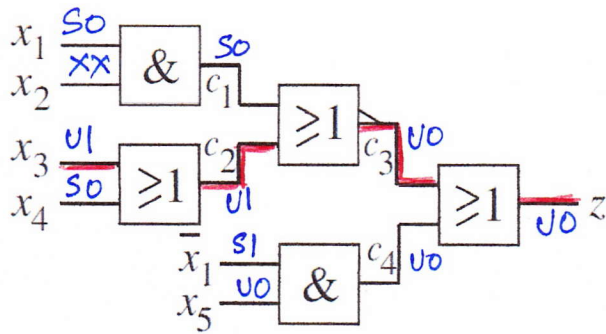


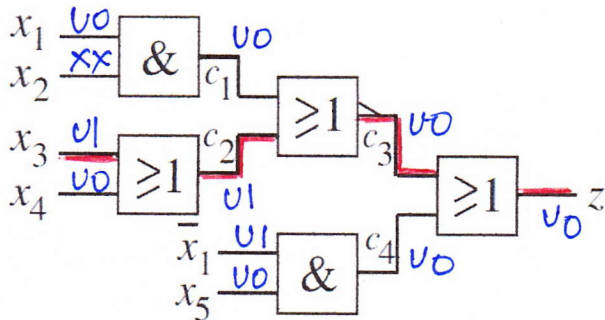
### 3.(i) Robust Pattern



$\uparrow x_3 c_2 c_3 z$

$\therefore$  Test pattern sequence :  
(0x00x, 0x100)

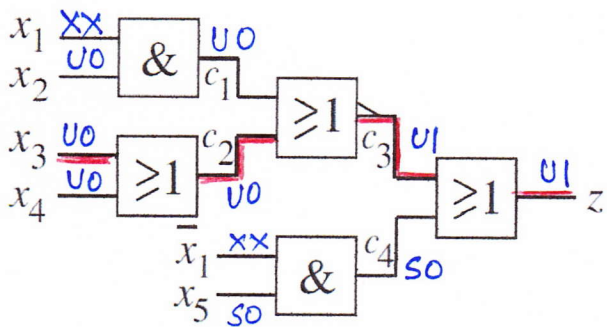
### Non-robust Pattern



$\uparrow x_3 c_2 c_3 z$

$\therefore$  Test pattern sequence :  
(xx0xx, 0x100)

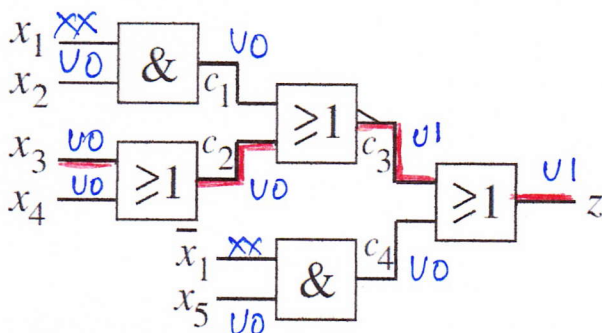
### 3.(ii) Robust Pattern



$\downarrow x_3 c_2 c_3 z$

$\therefore$  Test pattern sequence :  
(xx1x0, x0000)

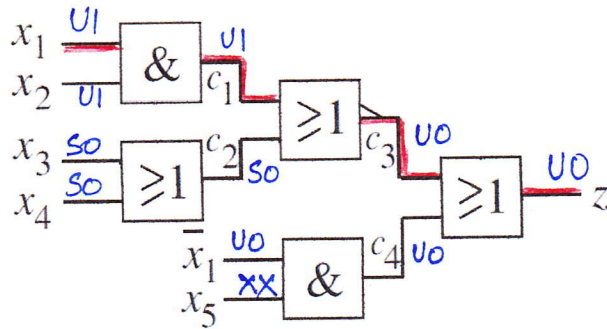
### Non-robust pattern



$\downarrow x_3 c_2 c_3 z$

(xx1xx, x0000)

