

1. (2 points)

Suppose

$$f(x) = |x| \cdot x$$

Then

$$f^{-1}(x) = \text{_____ if } x \geq 0,$$

and

$$f^{-1}(x) = \text{_____ if } x \leq 0.$$

Hint: Compute the inverse function separately in the two cases.
It may also help to draw the graph of f .

Answer(s) submitted:

- sqrtx
- sqrt-x

(score 0.5)

2. (2 points)

$$\text{Let } f(x) = 9 + (3x + 7)^3.$$

$$\text{Find } f^{-1}(x) = \text{_____}$$

$$\text{Find } (f(x))^{-1} = \text{_____}$$

Answer(s) submitted:

-
-

(incorrect)

3. (4 points)

Suppose

$$f(x) = x + 4 \quad \text{and} \quad g(x) = 2x - 5.$$

Then

$$(f \circ g)(x) = \text{_____}$$

$$(f \circ g)^{-1}(x) = \text{_____}$$

$$(f^{-1} \circ g^{-1})(x) = \text{_____}$$

$$(g^{-1} \circ f^{-1})(x) = \text{_____}$$

Answer(s) submitted:

-
-
-
-

(incorrect)

4. (5 points) Consider the function

$$f(x) = \frac{x}{8x - 1}.$$

a) Find the inverse function for f

$$f^{-1}(x) = \text{_____},$$

(b) The domain of f is $x \mid x \neq \text{_____}$

(c) The domain of f^{-1} is $x \mid x \neq \text{_____}$

(d) The range of f is $y \mid y \neq \text{_____}$

(d) The range of f^{-1} is $y \mid y \neq \text{_____}$

Answer(s) submitted:

-
-
-
-
-

(incorrect)

5. (1 point) Let

$$f(x) = \frac{x + 4}{x + 7}$$

$$f^{-1}(-3) = \text{_____}$$

Answer(s) submitted:

-

(incorrect)

6. (5 points) Enter T or F depending on whether the function is one-to-one or not. (You must enter T or F – True and False will not work.)

___1. $c(x) = \frac{x - 3}{2 + x}$

___2. $b(x) = 3x^3 - 3x$

___3. $a(x) = 3x^4 - 2x$

___4. $e(x) = 3\sqrt{x + 2}$

___5. $d(x) = (3x - 3)^2 + 3$

Answer(s) submitted:

-
-
-
-
-

(incorrect)

7. (1 point) Let $f(x) = x^3 + 4x + 4$. Find x if $f^{-1}(x) = 0$.
 $x = \underline{\hspace{2cm}}$

Answer(s) submitted:

•

(incorrect)

8. (1 point)

Find the inverse function of $g(x) = \frac{\sqrt{x}+4}{7-\sqrt{x}}$. If the function is not invertible, enter **NONE**.

$g^{-1}(x) = \underline{\hspace{2cm}}$

(Write your inverse function in terms of the independent variable x .)

Answer(s) submitted:

•

(incorrect)

9. (4 points)

Consider the functions $f(x) = \sqrt[3]{\frac{x}{5}} + 9$, $g(x) = \sqrt[3]{\frac{x-9}{5}}$, $h(x) = 9 + 5x^3$, $p(x) = -9 + 5x^3$, $q(x) = \sqrt[3]{\frac{x}{5}} - 9$, and $r(x) = \sqrt[3]{\frac{x+9}{5}}$.

Which of these functions are inverses of each other?

- A. $g(x)$ and $h(x)$
- B. $h(x)$ and $q(x)$
- C. $f(x)$ and $p(x)$
- D. $p(x)$ and $q(x)$
- E. $f(x)$ and $h(x)$
- F. $g(x)$ and $p(x)$
- G. $h(x)$ and $r(x)$
- H. $p(x)$ and $r(x)$
- I. No pairs of these functions are inverses of each other.

Answer(s) submitted:

•

(incorrect)

10. (1 point)

Consider the functions $f(x) = e^{7x}$, $g(x) = \ln(x) - 7$, $h(x) = 7\ln(x)$, $p(x) = \ln\left(\frac{x}{7}\right)$, $q(x) = \ln(x) + 7$, $r(x) = \ln(7x)$, and $s(x) = \frac{\ln(x)}{7}$.

