

CS 2209A

Cheat sheet for midterm

Rules of inference:

$ \begin{array}{c} p \\ p \rightarrow q \\ \hline q \end{array} $	Modus ponens
$ \begin{array}{c} \neg q \\ p \rightarrow q \\ \hline \neg p \end{array} $	Modus tollens
$ \begin{array}{c} p \\ \hline p \vee q \end{array} $	Addition
$ \begin{array}{c} p \wedge q \\ \hline p \end{array} $	Simplification

$ \begin{array}{r} p \\ q \\ \hline p \wedge q \end{array} $	Conjunction
$ \begin{array}{r} p \rightarrow q \\ q \rightarrow r \\ \hline p \rightarrow r \end{array} $	Hypothetical Syllogism
$ \begin{array}{r} p \vee q \\ \neg p \\ \hline q \end{array} $	Disjunctive Syllogism
$ \begin{array}{r} p \vee q \\ \neg p \vee r \\ \hline q \vee r \end{array} $	Resolution

Laws of propositional logic

Idempotent laws:	$p \vee p \equiv p$	$p \wedge p \equiv p$
Associative laws:	$(p \vee q) \vee r \equiv p \vee (q \vee r)$	$(p \wedge q) \wedge r \equiv p \wedge (q \wedge r)$
Commutative laws:	$p \vee q \equiv q \vee p$	$p \wedge q \equiv q \wedge p$
Distributive laws:	$p \vee (q \wedge r) \equiv (p \vee q) \wedge (p \vee r)$	$p \wedge (q \vee r) \equiv (p \wedge q) \vee (p \wedge r)$
Identity laws:	$p \vee F \equiv p$	$p \wedge T \equiv p$
Domination laws:	$p \wedge F \equiv F$	$p \vee T \equiv T$
Double negation law:	$\neg \neg p \equiv p$	
Complement laws:	$p \wedge \neg p \equiv F, \neg T \equiv F$	$p \vee \neg p \equiv T, \neg F \equiv T$
De Morgan's laws:	$\neg(p \vee q) \equiv \neg p \wedge \neg q$	$\neg(p \wedge q) \equiv \neg p \vee \neg q$
Absorption laws:	$p \vee (p \wedge q) \equiv p$	$p \wedge (p \vee q) \equiv p$
Conditional identities:	$p \rightarrow q \equiv \neg p \vee q$	$p \leftrightarrow q \equiv (p \rightarrow q) \wedge (q \rightarrow p)$