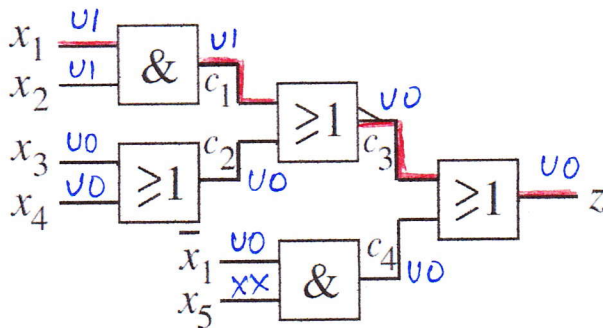
### 3.(iii) Robust Pattern



$\uparrow x_1, c_1, c_3, z$

$\therefore$  Test pattern sequence :  
(0x00x, 1100x)

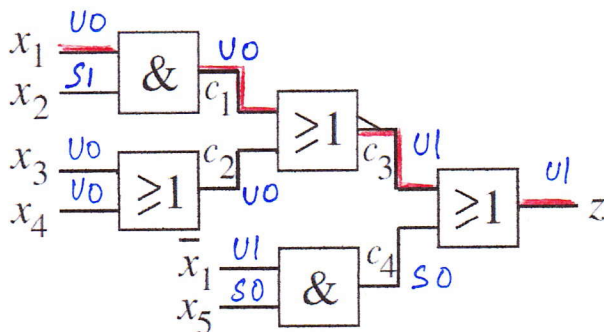
### Non-robust pattern



$\uparrow x_1, c_1, c_3, z$

$\therefore$  Test pattern sequence :  
(0xxxxx, 1100x)

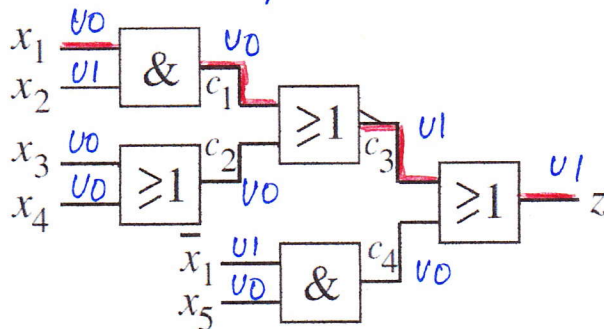
### 3.(iv) Robust pattern



$\downarrow x_1, c_1, c_3, z$

$\therefore$  Test pattern sequence :  
(11xx0, 01000)

