# CS3388B, Winter 2023

# Problem Set 3

Due: January 27, 2023

#### Exercise 1.

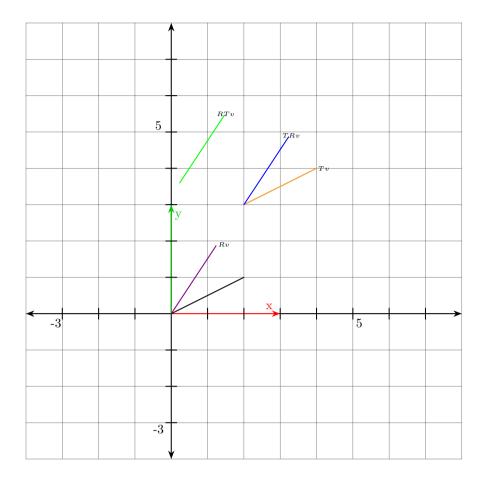
Consider a window with width 1000px and height 800px with a viewport whose opposite corners, in pixels, are (200, 100) and (800, 700).

Give the viewport matrix which transforms normalized device coordinates to this viewport.

**Exercise 2.** Consider the following affine transforms:

$$T = \begin{bmatrix} 1 & 0 & 2 \\ 0 & 1 & 3 \\ 0 & 0 & 1 \end{bmatrix} \qquad R = \begin{bmatrix} \cos(30) & -\sin(30) & 0 \\ \sin(30) & \cos(30) & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

Let  $M_1 = TR$  and  $M_2 = RT$  be two transformation matrices. Consider the line segment defined by  $v_1 = (0,0)$  and  $v_2 = (2,1)$ . Draw the line segment when transformed by  $M_1$  and when transformed by  $M_2$ . Describe, in words, what is the difference between the affine transforms  $M_1$  and  $M_2$ ? Why is the result different?



## Exercise 3.

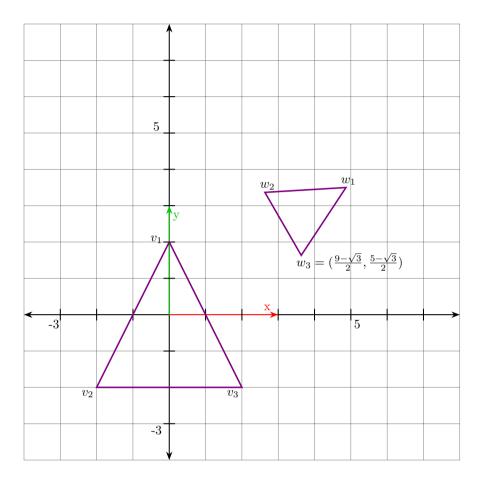
Consider the shear matrix

$$S = \begin{bmatrix} 1 & m \\ 0 & 1 \end{bmatrix}.$$
 
$$\begin{bmatrix} 0 & 1 & 0 \\ 0 & 0 & 0 \end{bmatrix}$$
 Find the inverse of  $S$  in homogeneous coordinates and show that  $\underline{SS^{-1} = I_3}$ , the 3x3 identity matrix.

## Exercise 4.

The below triangle  $(v_1, v_2, v_3)$  has been affinely transformed to  $(w_1, w_2, w_3)$  by a combination of a scaling, a trans-

lation, and a rotation. Let those individual transformations be described by the matrices *S*, *T*, *R*, respectively.



Using homogeneous coordinates, find the matrices S, T, R. Then find (through matrix-matrix and matrix-vector multiplication) the coordinates of  $w_1$  and  $w_2$ . What is the correct order of matrix multiplications to get the correct result?

TSRv is one correct order (of many). T, S, R :=

[1	0	4]	
[ [0	1	] 3]	
[ [0	0	] 1]	
[0.5		0	0]
[ [ 0	0.5		0]
[ [ 0		0	] 1]

[	1/2	]	
[	3	]	
[ 1/2		0]	
[	2	]	
[		]	
[ 1/2		]	
[ 3		]	
[	1/2	0]	
[ 2		]	
[		]	
[ 0	0	1]	