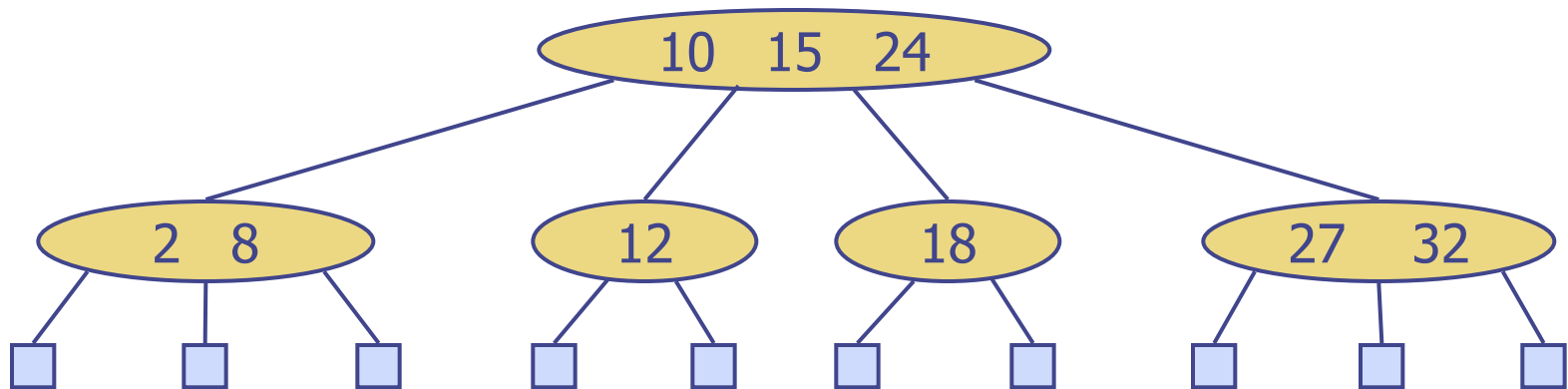


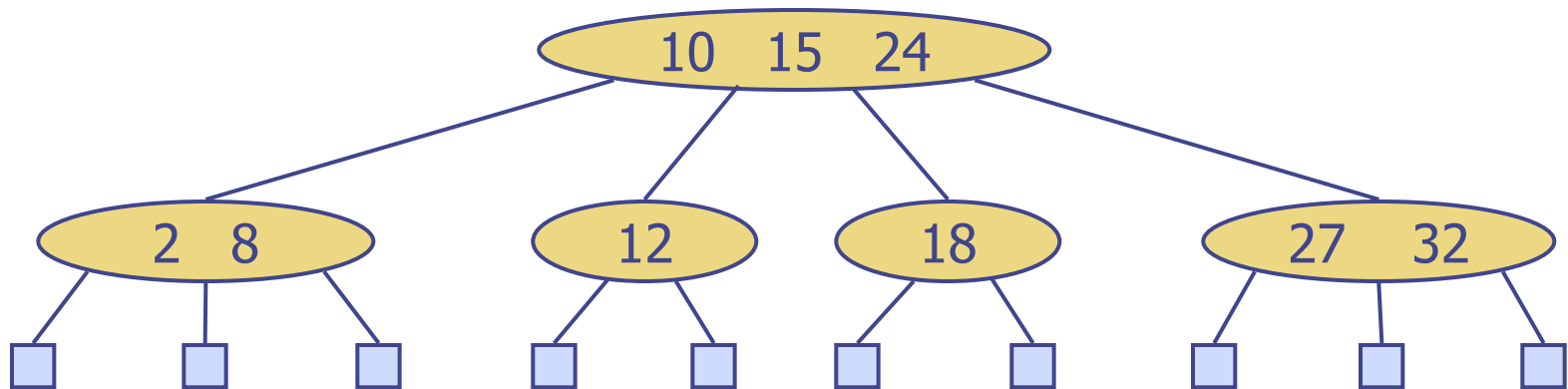
(2,4) Trees

- ◆ A (2,4) tree (also called 2-4 tree or 2-3-4 tree) is a multi-way search tree with the following properties