Which of the following functions is an inverse function of $f(x)$?

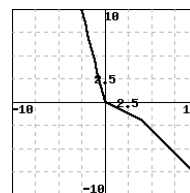
- A. $g(x)$
- B. $h(x)$
- C. $p(x)$
- D. $q(x)$
- E. $r(x)$
- F. $s(x)$
- G. None of these functions is an inverse function of $f(x)$.

Answer(s) submitted:

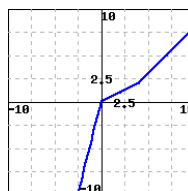
•

(incorrect)

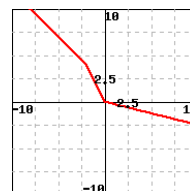
11. (1 point) Find the graph of the inverse of the function f graphed below.



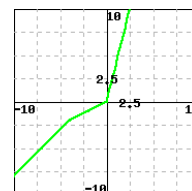
The graph of f



Graph A



Graph B



Graph C

The inverse of the function f is graphed in Graph (A, B or C):

Answer(s) submitted:

•

(incorrect)

12. (1 point)

If you are given the graph of f , how do you find the graph of f^{-1} ?

- (a) Reflect it over the x -axis.
- (b) Reflect it over the y -axis.
- (c) Reflect it over $y = x$.
- (d) Reflect it over $y = -x$.

Answer(s) submitted:

•

(incorrect)

13. (1 point) Find the inverse function of $f(x) = 3\log_2(6x - 4) + 9$.

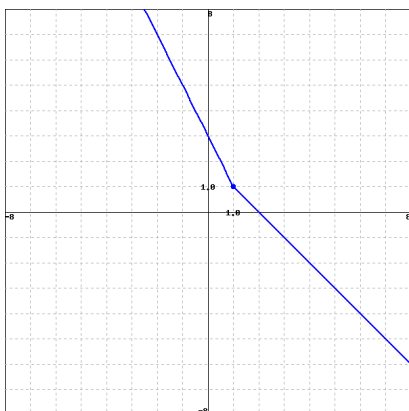
$f^{-1}(x) = \underline{\hspace{2cm}}$

Answer(s) submitted:

•

(incorrect)

14. (5 points) Use the given graph of the function f to find the following values for f^{-1} .



1. $f^{-1}(-4) = \underline{\hspace{2cm}}$
2. $f^{-1}(-3) = \underline{\hspace{2cm}}$
3. $f^{-1}(0) = \underline{\hspace{2cm}}$
4. $f^{-1}(2) = \underline{\hspace{2cm}}$
5. $f^{-1}(4) = \underline{\hspace{2cm}}$

Note: You can click on the graph to enlarge the image.

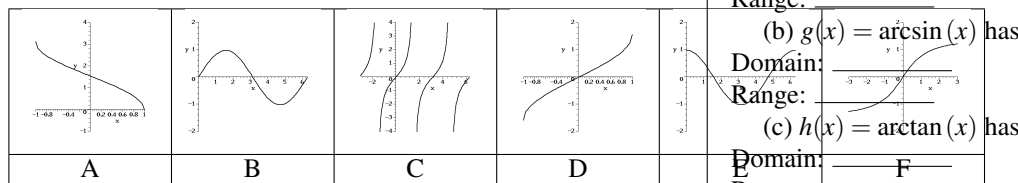
Answer(s) submitted:

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•

(incorrect)

15. (6 points) Match the functions with their graphs.

- ___1. $f(x) = \cos(x)$
- ___2. $f(x) = \sin(x)$
- ___3. $f(x) = \tan(x)$
- ___4. $f(x) = \arcsin(x)$
- ___5. $f(x) = \arccos(x)$
- ___6. $f(x) = \arctan(x)$



(Click on image for a larger view . The small images may not show up properly on a hard copy, but they will be fine in a browser.)

