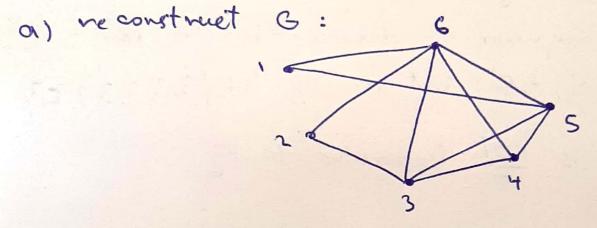
. Consider the following adjacency matrix of graph G:

[000001]

[000001]

[01011]

[001011]



b) is there any path between wodes 122?
Jes, 7-+6-+2

c) find degrees of the nodes in this graph:
d, (2,2,4,3,4,5)

d) find #edges in G from the degrees of the

vertices: [di, 2e

=> e,  $(2+2+4+3+4+5)/2 = \frac{20}{2} = 10$ 

e) is G bipartite? NO, (Hint: Assume it's bipartite. color of G should be dit-ferent from all other vertices. reach contradiction)

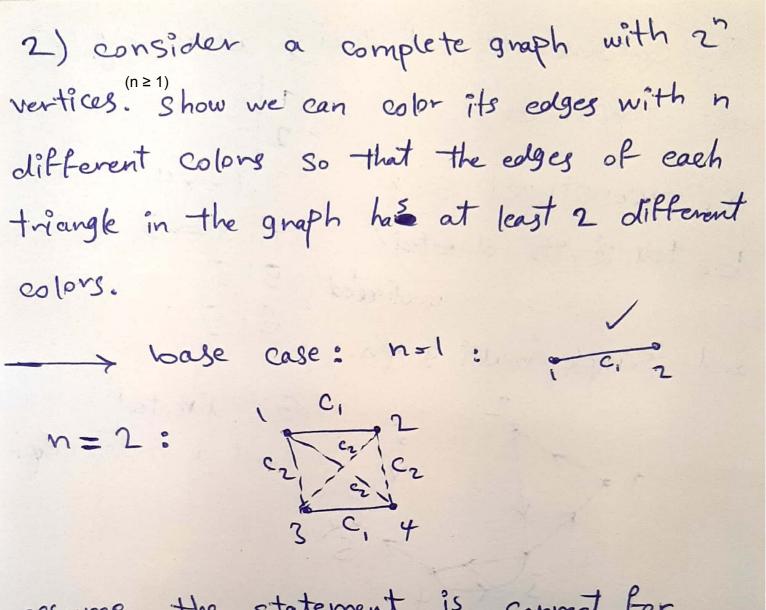
P) is this graph isomorphic to We? - let's consider we : 1EG = 10 1/6 = 6 1 E = 10 1 W = 1 = 6 (in increasing order)

However, Sequence of degrees for G is:

(2, 2, 3, 4, 4, 5) but for Wg is: (3,3,3,3,5) =D G is NOT isomorphic to WG. 9) Does G have an Euler circuit/path? Euler poth: 4-6-3-4-5-3-2-6-1-0-5-6 \* Note that the starting & eding vertices of the path have odd degrees. No Euler circuit, (because there are nodes with odd degree)

h) is G connected? yes

7) consider the following adjacency list 1 2 2 3 1, 4 4 3, 5 of graph G. a. reconstruct 6: b. teu if its directed/ 5 5 6 5 undirected and Simple/multi graph. Gis directed and simple c. Find the strong/weak components:  $c_1: \{1,2,3,4\}$ strong  $c_2: \{5\}$ components  $c_3: \{6\}$ {1,2,3,4,5,63 weak components: d. cheek Euler path / circuit: NO Euler path & No Euler circuit



assume the statement is correct for nsk =12 we can color the edges of a complete graph with 2 vertices with k different colors so that each triangle has at least 2 diff color we want to show for nsk+1

The put 2 complete graphs with 2 nodes next to each other & color the edges of each of them with k colors. color the edges between them with color k+1.