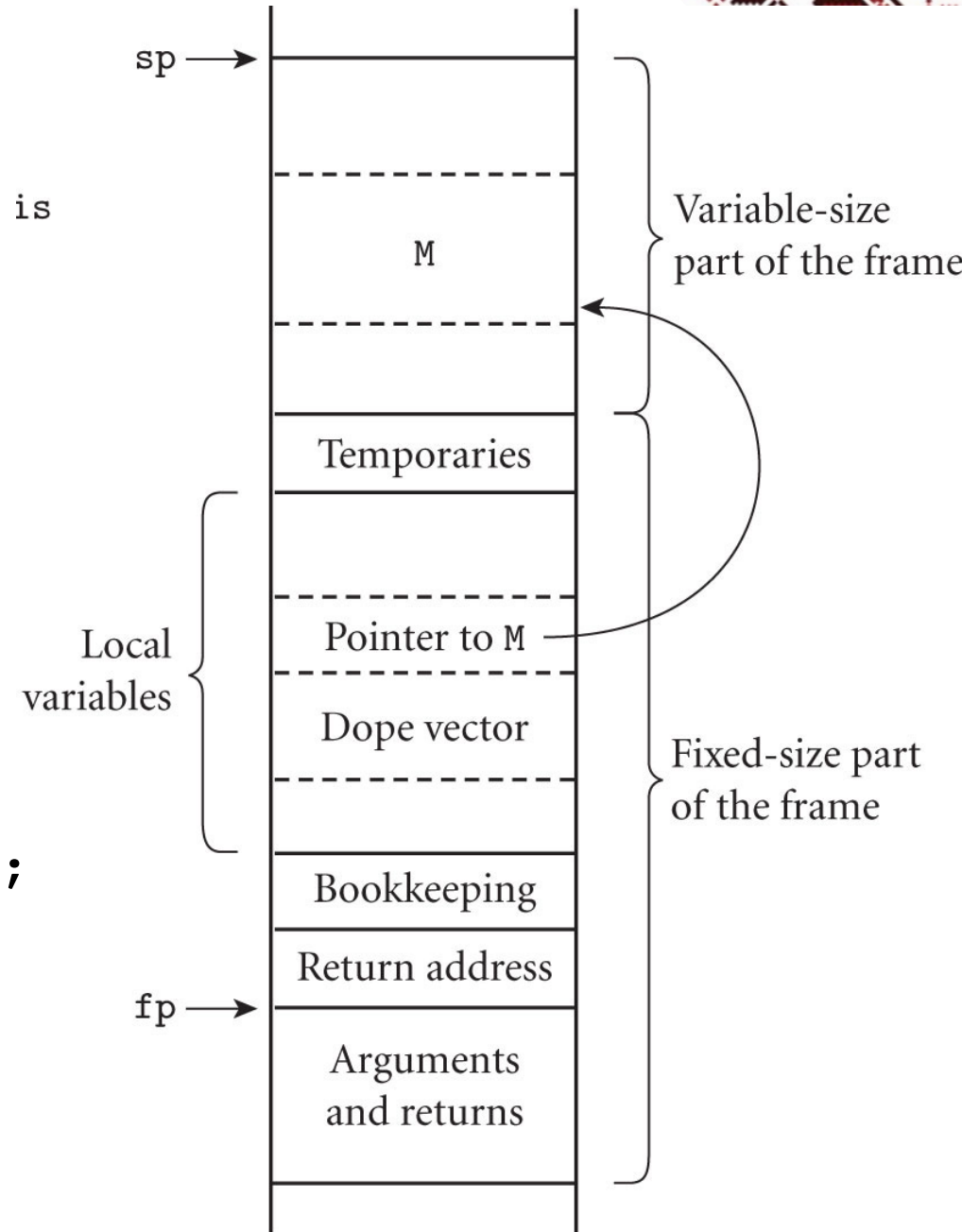
```
void square(int n, double M[n][n]) {  
    double T[n][n];  
    for (int i = 0; i < n; i++) { // copy product to T  
        for (int j = 0; j < n; j++) {  
            double s = 0;  
            for (int k = 0; k < n; k++)  
                s += M[i][k] * M[k][j];  
            T[i][j] = s;  
        }  
    }  
    for (int i = 0; i < n; i++) { // copy T back to M  
        for (int j = 0; j < n; j++)  
            M[i][j] = T[i][j];  
    }  
}
```

Arrays

- Shape known at elaboration time
 - can be allocated on stack
 - in the variable-size part