Answer(s) submitted:

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•

•
•
•

(incorrect)

16. (4 points) Evaluate the following expressions. Your answer must be an angle $-\pi/2 \leq \theta \leq \pi$ in radians, written as a multiple of π . Note that π is already provided in the answer so you simply have to fill in the appropriate multiple. E.g. if the answer is $\pi/2$ you should enter 1/2. Do not use decimal answers. Write the answer as a fraction or integer.

$\sin^{-1}(\sin(5\pi/3)) = \underline{\hspace{2cm}} \pi$
 $\sin^{-1}(\sin(3\pi/4)) = \underline{\hspace{2cm}} \pi$
 $\cos^{-1}(\cos(-5\pi/6)) = \underline{\hspace{2cm}} \pi$
 $\cos^{-1}(\cos(3\pi/4)) = \underline{\hspace{2cm}} \pi$

Answer(s) submitted:

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•
•
•

(incorrect)

17. (3 points) Find the inverse of the following function and state its domain.

$f(x) = 6\cos(12x) + 4$

Type 'arccos' for the inverse cosine function in your answer.

$f^{-1}(x) = \underline{\hspace{2cm}}$

Domain= [,]

Answer(s) submitted:

•
•
•

(incorrect)

18. (6 points)

State the domain and range of each of the following functions:

(Enter your answers as inequalities: help (inequalities). Your domains should be inequalities in x and ranges, in y . As always, type π for π . If you wish to enter ∞ , type *infinity* .)

(a) $f(x) = \arccos(x)$ has

Domain:

Range:

(b) $g(x) = \arcsin(x)$ has

Domain:

Range:

(c) $h(x) = \arctan(x)$ has

Domain:

Range:

Answer(s) submitted:

•
•
•
•
•
•

(incorrect)

19. (1 point) Find the exact value.

$$\sin\left(2\cos^{-1}\left(\frac{9}{41}\right)\right) = \underline{\hspace{2cm}}$$

Answer(s) submitted:

•

(incorrect)

20. (4 points)

Find the domain and the range of $g(x) = \sin^{-1}(3x + 1)$.

Domain: $\underline{\hspace{1cm}} \leq x \leq \underline{\hspace{1cm}}$

Range: $\underline{\hspace{1cm}} \leq y \leq \underline{\hspace{1cm}}$

Answer(s) submitted:

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•

•

(incorrect)

21. (2 points)

Find the exact value of each expression:

(a) $\sec(\arctan(2))$

(b) $\cos(2\sin^{-1}(\frac{5}{13}))$

(a) $\underline{\hspace{2cm}}$

(b) $\underline{\hspace{2cm}}$

Answer(s) submitted:

•

•

(incorrect)

22. (2 points) Complete the identity using the triangle method

(a) $\cos(\tan^{-1}(x)) = \underline{\hspace{2cm}}$

(b) $\sin(\sec^{-1}(x)) = \underline{\hspace{2cm}}$

Answer(s) submitted:

•

•

(incorrect)

23. (1 point) Evaluate the limit

$$\lim_{x \rightarrow 16} \frac{16 - x}{4 - \sqrt{x}} = \underline{\hspace{2cm}}.$$

Answer(s) submitted:

•

(incorrect)

24. (6 points) Let

$$f(x) = \frac{5x - 15}{x^4 - 12x^3 + 36x^2}.$$

Find each point of discontinuity of f , and for each give the value of the point of discontinuity and evaluate the indicated one-sided limits.

If needed, use 'INF' for ∞ and '-INF' for $-\infty$.

If you have more than one point, give them in numerical order,

from smallest to largest.

If you have extra boxes, fill each in with an 'x'.

Point 1: $C = \underline{\hspace{2cm}}$

$$\lim_{x \rightarrow C^-} f(x) = \underline{\hspace{2cm}}$$

$$\lim_{x \rightarrow C^+} f(x) = \underline{\hspace{2cm}}$$

Point 2: $C = \underline{\hspace{2cm}}$

$$\lim_{x \rightarrow C^-} f(x) = \underline{\hspace{2cm}}$$

$$\lim_{x \rightarrow C^+} f(x) = \underline{\hspace{2cm}}$$

Point 3: $C = \underline{\hspace{2cm}}$

$$\lim_{x \rightarrow C^-} f(x) = \underline{\hspace{2cm}}$$

$$\lim_{x \rightarrow C^+} f(x) = \underline{\hspace{2cm}}$$

Answer(s) submitted:

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•

(incorrect)

25. (3 points)

$$\text{Let } f(x) = \begin{cases} \sqrt{-3-x} + 5, & \text{if } x < -4 \\ 5, & \text{if } x = -4 \\ 2x + 14, & \text{if } x > -4 \end{cases}$$

Calculate the following limits. Enter **DNE** if the limit does not exist.

$$\lim_{x \rightarrow -4^-} f(x) = \underline{\hspace{2cm}}$$

$$\lim_{x \rightarrow -4^+} f(x) = \underline{\hspace{2cm}}$$

$$\lim_{x \rightarrow -4} f(x) = \underline{\hspace{2cm}}$$

Answer(s) submitted:

• 6

• 6

• 6

(correct)

26. (1 point) Let $f(x) = \sqrt{x} - 7$.

Then $\lim_{h \rightarrow 0} \frac{f(1+h) - f(1)}{h} = \underline{\hspace{2cm}}$

If the limit does not exist enter DNE.

Answer(s) submitted:

- 1/2

(correct)

27. (4 points) Evaluate the limits.

$$f(x) = \begin{cases} \frac{|2x|}{x} & x \neq 0 \\ 0 & x = 0 \end{cases}$$

Enter **DNE** if the limit does not exist.

a) $\lim_{x \rightarrow 0^-} f(x) = \underline{\hspace{2cm}}$

b) $\lim_{x \rightarrow 0^+} f(x) = \underline{\hspace{2cm}}$

c) $\lim_{x \rightarrow 0} f(x) = \underline{\hspace{2cm}}$

d) $f(0) = \underline{\hspace{2cm}}$

Answer(s) submitted:

- -2
- 2
- DNE
- 0

(correct)

28. (1 point) Use the Squeeze Theorem to evaluate the limit $\lim_{x \rightarrow 2} f(x)$, if

$$4x - 4 \leq f(x) \leq x^2 \quad \text{on } [0, 4].$$

Enter **DNE** if the limit does not exist.

Limit = $\underline{\hspace{2cm}}$

Answer(s) submitted:

- 2

(incorrect)

29. (1 point) Use the Squeeze Theorem to evaluate the limit

$$\lim_{x \rightarrow 0} \sin x \cos \left(\frac{1}{x^5} \right)$$

Enter **DNE** if the limit does not exist.

Limit = $\underline{\hspace{2cm}}$

Answer(s) submitted:

-

(incorrect)

30. (3 points) Evaluate the limits. If a limit does not exist, enter **DNE**.

$\lim_{x \rightarrow -6^+} \frac{|x+6|}{x+6} = \underline{\hspace{2cm}}$

$\lim_{x \rightarrow -6^-} \frac{|x+6|}{x+6} = \underline{\hspace{2cm}}$

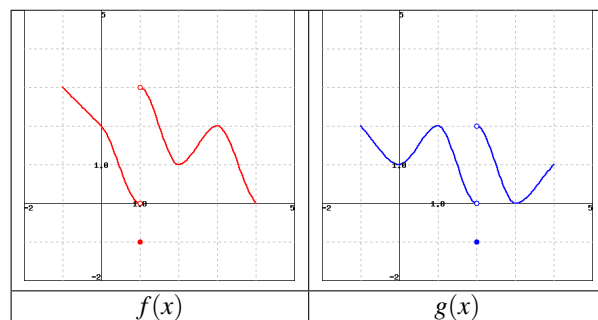
$\lim_{x \rightarrow -6} \frac{|x+6|}{x+6} = \underline{\hspace{2cm}}$

Answer(s) submitted:

-
-
-

(incorrect)

31. (24 points)



The graphs of $f(x)$ and $g(x)$ are given above. Use them to evaluate each quantity below. Write **DNE** if the limit or value does not exist (or if it's infinity).

