

H4Q1:

Proof: Suppose  $a \in B \setminus C$ , then  $a \in B$  and  $a \notin C$ . Since  $a \in B$ ,  $a \in A \cup B$ . Since  $a \notin C$ ,  $a \notin C \cap D$ . Thus,  $a \in B \setminus C$  implies  $a \in (A \cup B) \setminus (C \cap D)$   $\square$

H4Q2:

It is false.

Proof: To get a counterexample, we could let  $n=7$ , which is a prime number, so  $n^2+n+7=(7+1+1) \times 7=9 \times 7$ , which is not a prime number. Thus, the argument is false.  $\square$

H4Q3:

Proof: To prove that if  $x \neq 1$ , then  $y \neq 2$ . We could assume that  $y=2$ . then the equation would be  $4x=2x+2$ . and  $x=1$ . So if  $y=2$  then  $x=1$ , which is the contrapositive of "if  $x \neq 1$ , then  $y \neq 2$ ". Thus,  $xy^2=2x+y$  implies that if  $x \neq 1$ , then  $y \neq 2$ .  $\square$