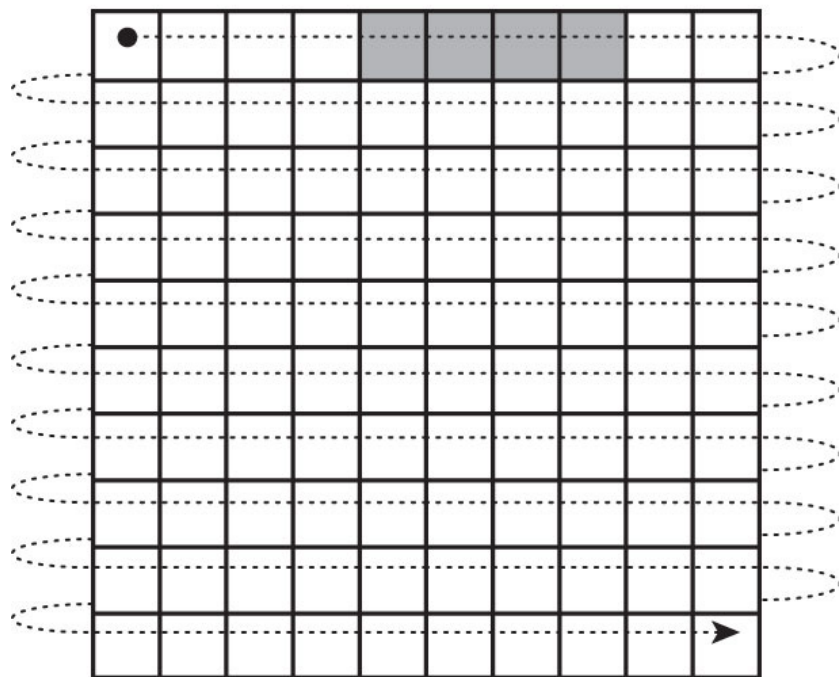
- Example:

```
// C99:  
void foo (int size) {  
    double M[size][size];  
    ...  
}
```

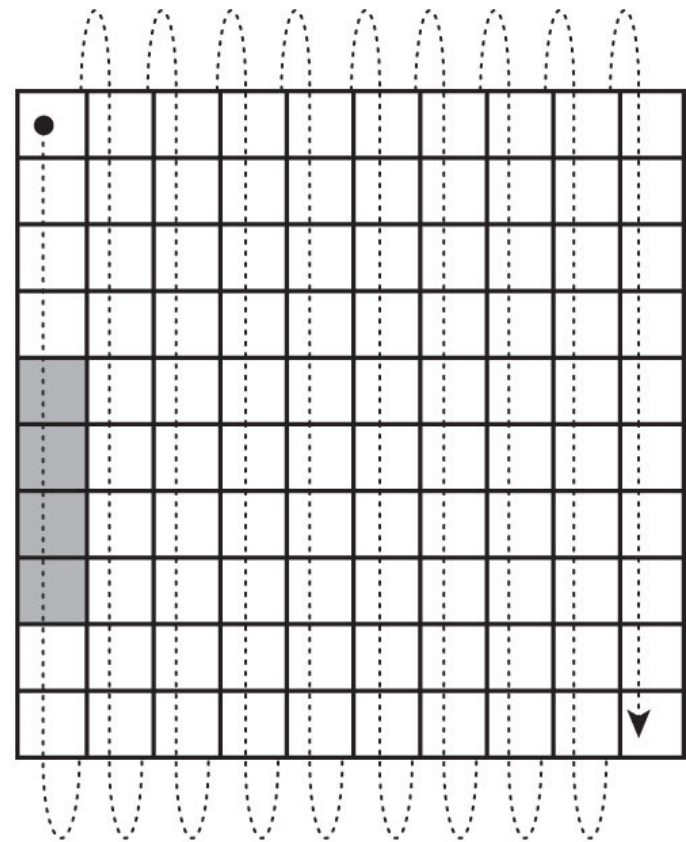


Arrays

- Memory layout
 - column major order – Fortran
 - row major order – everybody else



Row-major order



Column-major order

Arrays

- Memory layout
- Contiguous allocation
 - consecutive locations in memory: $A[2, 4]$, $A[2, 5]$
 - consecutive rows adjacent in memory
- Row pointers
 - consecutive rows anywhere in memory
 - extra memory for pointers
 - rows can have different lengths (ragged array)
 - can construct an array from existing rows without copying
- C, C++, C# - allow both
- Java – only row-pointer for all arrays