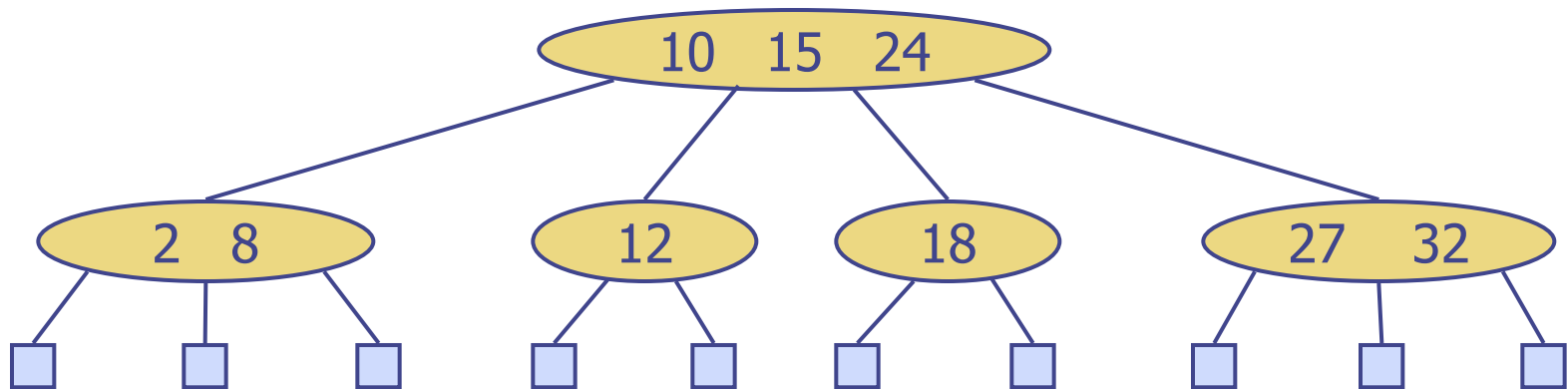
(2,4) Trees

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 - **Node-Size Property:** every internal node has 2, 3, or 4 children