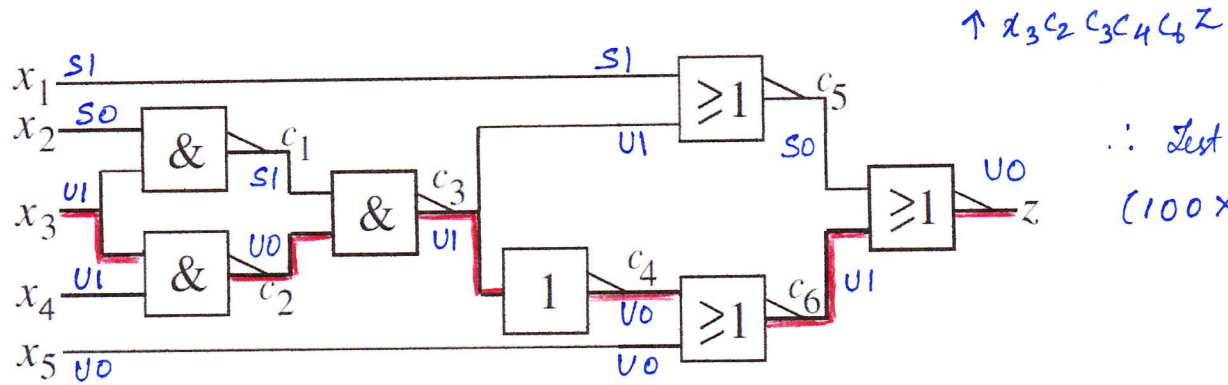
### Non-robust pattern



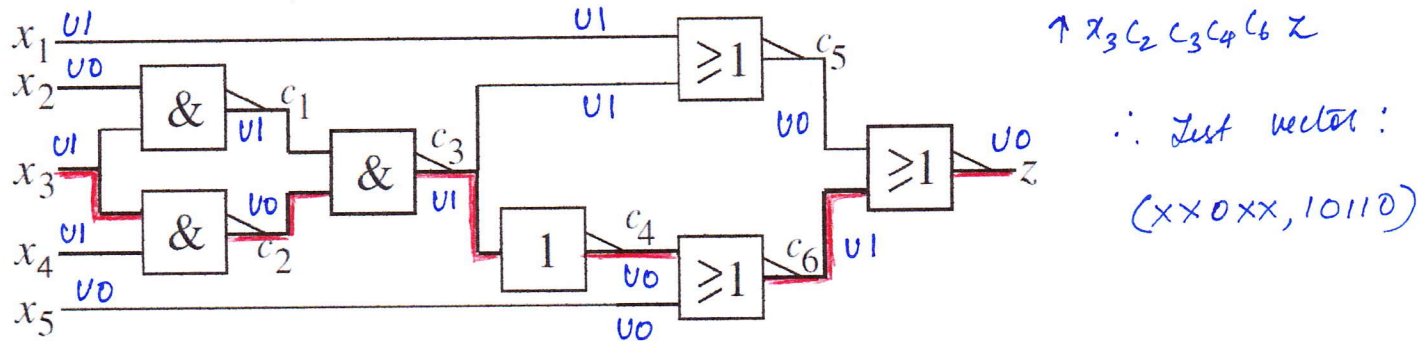
$\downarrow x_1, c_1, c_3, z$

$\therefore$  Test pattern sequence :  
(1xxxx, 01000)