Arrays

- Example: C – array of strings
 - true two-dimensional array

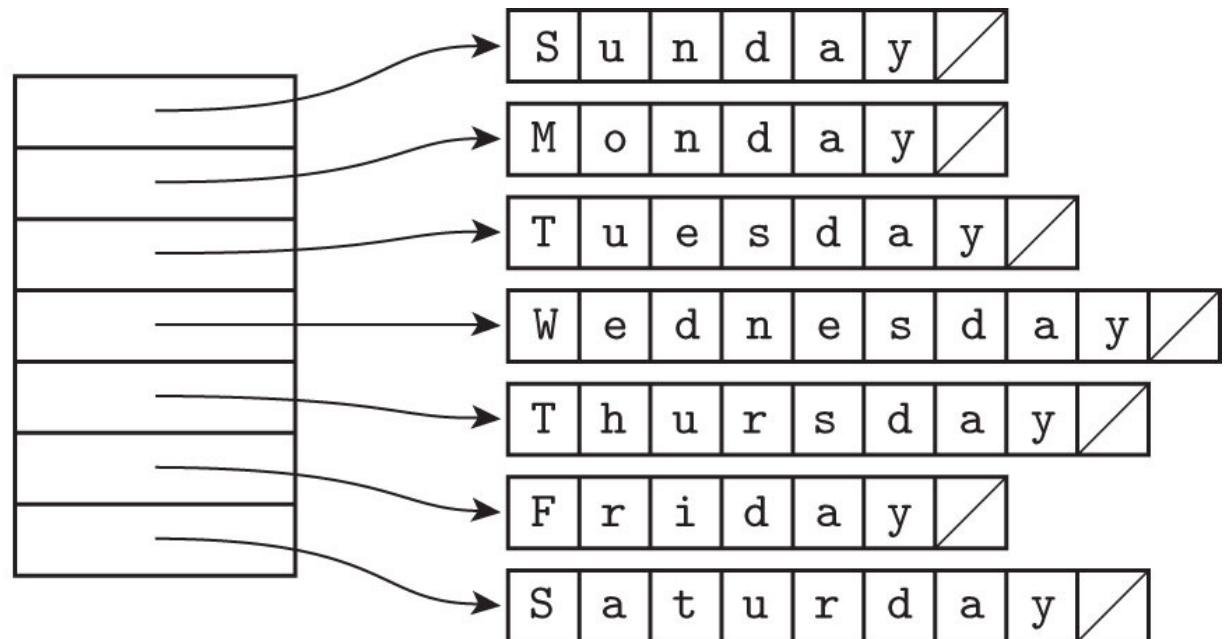
```
char days[][10] = {  
    "Sunday", "Monday", "Tuesday",  
    "Wednesday", "Thursday",  
    "Friday", "Saturday"  
};  
...  
days[2][3] == 's'; /* in Tuesday */
```

S	u	n	d	a	y			
M	o	n	d	a	y			
T	u	e	s	d	a	y		
W	e	d	n	e	s	d	a	y
T	h	u	r	s	d	a	y	
F	r	i	d	a	y			
S	a	t	u	r	d	a	y	

Arrays

- Example: C – array of strings
 - array of pointers

```
char *days[] = {  
    "Sunday", "Monday", "Tuesday",  
    "Wednesday", "Thursday",  
    "Friday", "Saturday"  
};  
...  
days[2][3] == 's'; /* in Tuesday */
```



