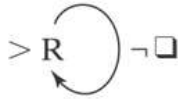
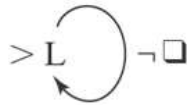


## Useful machines



Find the first blank square to the right of the current square.

$R_q$



Find the first blank square to the left of the current square.

$L_q$



Find the first nonblank square to the right of the current square.

$R_{-q}$



Find the first nonblank square to the left of the current square

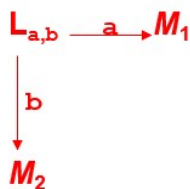
$L_{-q}$

$L_a$

Find the first occurrence of  $a$  to the left of the current square.

$R_{a,b}$

Find the first occurrence of  $a$  or  $b$  to the right of the current square.



Find the first occurrence of  $a$  or  $b$  to the left of the current square, then go to  $M_1$  if the detected character is  $a$ ; go to  $M_2$  if the detected character is  $b$ .

$L_{x \leftarrow a,b}$

Find the first occurrence of  $a$  or  $b$  to the left of the current square and set  $x$  to the value found.

$L_{x \leftarrow a,b} R_x$

Find the first occurrence of  $a$  or  $b$  to the left of the current square, set  $x$  to the value found, move one square to the right, and write  $x$  ( $a$  or  $b$ ).

# Turing Machines as Language Recognizers

$M$  **decides** a language  $L \subseteq \Sigma^*$  iff:

For any string  $w \in \Sigma^*$  it is true that:

if  $w \in L$  then  $M$  **accepts**  $w$ , and

if  $w \notin L$  then  $M$  **rejects**  $w$ .

A language  $L$  is **decidable** iff there is a Turing machine  $M$  that decides it. In this case, we will say that  $L$  is in **D**.