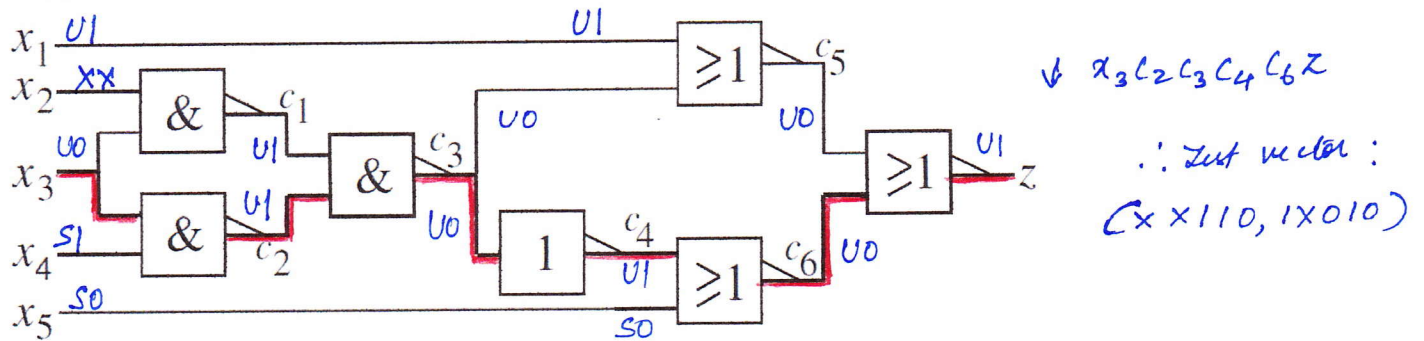
#### 4 (i) Robust pattern



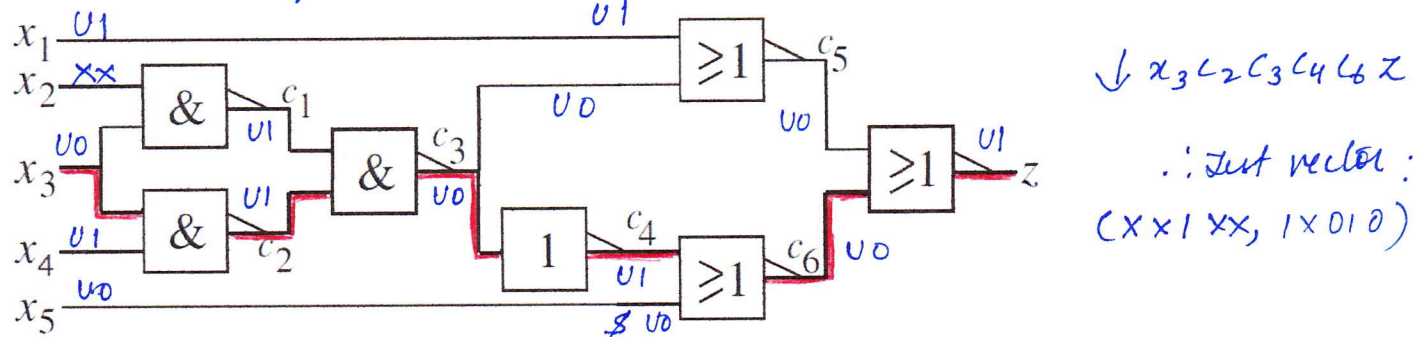
#### (ii) Non-robust pattern



#### 4 (ii) Robust Pattern

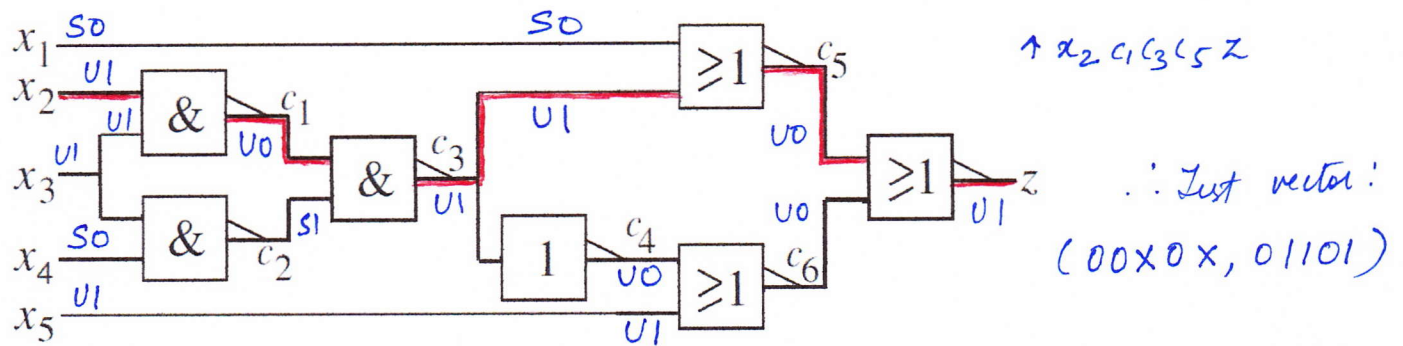


#### Non-robust pattern

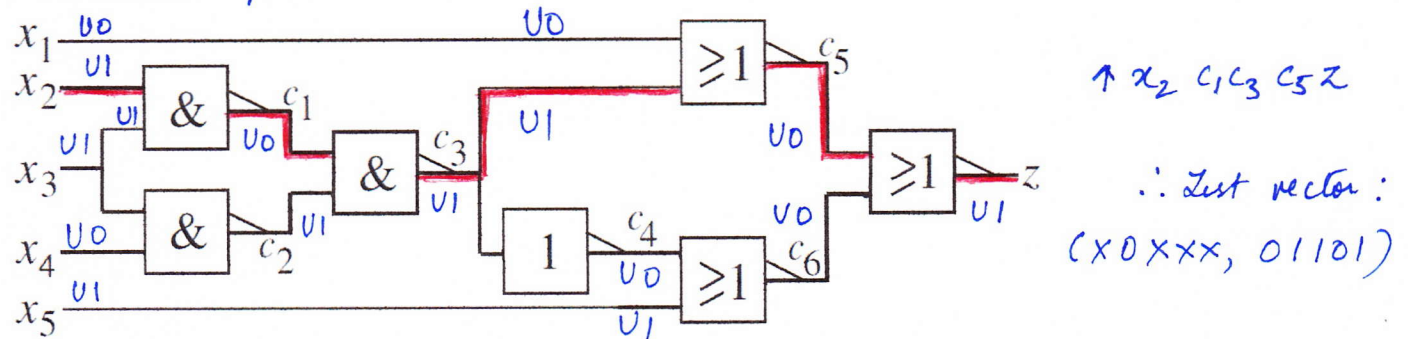




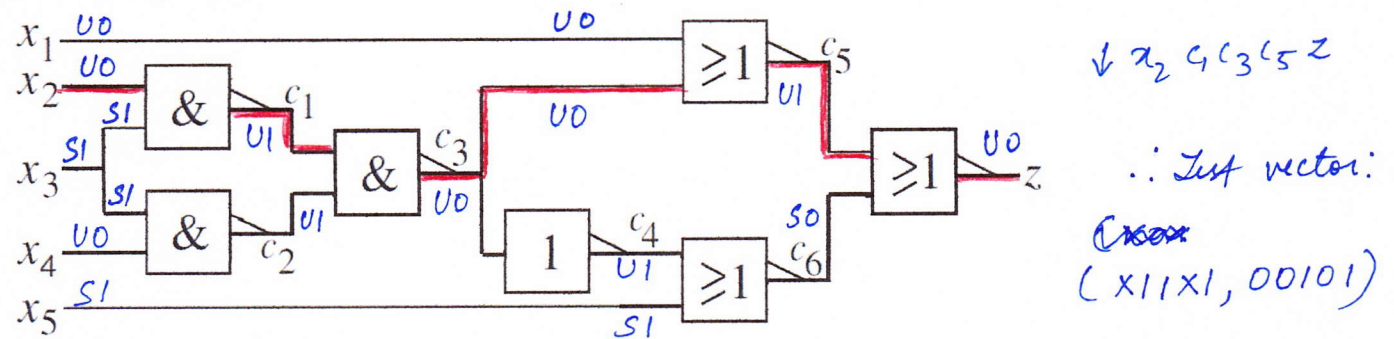
4 ciii) Robust pattern



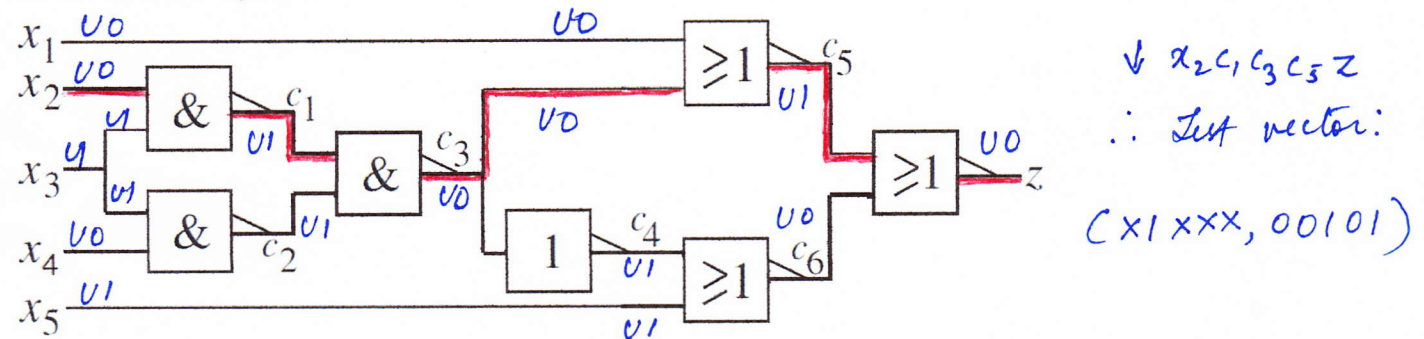
Non-robust pattern



4. (iv) Robust pattern



Non-robust pattern



**Problem 1- continued**

**Problem 14.4 of textbook**

**Problem 14.4:** Proof that March C- detects all unlinked CFdss

March C- algorithm: {  $\Downarrow(w0)$ ;  $\Uparrow(r0, w1)$ ;  $\Uparrow(r1, w0)$ ;  $\Downarrow(r0, w1)$ ;  $\Downarrow(r1, w0)$ ;  $\Downarrow(r0)$  }

March elements: M0 M1 M2 M3 M4 M5

Note: The fault  $\langle r0; \downarrow \rangle_{av}$  means that the  $r0$  operation applied to the a-cell causes a  $\downarrow$  transition in the v-cell; for the case  $a < v$  (i.e., the address of the a-cell is lower than the address of the v-cell).

The fault  $\langle w1; \downarrow \rangle_{va}$  means that the  $w1$  applied to the a-cell causes a  $\downarrow$  transition in the v-cell, for  $v < a$ .

| Operation<br>on a-cell | Disturbance<br>of v-cell | Fault detected by march element, or march pair |         |