Arrays

■ Address calculation

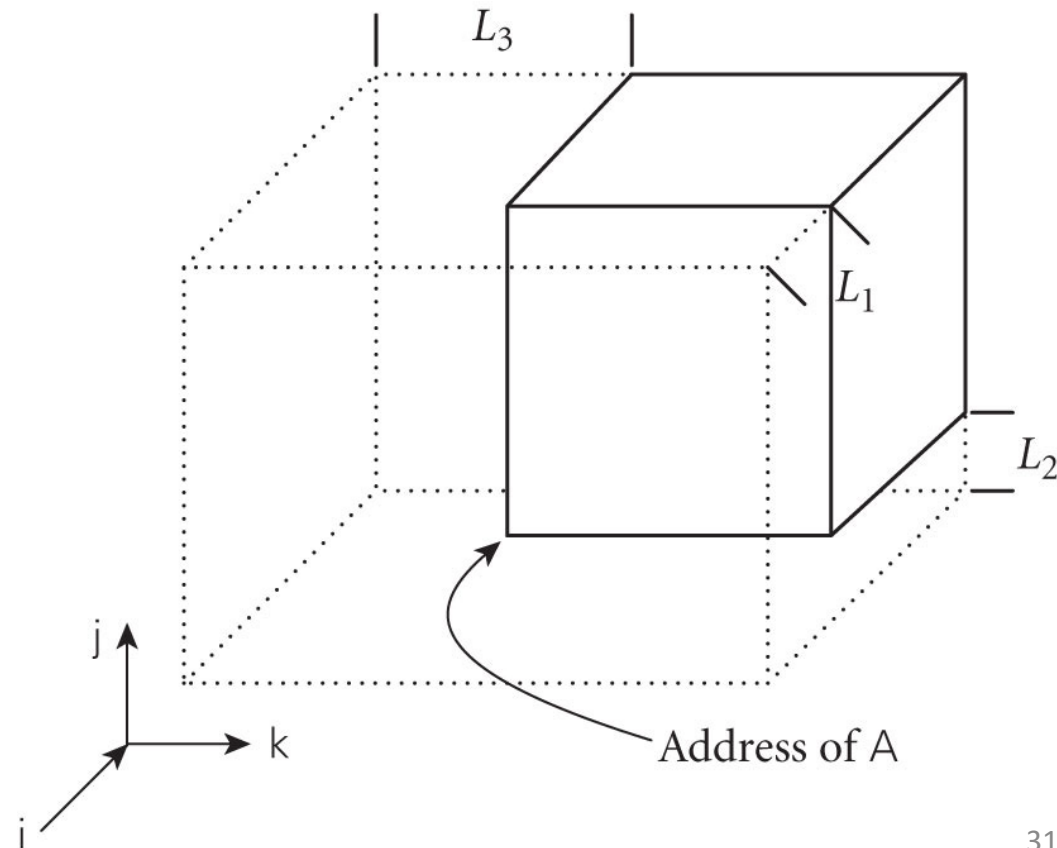
A : array $[L_1..U_1]$ of array $[L_2..U_2]$ of array $[L_3..U_3]$ of `elem_type`;

$S_3 = \text{size of elem_type}$

$S_2 = (U_3 - L_3 + 1) \times S_3$

$S_1 = (U_2 - L_2 + 1) \times S_2$

address of $A[i, j, k]$
= address of A
+ $(i - L_1) \times S_1$
+ $(j - L_2) \times S_2$
+ $(k - L_3) \times S_3$



Arrays

- Faster address calculation

address of $A[i, j, k]$

$$= \text{address of } A + (i - L_1) \times S_1 + (j - L_2) \times S_2 + (k - L_3) \times S_3$$

- Fewer operations

- $C = [(L_1 \times S_1) + (L_2 \times S_2) + (L_3 \times S_3)]$
- C – known at compile time

address of $A[i, j, k]$

$$= \text{address of } A + (i \times S_1) + (j \times S_2) + (k \times S_3) - C$$

Sets

- *Set*: unordered collection of an arbitrary number of distinct values of a common type
- Implementation
 - *characteristic array* – one bit for each value (small base type)
 - efficient operations – bitwise op
 - general implementation: hash tables, trees, etc.
 - Python, Swift – built-in sets
 - Others use dictionaries, hashes, maps

```
X = set(['a', 'b', 'c', 'd']) # set constructor
Y = {'c', 'd', 'e', 'f'}     # set literal
U = X | Y                    # union
I = X & Y                     # intersection
D = X - Y                    # difference
O = X ^ Y                    # symmetric diff.
'c' in I                     # membership
```


Pointers and Recursive Types

- *Pointer*

- a variable whose value is a reference to some object
- not needed with a reference model of variables
- needed with a value model of variables
- efficient access to complicated objects

