

$\frac{\infty}{\infty}, \frac{0}{0} \leftarrow$ 洛! 都TM给我洛!

$$x \rightarrow \infty. \quad \frac{\ln x}{\sqrt{x}} \quad f'(x) = \frac{\frac{1}{x} \cdot \sqrt{x} - \frac{1}{2\sqrt{x}} \ln x}{x}$$

$$= \frac{\frac{1}{\sqrt{x}} (1 - \frac{1}{2} \ln x)}{x^{\frac{3}{2}}}$$

$$f''(x) = \frac{-\frac{1}{2} \frac{1}{x} \rightarrow 0}{\frac{3}{2} x^{\frac{5}{2}} \rightarrow \infty} \Rightarrow 0.$$

$x \rightarrow \infty.$

1. definitions.
2. Fundamental formula of calculus
3. computations.
4. applications.

3.9. Anti-derivatives.

Def: A function $F(x)$ is called an anti-derivative of $f(x)$ if $F'(x) = f(x)$.

e.g. ~~for~~ $f(x) = \sin x$ $F(x) = \cos x$.

~~cos x~~ $\sin x$ is the anti-derivative of $\cos x$.

if $F(x)$ is an anti-derivative of $f(x)$, then $F(x) = \int f(x) dx$.

How to find an anti-derivative?

1- Guess

$$F(x) \xrightarrow{F'(x)} f(x)$$

$$\int f(x) dx.$$

$$F(x) \quad \bigg| \quad f(x).$$

1	$x + C$
$\cos x$	$\sin x + C$
$f(x)$	$f(x) + C$

$$4\sin x + \cancel{2x^5 - \sqrt{x}}$$

$$4\sin x + \cancel{4\cos x} + 2x^4 - \frac{1}{\sqrt{x}} \quad x^{-\frac{1}{2}}$$

$$\underline{-4\cos x + \frac{2}{5}x^5 - 2\sqrt{x}}$$