|------------------------|--------------------------|--|---------|
|                        |                          | $a < v$  | $a > v$ |
| $r0$                   | $\downarrow$             | M3-M4  | M1-M2   |
| $r0$                   | $\uparrow$               | M1   | M3      |
| $r1$                   | $\downarrow$             | M2   | M4      |
| $r1$                   | $\uparrow$               | M4-M5  | M2-M3   |
| $w0$                   | $\downarrow$             | M2   | M4      |
| $w0$                   | $\uparrow$               | M4-M5  | M2-M3   |
| $w1$                   | $\downarrow$             | M3-M4  | M1-M2   |
| $w1$                   | $\uparrow$               | M1   | M3      |

From inspecting the table, one can verify that all CFdss are detected by March C-.

Problem 14.5 of textbook

Consider the following MATS + scheme

$$\{\uparrow\downarrow(w_0); \uparrow(r_0, w_1); \downarrow(r_1, w_0)\}$$

Expansion B-cells/word the following scheme is applied.

$$\{\uparrow\downarrow(w_a); \uparrow(r_a, w_b); \downarrow(r_b, w_a)\}$$

where  $b$  is complement of  $a$ , ' $a$ ' & ' $b$ ' are called background words also written as;

$$\{\uparrow\downarrow(w_{00\dots 0}); \uparrow(r_{00\dots 0}, w_{11\dots 1}); \downarrow(r_{11\dots 1}, w_{00\dots 0})\}$$