- *Recursive type*

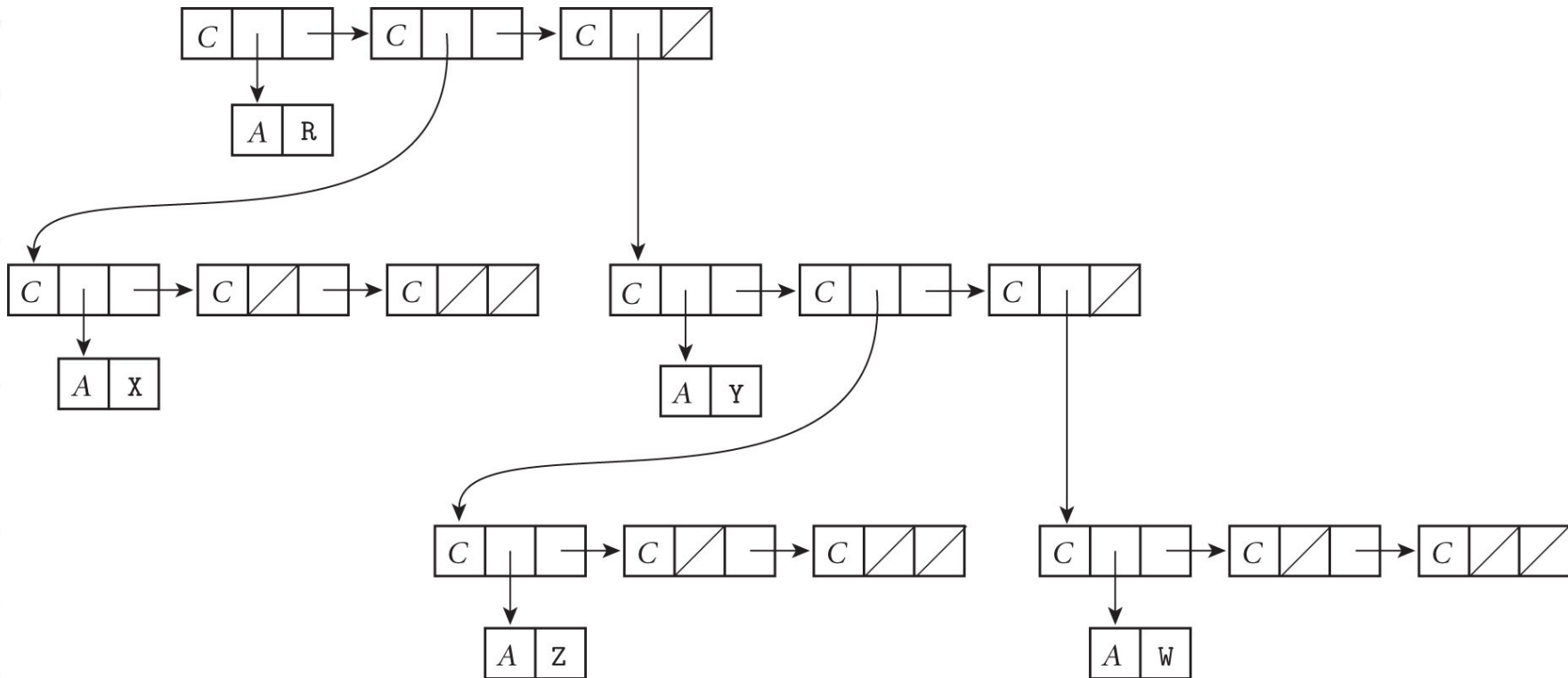
- objects contain references to other objects
- can create dynamic data structures

- Pointer \neq address

- pointer = high-level concept; reference to object
- address = low-level concept; location in memory
- pointers are implemented as addresses

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```
' (#\R (#\X ()()) (#\Y (#\Z ()()) (#\W ()())) )
```



Pointers and Recursive Types

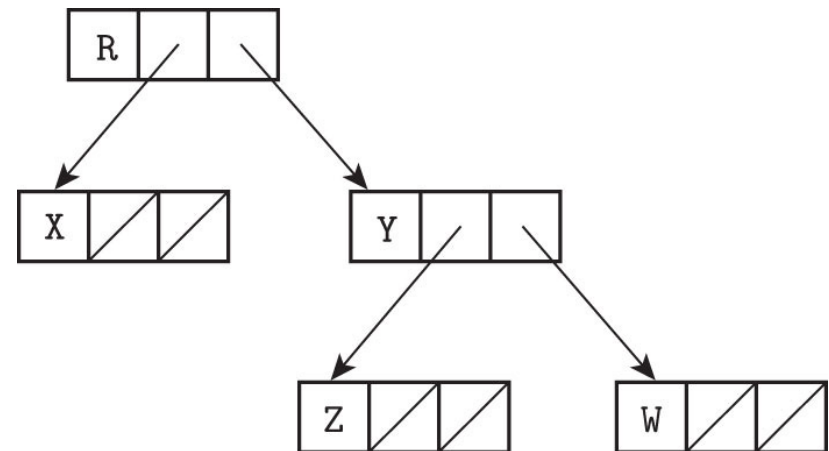
- Value model example: Tree in C

```
struct chr_tree {  
    struct chr_tree *left, *right;  
    char val;  
};
```