___1. $\lim_{x \rightarrow 1^+} [f(x)g(x)]$

___2. $f(g(1))$

___3. $f(2)/g(2)$

___4. $\lim_{x \rightarrow 2^+} [f(x) + g(x)]$

___5. $\lim_{x \rightarrow 1^+} [f(g(x))]$

___6. $\lim_{x \rightarrow 2^+} [f(g(x))]$

___7. $\lim_{x \rightarrow 2^+} [f(x)/g(x)]$

___8. $\lim_{x \rightarrow 1^-} [f(x) + g(x)]$

___9. $\lim_{x \rightarrow 2^-} [f(g(x))]$

___10. $f(g(2))$

___11. $\lim_{x \rightarrow 1^+} [f(x) + g(x)]$

___12. $\lim_{x \rightarrow 2^-} [f(x)/g(x)]$

___13. $f(1) + g(1)$

___14. $\lim_{x \rightarrow 2^-} [f(x)g(x)]$

___15. $f(1)/g(1)$

___16. $f(2)g(2)$

___17. $\lim_{x \rightarrow 1^-} [f(x)g(x)]$

___18. $\lim_{x \rightarrow 1^-} [f(x)/g(x)]$

___19. $\lim_{x \rightarrow 2^-} [f(x) + g(x)]$

- ____20. $f(2) + g(2)$
 ____21. $\lim_{x \rightarrow 1^+} [f(x)/g(x)]$
 ____22. $f(1)g(1)$
 ____23. $\lim_{x \rightarrow 2^+} [f(x)g(x)]$
 ____24. $\lim_{x \rightarrow 1^-} [f(g(x))]$

Answer(s) submitted:

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(incorrect)

32. (3 points)

A function is said to have a **vertical asymptote** wherever the limit on the left or right (or both) is either positive or negative infinity.

For example, the function $f(x) = \frac{-3(x+2)}{x^2+4x+4}$ has a vertical asymptote at $x = -2$.

Find each of the following limits.

$$\lim_{x \rightarrow -2^-} \frac{-3(x+2)}{x^2+4x+4} = \text{_____} \text{ help (limits)}$$

$$\lim_{x \rightarrow -2^+} \frac{-3(x+2)}{x^2+4x+4} = \text{_____} \text{ help (limits)}$$

$$\lim_{x \rightarrow -2} \frac{-3(x+2)}{x^2+4x+4} = \text{_____} \text{ help (limits)}$$

Answer(s) submitted:

-
-
-

(incorrect)

33. (4 points)

Part 1: Evaluate the limit

Evaluate the following limit by simplifying the expression (first answer box) and then evaluating the limit (second answer box).

$$\lim_{x \rightarrow 9} \frac{x-9}{\sqrt{x}-\sqrt{9}} = \lim_{x \rightarrow 9} \text{_____} = \text{_____}.$$

Hint: Treat $x-9$ as a difference of squares. Note: In your written solution, you should write the limit statement $\lim_{x \rightarrow 9}$ in every step except the last one, where the limit is finally evaluated.

Part 2: Follow-up question

Answer(s) submitted:

-
-
-
-

(incorrect)

34. (4 points) Evaluate the following limits:

$$1. \quad \lim_{x \rightarrow 3^-} \frac{2}{x-3} = \text{_____}$$

$$2. \quad \lim_{x \rightarrow 3^+} \frac{2}{x-3} = \text{_____}$$

$$3. \quad \lim_{x \rightarrow 0} \frac{1}{x^2(x+7)} = \text{_____}$$

$$4. \quad \lim_{x \rightarrow 5} \frac{2}{(x-5)^6} = \text{_____}$$

Answer(s) submitted:

-
-
-
-

(incorrect)

35. (5 points)

A function is said to have a **horizontal asymptote** if either the limit at infinity exists or the limit at negative infinity exists.