- \* Since SAF is related to single cell, SAFs can be detected only
- \* Since  $(r_{11\dots 1} \dots w_{11\dots 1})$  and  $(r_{00\dots 0} \dots w_{00\dots 0})$  are satisfied with  $M_1$  &  $M_2$  it can detect AFs

Ex: Example of a MATS + algo for a memory with  $B=4$  consider the foll scheme.

$$\{\uparrow\downarrow(w_{0000}); \uparrow(r_{0000}, w_{1111}); \downarrow(r_{1111}, w_{0000})\}$$

$M_0 \qquad \qquad \qquad M_1 \qquad \qquad \qquad M_2$

The above scheme can detect SA-0 & SA1

4 Zeroes are expected which will detect SA1 in any cell  
Hlly SA0 is detected with  $M_1$  &  $M_2$ .

**Problem 1—continued**

**Problem 14.6 of textbook**

**Problem 14.6:** The restrictions for march tests when applied to FIFOs are:

1. The RA (WA) is automatically *incremented* upon completion of a Read (Write) operation; hence, only the  $\uparrow$  address order can be used in march elements.
2. Because of the fact that the RA and WA automatically increment upon completion of every Read (Write) operation, a march element can only contain a single Read and/or a single Write operation; i.e., only march elements of the following forms are possible:  
 $\uparrow(rx), \uparrow(wx), \uparrow(rx, wy), \uparrow(wy, rx)$ ; where  $x, y \in \{0, 1\}$ .