```
my_ptr = malloc(sizeof(struct chr_tree));
```

- C++, Java, C# – type safe

```
my_ptr = new chr_tree(arg_list);  
(*my_ptr).val = 'X';  
my_ptr->val = 'X';
```



Pointers and Recursive Types

- *Dangling reference*

- live pointer that no longer points to a valid object
- Example: caused by local variable after subroutine return:

```
int i = 3;
int *p = &i;
...
void foo(){ int n = 5; p = &n; }
...
cout << *p;           // prints 3
foo();
...
cout << *p; // undefined behavior: n is no
              longer live
```

Pointers and Recursive Types

- Dangling reference
 - Example: caused by manual deallocation:

```
int *p = new int;  
*p = 3;  
...  
cout << *p;          // prints 3  
delete p;  
...  
cout << *p; // undefined behavior: *p has been  
              reclaimed
```

- Problem: a dangling reference can write to memory that is part of a different object; it may even interfere with bookkeeping, corrupting the stack or heap

Garbage collection

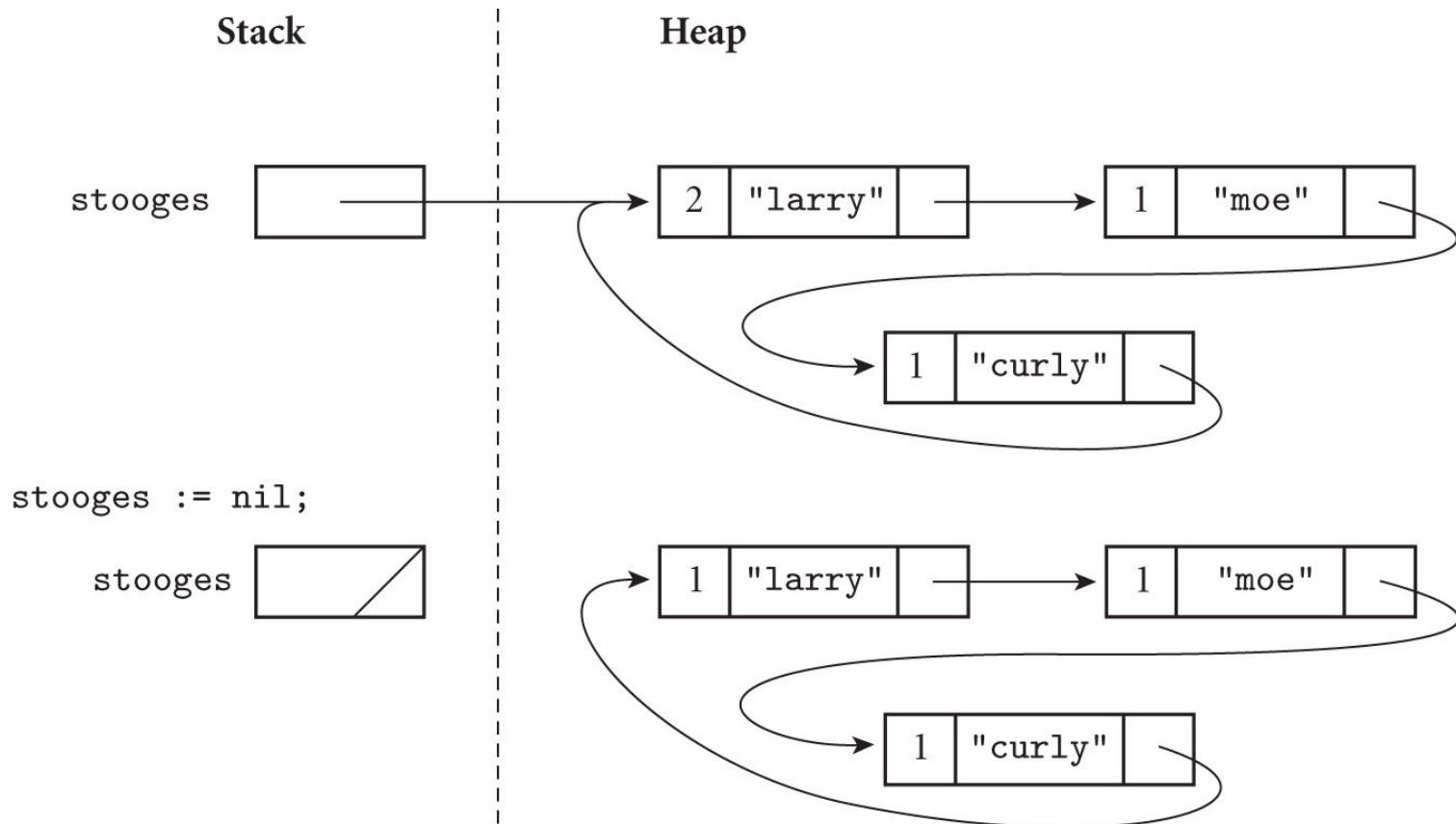
- *Garbage collection*
 - automatic reclamation of memory
 - slower than manual (`delete`)
 - difficult to implement