Show that each of the following functions has a horizontal asymptote by calculating the given limit.

$$\lim_{x \rightarrow \infty} \frac{-3x}{14+2x} = \text{_____}$$

$$\lim_{x \rightarrow -\infty} \frac{7x-4}{x^3+12x-4} = \text{_____}$$

$$\lim_{x \rightarrow \infty} \frac{x^2-4x-14}{10-7x^2} = \text{_____}$$

$$\lim_{x \rightarrow \infty} \frac{\sqrt{x^2+6x}}{10-10x} = \text{_____}$$

$$\lim_{x \rightarrow -\infty} \frac{\sqrt{x^2+6x}}{10-10x} = \text{_____}$$

Answer(s) submitted:

-

-
-
-
-

(incorrect)

36. (2 points) Let

$$f(x) = \frac{x+3}{4x^6}.$$

Find the equations of the horizontal asymptotes and the vertical asymptotes of $f(x)$. If there are no asymptotes of a given type, enter 'NONE'. If there is more than one asymptote of a given type, give a comma separated list (i.e.: 1, 2,...).

Horizontal asymptotes: $y =$ _____ Vertical Asymptotes: $x =$ _____

Answer(s) submitted:

-
-

(incorrect)

37. (1 point) Evaluate the limit

$$\lim_{y \rightarrow 3} \frac{4(y^2 - 1)}{4y^2(y - 1)^3}$$

If the limit does not exist enter DNE.

Limit = _____

Answer(s) submitted:

-

(incorrect)

38. (1 point) Evaluate the limit

$$\lim_{y \rightarrow 1} \frac{y^3 - 1}{y^2 - 1}$$

If the limit does not exist enter DNE.

Limit = _____

Answer(s) submitted:

-

(incorrect)

39. (2 points) Identify the horizontal and vertical asymptotes, if any, of the given function.

$$f(x) = \frac{x^2 - 1}{-x^2 - 1}$$

Separate multiple answers by commas. Enter **DNE** if an asymptote does not exist.

a) Horizontal asymptote(s): $y =$ _____

b) Vertical asymptote(s): $x =$ _____

Answer(s) submitted:

-
-

(incorrect)

40. (2 points)

Evaluate the following limits. If needed, enter INF for ∞ and MINF for $-\infty$.

(a)

$$\lim_{x \rightarrow \infty} (\sqrt{x^2 + 4x + 1} - x) =$$

(b)

$$\lim_{x \rightarrow -\infty} (\sqrt{x^2 + 4x + 1} - x) =$$

Answer(s) submitted:

- 2
- INF

(correct)

41. (1 point) Find the following limit.

Notes: Enter "DNE" if limit Does Not Exist.

$$\lim_{x \rightarrow -\infty} \frac{-6e^{-x} + e^x}{5e^{-x} + 3e^x} =$$

Answer(s) submitted:

- -6/5

(correct)

42. (1 point) Find the following limit.

Notes: Enter "DNE" if limit Does Not Exist.

$$\lim_{x \rightarrow 0^+} \ln\left(\frac{4}{x^6}\right) =$$

Answer(s) submitted:

- Infinity

(correct)

43. (1 point) Find the following limit.

Notes: Enter "DNE" if limit Does Not Exist.

$$\lim_{x \rightarrow \frac{\pi}{2}^-} e^{\tan(x)} =$$

Answer(s) submitted:

- Infinity

(correct)

44. (1 point) For the equation

$$x + \sin(x) = 1$$

does the intermediate value theorem show at least one solution on the interval $[0, \frac{\pi}{6}]$?

- ?
- Yes, it shows there must be at least one solution
- No, it is not conclusive
- No, it show no solutions

Answer(s) submitted:

- Yes, it shows there must be at least one solution

(correct)

45. (1 point) Find a value of the constant k , if possible, at which

$$f(x) = \begin{cases} kx^2 & x \leq -5 \\ 10x + k & x > -5 \end{cases}$$

is continuous everywhere.

$k =$ _____ (enter "none" if no value).

Answer(s) submitted:

- $-25/12$

(correct)

46. (4 points)

Part 1: Evaluate the limit

Part 2: Follow-up question

$$\lim_{x \rightarrow 1} \frac{\sqrt{x} - x^2}{1 - \sqrt{x}} = \lim_{x \rightarrow 1} \frac{\quad}{\quad} = \quad.$$

Answer(s) submitted:

- $x(1+x+x^2)$
- 3
- $(1/(2*\sqrt{x})-2x)/-1/(2*\sqrt{x})$
- 3

(score 0.75)