E.g.,  $\uparrow(w0), \uparrow(r0, w1), \uparrow(r1, w0), \uparrow(w0, r1)$ , etc., are examples of possible march elements. The consequence of these restrictions is that not all AFs and not all CFs will be detectable.

7.) Problem 14.7 of textbook;

→ Memory is one-bit wide, thus, the following take place:  
 $A[0] = 0$ ,  $A[1] = 1$ ,  $A[2] = 0$ , ...,  $A[256] = 0$  ...

→ Read  $A[I]$  and write the complement  $A[1023] = 1$

$A[0] = 1$ ,  $A[1] = 0$ ,  $A[2] = 1$ , ...,  $A[256] = 1$  ...

$A[1023] = 0$

→ Read  $A[I]$

- (i) To detect unlinked Afs, either  $(rx \dots w\bar{x})$  or  $(r\bar{x} \dots wx)$  is used. If  $(r0, w1)$  was used only

$A[0]$ ,  $A[2]$  were detected. Thus, all the Afs cannot be detected.

- (ii) For Stuck-At faults: SA0:  $\{\Downarrow w0; \uparrow(w1, r1)\}$  is used and SA1:  $\{\Downarrow w1; \uparrow(w0, r0)\}$  is used. Thus, all the SAFs can be detected.

- (iii) Since, there is only one transition, all TFs cannot be detected.

- (iv) All the CFs cannot be detected by this test. e.g.  $\langle 0; 1 \rangle$  cannot be detected.



**Problem 1- continued**

**Problem 14.8 of textbook**

**Problem 14.8:** Design a minimal march test which detects the following faults:

1. Linked CFids of the form  $\langle \uparrow; \downarrow \rangle a_1 v \# \langle \uparrow; \uparrow \rangle a_2 v$

Note: For the set of linked CFids of the form:  $\langle \uparrow; \downarrow \rangle a_1 v \# \langle \uparrow; \uparrow \rangle a_2 v$  holds that  $a_1 < v$  and  $a_2 < v$ ; in addition the set consists of two members: 1.  $a_1 < a_2$  and 2.  $a_2 < a_1$ . This fault will be detected by the test:  $\{\uparrow(w0); \uparrow(r0, w1); \uparrow(r1, w0, w1)\}$

2. Linked CFids of the form  $\langle \uparrow; \downarrow \rangle \# \langle \uparrow; \uparrow \rangle$

Note: For the set of linked CFids of the form  $\langle \uparrow; \downarrow \rangle \# \langle \uparrow; \uparrow \rangle$  holds that the a-cells may take on any position relative to the v-cell; the set therefore consists of six members. This fault will be detected by the test:  $\{\uparrow(w0); \uparrow(r0, w1); \uparrow(r1, w0, w1); \downarrow(r1, w0, w1); \downarrow(w0); \downarrow(r0, w1)\}$