 - eliminates the need to check for dangling references
 - very convenient for programmers
 - essential for functional languages
 - increasingly popular in imperative languages
 - Java, C#

Garbage collection

- *Reference counts*
 - object no longer useful when no pointers to it exist
 - store *reference count* for each object
 - initially set to 1
 - update when assigning pointers
 - update on subroutine return
 - when 0, reclaim object

Garbage collection

- Reference counts
 - $\text{count} \neq 0$ does not necessarily mean useful (circular lists)



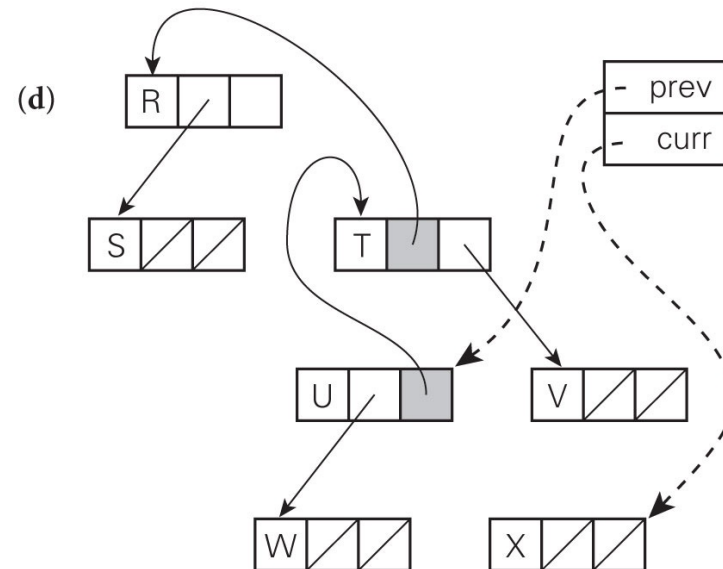
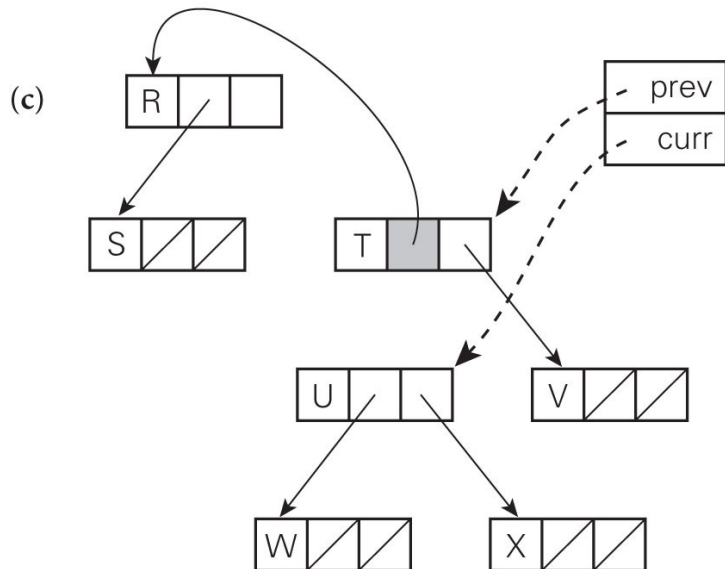
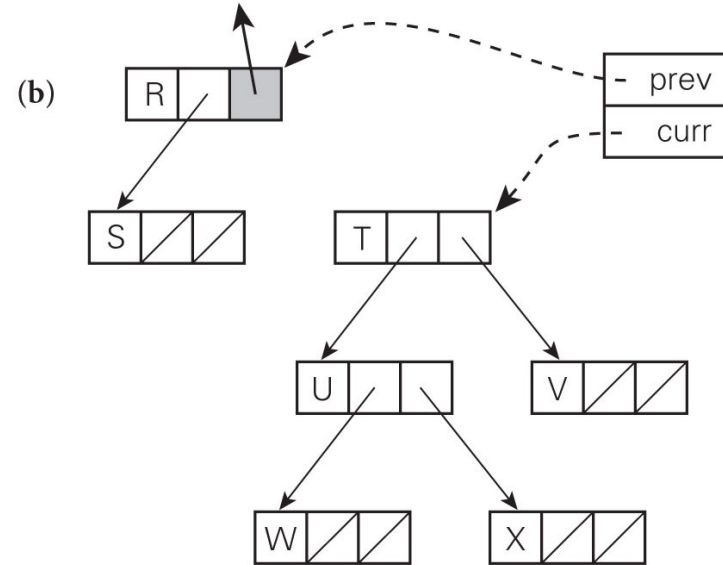
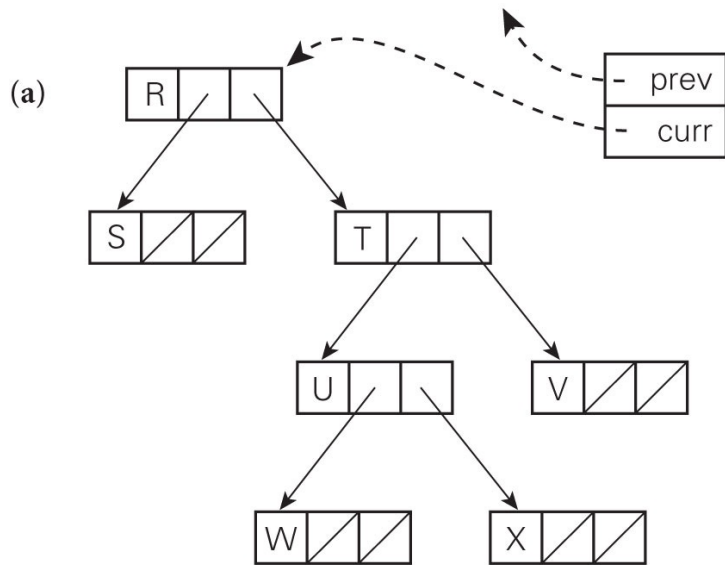
Garbage collection

- Smart pointers in C++
- `unique_ptr`
 - one object only
- `shared_ptr`
 - implements a reference count
- `weak_ptr`
 - does not affect counts; for, e.g., circular structures

Garbage collection

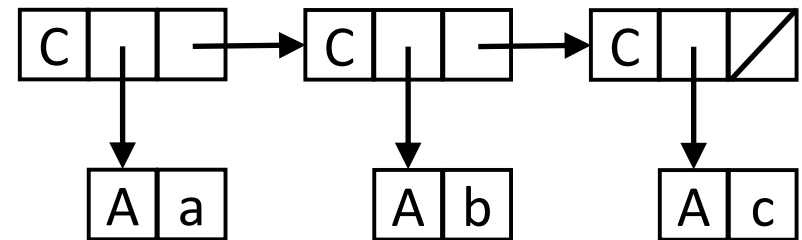
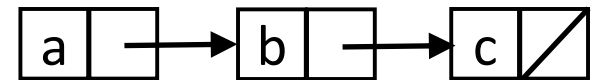
- *Tracing collection*
 - object useful if reachable via chain of valid pointers from outside the heap
