

Oct 18

COMPSCI 3331

Fall 2022

What's next?

- ▶ Assignment 1: solutions available tomorrow. Marks available before A2 deadline.
- ▶ Assignment 2: due Oct 26.
- ▶ Quiz 2 marks available now.
- ▶ Quiz 4: up to end of Lecture 8.
- ▶ Midterm: October 25. Includes **at least** all of Lecture 8.

Assignment

A2 Q2

should not show a particular example.

- ▶ What does $p_a(L)$ do? *show closure property*
- ▶ What do we do for this question?

A2 Q3b

- ▶ Instead of using pumping lemma, use other facts you know.
- ▶ In particular, can use part (a).

$$p_a(L) = \{ w \in \Sigma^* \mid \exists n \geq 0, w a^n G L \}.$$

Showing languages aren't regular

- ▶ $L_5 = \{w \in \{a,b,c,d\}^* : \forall x \in \{a,b,c,d\}, |w|_x = 0 \text{ or } |w|_x \geq 5\}$ 5⁴ states. $(a=0111w_a \geq 5) + (b=0111w_b \geq 5) + \dots$ calculable.
- ▶ $L_6 = L^*$ where $L = \{a^n b^n : n \geq 0\}$ L is not regular. $\Rightarrow L^*$ is not reg.
- ▶ $L_7 = \{w \in \{a,b\}^* : |w|_a \equiv |w|_b \pmod{10}\}$
- ▶ $L_8 = \{w \in \{a,b\}^* : \exists u \in \{a,b\}^*, w = uu^R\}$ \leftarrow inf ormal.
↑
requires too much memory.

L_6 : pumping lemma: $a^n b^n$.

CFGs

Grammar 1

$$V = \{S\}$$

$$\Sigma = \{a, b, \# \}$$

S is the start symbol

$$S \rightarrow aSb$$

$$S \rightarrow aSbb$$

$$S \rightarrow \#$$

rules
that apply

update this
statement with
S :self until
S is replaced.

S could be replaced
with any other symbol.

same
state

Grammar 2

$$V = \{S\}$$

$$\Sigma = \{a, b\}$$

S is the start symbol

$$S \rightarrow aSa$$

$$S \rightarrow bSb$$

$$S \rightarrow SS$$

$$S \rightarrow \varepsilon$$

How do we prove that $L = L(G)$?

$$\{a^i \# b^j : 0 \leq i \leq j \leq 2i\}.$$

$$S \rightarrow aSb$$

$$S \rightarrow aSbb$$

$$S \rightarrow \#$$

- 1) $L \subseteq L(G)$
prove by showing the derivation.
 $S \Rightarrow$ steps of rules showing
- 2) $L(G) \subseteq L$: induction.

Writing Grammars *kelvin*

- ▶ Nested dependencies are ok. $L = \{a^n b^m c^m d^n : n, m \geq 0\}$.
- ▶ “Serial dependencies are not. $L = \{a^n b^m c^n d^m : n, m \geq 0\}$.

S

$\{a, b, c, d\}$

$S \rightarrow asd$

$S \rightarrow T$ *↳ this step*

$T \rightarrow bTc$ *is essential!*

$T \rightarrow \epsilon$

More examples

- ▶ $L_1 = \{a^i b^j c^i : i, j \geq 0\}$
- ▶ $L_2 = \{a^n b^m : n > m\}$
- ▶ $L_3 = \{a^n b^m : n \neq m\}$
- ▶ $L_4 = L_1^*$
- ▶ $L_5 = \{a^i b^j c^k : i = j \text{ or } j = k\}$

$$\begin{cases} S \rightarrow aSc \\ S \rightarrow T \\ T \rightarrow bT \\ T \rightarrow \epsilon \end{cases}$$

$$L_2 + \{a^n b^m : n < m\} \Rightarrow$$

$$\begin{cases} S_1 \rightarrow aS_1 \\ S_1 \rightarrow aT_1 \\ T_1 \rightarrow aT_1b \\ T_1 \rightarrow \epsilon \\ S_2 \rightarrow S_2b \Rightarrow \\ S_2 \rightarrow T_2b \\ T_2 \rightarrow aT_2b \\ T_2 \rightarrow \epsilon \end{cases}$$

$$\begin{cases} S \rightarrow S_1 \\ S \rightarrow S_2 \\ S_1 \rightarrow aT \\ S_2 \rightarrow Tb \\ S_1 \rightarrow aS_1 \\ S_2 \rightarrow S_2b \\ T \rightarrow aTb \\ T \rightarrow \epsilon \end{cases}$$

$$\begin{aligned} S &\rightarrow aT \\ T &\rightarrow aTb \\ T &\rightarrow \epsilon \\ S &\rightarrow aS \end{aligned}$$

$$\begin{aligned} X &= L_1 \\ X &\rightarrow \epsilon \\ X &\rightarrow XX \end{aligned}$$

Midterm prep.

- ▶ Your group is now available.
- ▶ To find it go to Dropbox (left hand side) and open the file in your dropbox.
- ▶ On the website there's an image of the lecture theatre.
- ▶ Shows your suggested meeting point for your group.

Midterm Format

- ▶ You must write both parts of the midterm.
- ▶ Individual Portion: 90 % of your grade.
- ▶ Group Portion: 10 % of your grade.
- ▶ But your mark will never go down because of the group portion (if you write it). ($\max(.9S_1 + .1S_2, S_1)$)
- ▶ Time: 80 minutes for individual stage, 5 minutes to find groups, 20 minutes for group stage.