## WESTERN UNIVERSITY Department of Applied Mathematics

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## Calculus 2402A ASSIGNMENT 3B

Release: Wednesday September 30, 2020 Due: Thursday October 8, 2020 at 11:59 PM

Show all your work, unjustified answers will receive little or no credit.

1. [5 marks] Given  $f(x, y, z) = 4xyz - x^4 - y^4 - z^4$ , find the critical points and classify them.

$$7x = 4yz - 4x^3 = 0$$
 $7y = 4xz - 4y^2 = 0$ 
 $7z = 4yx - 4z^2 = 0$ 

the critical points are co, 0,0) and l1,1,1).

: (0,0,0) needs further dismission,

(1,1,1) is regative deitined and the maximum volue 25 1

2. [5 marks] Given  $f(x, y, z) = xy + x^2z - x^2 - y - z^2$ , find the critical points and classify them.

$$7x^{2}y^{2}+2x^{2}-2x^{2}0$$
 $7y^{2}-x^{2}-1$ 
 $7y^{2}-x^{2}-2y^{2}=0$ 
 $7x^{2}-2y^{2}-2y^{2}=0$ 
 $7x^{2}-2y^{2}-2y^{2}=0$ 

the only critical point is (1,1, 2).

$$\begin{aligned}
\frac{1}{3}xx &= 2 \cdot 2 \cdot 2 & \frac{1}{3}xy &= 1 & \frac{1}{3}xz &= 2 \cdot x \cdot \\
\frac{1}{3}yx &= 1 & \frac{1}{3}yy &= 0 & \frac{1}{3}yz &= 0 \\
\frac{1}{3}zx &= 2 \cdot x & \frac{1}{3}zy &= 0 & \frac{1}{3}zz &= 2 \cdot x \cdot \end{aligned}$$

2. (1,1, 2) is negative deifined and the maximum value is - 34

3. [5 marks] Find the third degree Taylor polynomial of  $f(x,y) = \frac{1}{2+x-2y}$  near the point (2,1).

a=2 b=1 h=x k=y.

7(2,7)=(2+2-27)

=
$$\frac{1}{3!}\left[(x-2)\frac{1}{3}x(2,1)+(y-1)\frac{1}{3}y(2,1)\right]^{\frac{1}{2!}\left[(x-2)\frac{1}{3}x(2,1)+(y-1)\frac{1}{3}y(2,1)\right]^{2}}$$

$$7x^{2} - (2tx - 2y)^{-2}$$
 $7xx^{2} - 6(2tx - 2y)^{-3}$ 
 $-\frac{1}{4}$ 
 $= -\frac{3}{8}$ 

$$\frac{1}{2}$$
 = 2 (2+x-2y)<sup>-2</sup>.  $\frac{1}{2}$  =  $\frac{1}{2}$  =

4. [5 marks] Find the third degree Taylor polynomial of  $f(x,y) = \ln(x^2 + y^2)$  near the point (1,0).

$$\frac{1}{1+x^2+y^2} = \frac{2x}{(x^2+y^2)^2} = \frac{2(x^2+y^2)^2}{(x^2+y^2)^2} = \frac{2x^2}{(x^2+y^2)^2} = \frac{8xy^2}{(x^2+y^2)^2}$$

$$\frac{1}{3} = \frac{2y}{x^2 + y^2} = \frac{2x^2}{(x^2 + y^2)^2} = \frac{2x^2}{(x^2 + y^2)^2}$$

$$= 0$$

$$= 2$$

$$f_{(x,y)} = 0 + 2(x-1) + \frac{1}{2} \cdot 2y$$
  
= 2x+y-2.