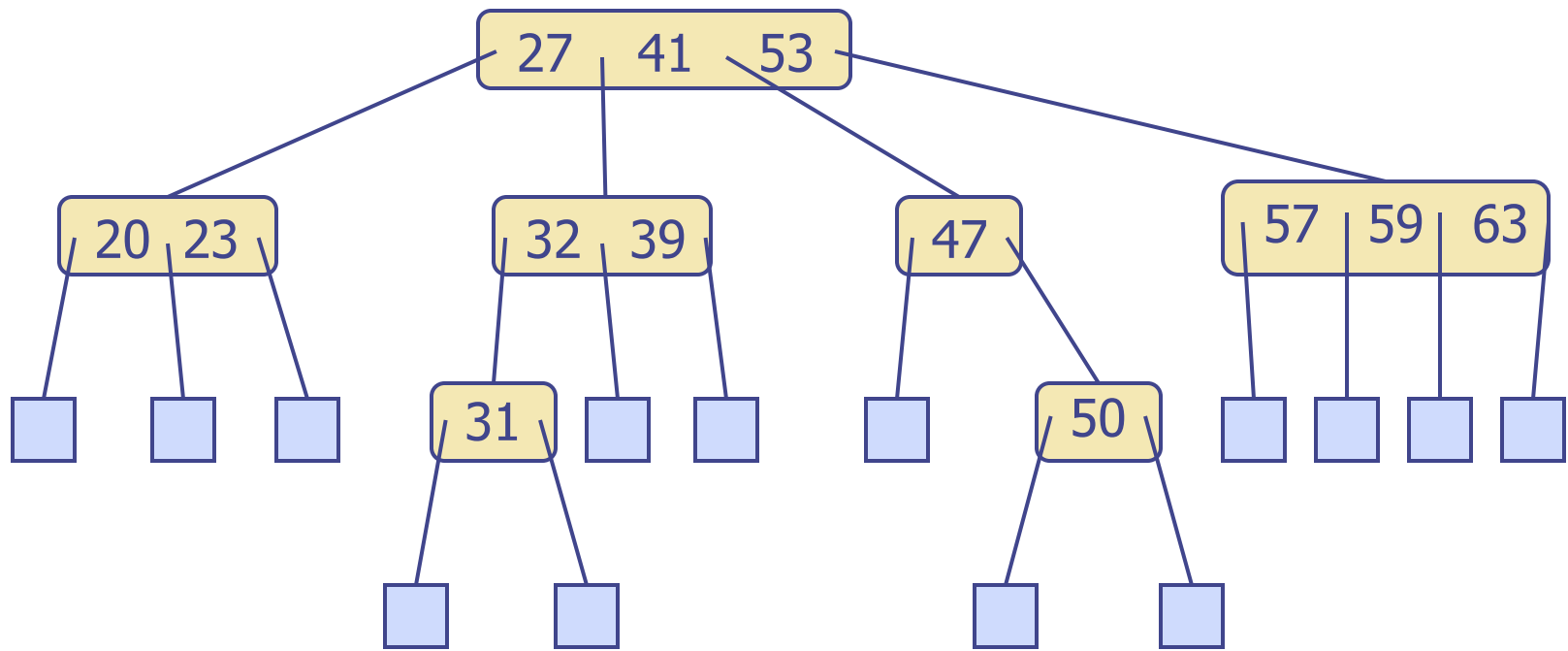


(2,4) Trees

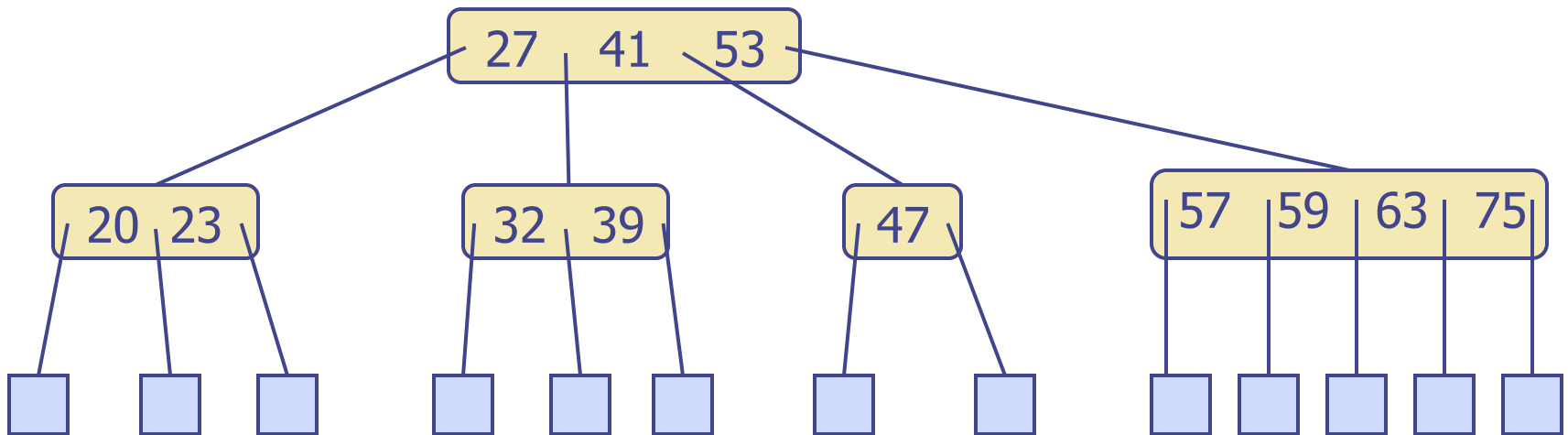
- ◆ A (2,4) tree (also called 2-4 tree or 2-3-4 tree) is a multi-way search tree with the following properties
 - **Node-Size Property**: every internal node has 2, 3, or 4 children
 - **Depth Property**: all the leaves are in the same level



(2,4) Tree?



(2,4) Tree?