## Problem 5

| Faults   | Sensitizes    | Detects       |
|--|---------------|---------------|
| AF   | M2            | M3            |
|  | M1            | M4            |
| SAF  | M0            | M1            |
|  | M1            | M2            |
| TF   | M1            | M2            |
|  | M2            | M3            |
| CFin ( $a < v, \langle \uparrow; \uparrow \rangle$ )   | M1            | M1            |
| CFin ( $a < v, \langle \downarrow; \uparrow \rangle$ ) | M2            | M2            |
| CFin ( $a > v, \langle \uparrow; \uparrow \rangle$ )   | M3            | M3            |
| CFin ( $a > v, \langle \downarrow; \uparrow \rangle$ ) | M4            | M4            |
| CFid ( $a < v, \langle \uparrow; 0 \rangle$ )          | M3            | M4            |
| CFid ( $a < v, \langle \uparrow; 1 \rangle$ )          | M1            | M1            |
| CFid ( $a < v, \langle \downarrow; 0 \rangle$ )        | M2            | M2            |
| CFid ( $a < v, \langle \downarrow; 1 \rangle$ )        | M4            | M5            |
| CFid ( $a > v, \langle \uparrow; 0 \rangle$ )          | M1            | M4            |
| CFid ( $a > v, \langle \uparrow; 1 \rangle$ )          | M3            | M3            |
| CFid ( $a > v, \langle \downarrow; 0 \rangle$ )        | M4            | M4            |
| CFid ( $a > v, \langle \downarrow; 1 \rangle$ )        | M2            | M3            |
| CFst( $a < v, \langle 0; 0 \rangle$ )                  | M2            | M2            |
| CFst( $a < v, \langle 0; 1 \rangle$ )                  | M4            | M5            |
| CFst( $a < v, \langle 1; 0 \rangle$ )                  | M3            | M4            |
| CFst( $a < v, \langle 1; 1 \rangle$ )                  | M1            | M1            |
| CFst( $a > v, \langle 0; 0 \rangle$ )                  | M4            | M4            |
| CFst( $a > v, \langle 0; 1 \rangle$ )                  | M2            | M3            |
| CFst( $a > v, \langle 1; 0 \rangle$ )                  | M1            | M2            |
| CFst( $a > v, \langle 1; 1 \rangle$ )                  | M3            | M3            |
| linked CFid  | Cannot detect | Cannot detect |

## Problem 6

| Faults   | Sensitizes | Detects |
|--|------------|---------|
| AF   | M5         | M5      |
| SAF  | M1         | M1      |
|  | M2         | M2      |
| TF   | M1         | M1      |
|  | M2         | M2      |
| CFin ( $a < v, \langle \uparrow; \uparrow \rangle$ )   | M1         | M1      |
| CFin ( $a < v, \langle \downarrow; \uparrow \rangle$ ) | M2         | M2      |
| CFin ( $a > v, \langle \uparrow; \uparrow \rangle$ )   | M3         | M3      |
| CFin ( $a > v, \langle \downarrow; \uparrow \rangle$ ) | M4         | M4      |
| CFid ( $a < v, \langle \uparrow; 0 \rangle$ )          | M3         | M4      |
| CFid ( $a < v, \langle \uparrow; 1 \rangle$ )          | M1         | M1      |
| CFid ( $a < v, \langle \downarrow; 0 \rangle$ )        | M2         | M2      |
| CFid ( $a < v, \langle \downarrow; 1 \rangle$ )        | M4         | M5      |
| CFid ( $a > v, \langle \uparrow; 0 \rangle$ )          | M1         | M2      |
| CFid ( $a > v, \langle \uparrow; 1 \rangle$ )          | M3         | M3      |
| CFid ( $a > v, \langle \downarrow; 0 \rangle$ )        | M4         | M4      |
| CFid ( $a > v, \langle \downarrow; 1 \rangle$ )        | M2         | M5      |
| CFst( $a < v, \langle 0; 0 \rangle$ )                  | M2         | M2      |
| CFst( $a < v, \langle 0; 1 \rangle$ )                  | M2         | M3      |
| CFst( $a < v, \langle 1; 0 \rangle$ )                  | M3         | M4      |
| CFst( $a < v, \langle 1; 1 \rangle$ )                  | M1         | M1      |
| CFst( $a > v, \langle 0; 0 \rangle$ )                  | M1         | M1      |
| CFst( $a > v, \langle 0; 1 \rangle$ )                  | M2         | M2      |
| CFst( $a > v, \langle 1; 0 \rangle$ )                  | M4         | M4      |
| CFst( $a > v, \langle 1; 1 \rangle$ )                  | M3         | M3      |
| linked CFid  | M2         | M3      |
|  | M1         | M4      |
|  | M4         | M5      |
|  | M3         | M6      |