 - *Mark-and-sweep*
 - (1) mark entire heap as “useless”
 - (2) starting from outside heap, recursively mark as “useful”
 - (3) move “useless” block from heap to free list
 - Step (2) requires a potentially very large stack
 - Without stack: *pointer reversal* (next slide)
- *Stop-and-copy*: defragmentation
 - use half of heap; copy useful data compactly to the other one

Pointer reversal



Lists

- *List*: empty or (head + tail)
- essential in functional and logic programming (recursive)
- used also in imperative languages
- *Homogeneous* (same type): ML
- *Heterogeneous*: Scheme



Lists

- Scheme:

- `' (. . .)` prevents evaluation; also `(quote (. . .))`

`(+ 1 2) ⇒ 3`

`' (+ 1 2) ⇒ ' (+ 1 2)`

`(cons 'a '(b)) ⇒ '(a b)`

`(car '(a b)) ⇒ a`

`(car '()) ⇒ error`

`(cdr '(a b c)) ⇒ '(b c)`

`(cdr '(a)) ⇒ '()`

`(cdr '()) ⇒ error`

`(append '(a b) '(c d)) ⇒ '(a b c d)`

Lists

- *List comprehension*

- adapted from traditional math set notation:

$$\{i \times i \mid i \in \{1, \dots, 10\} \wedge i \bmod 2 = 1\}$$

- Example: Python

```
[i*i for i in range(1, 10) if i % 2 == 1]
```

```
⇒ [1, 9, 25, 49, 81]
```