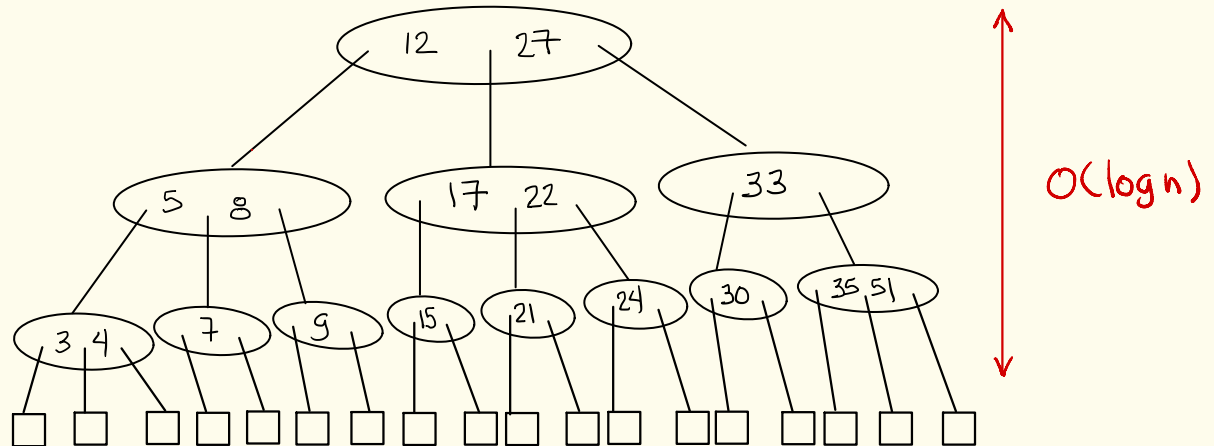
What is the Maximum Height of a (2,4) Tree?

What is the Maximum Height of a (2,4) Tree?

Build the tallest possible (2,4) tree with n keys : k_1, k_2, \dots, k_n

1

Implementing an Ordered Dictionary with a (2,4) tree



$get(k)$

$smallest()$

$largest()$

$successor(k)$

$predecessor(k)$

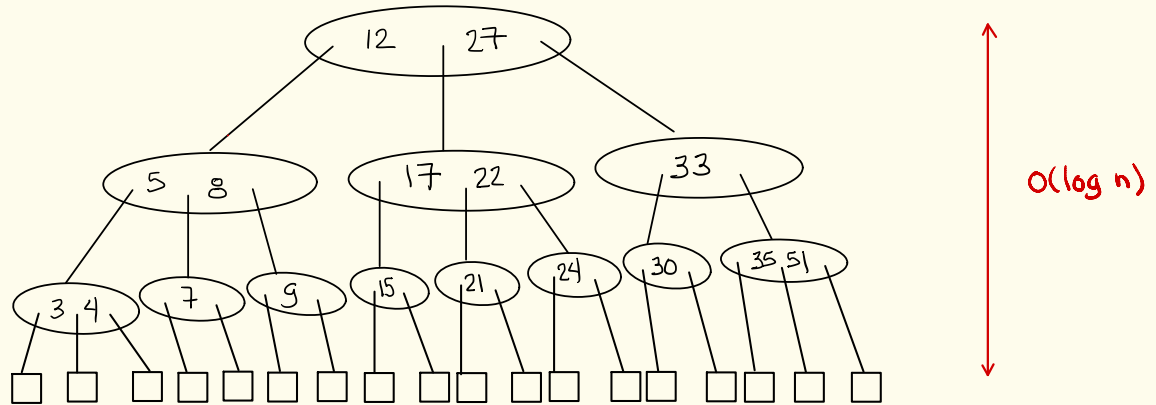
$put(k, d)$

$remove(k)$

Ordered Dictionary Operations on a Multiway Search Tree of Degree d

smallest	$O(\text{height})$
largest	$O(\text{height})$
get	$O(\text{height} \times \log d)$
successor	$O(\text{height} \times \log d)$
predecessor	$O(\text{height} \times \log d)$
put	$O(d + \text{height} \times \log d)$
remove	$O(d + \text{height} \times \log d)$

Implementing an Ordered Dictionary with a (2,4) tree



$\left. \begin{array}{l} \text{get}(k) \\ \text{smallest}() \\ \text{largest}() \\ \text{successor}(k) \\ \text{predecessor}(k) \end{array} \right\} O(\log n)$

$\text{put}(k, d)$
 $\text{remove}(k)$

insert 12

