

# Demographic Origins of the Startup Deficit<sup>1</sup>

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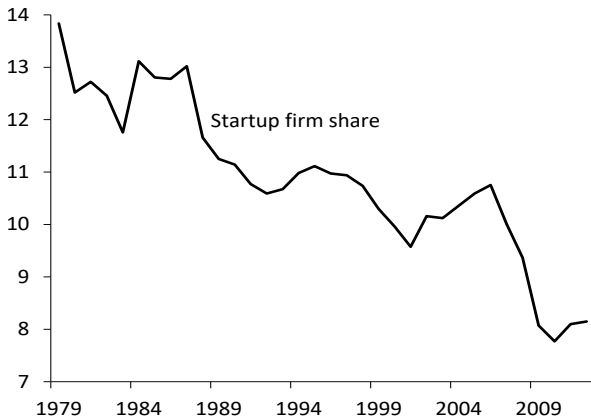
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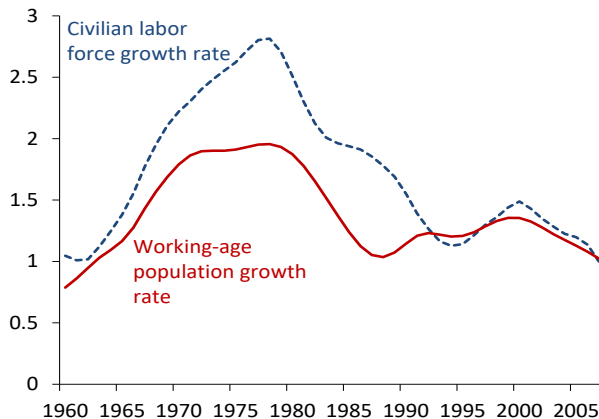
<sup>1</sup>Any opinions and conclusions expressed herein are those of the author(s) and do not necessarily represent the views of the U.S. Census Bureau, Federal Reserve Bank of New York or the Federal Reserve System. All results have been reviewed to ensure that no confidential information is disclosed.

# U.S. startup rate

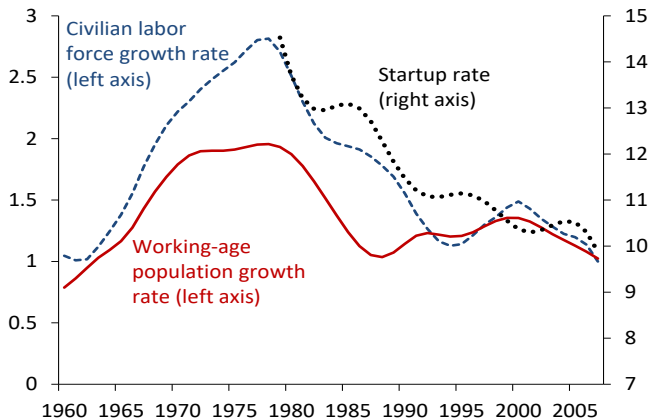


Source: U.S. Census Bureau Business Dynamics Statistics.

## Annual labor supply growth rate trend, 1960-2007



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**Demographic Channel:** Decline in the labor supply growth rate is a key driver of the decline in firm entry.

Linking labor supply growth and firm entry

# A stylized firm dynamics framework

Consider an economy with

- ▶  $\mu_t$  identically sized firms
- ▶ exogenous exit,  $x_t$
- ▶  $M_t$  firms enter
- ▶ labor supply,  $N_t$ , grows at rate  $\eta_t$

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Number of firms evolves according to

$$\mu_{t+1} = (1 - x_t)\mu_t + M_{t+1}.$$

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Number of firms per worker  $\bar{\mu}_t \equiv \mu_t / N_t$  evolves as

$$\bar{\mu}_{t+1} = \frac{1 - x_t}{1 + \eta_t} \bar{\mu}_t + \bar{M}_{t+1}.$$



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$$\text{Flow-balance } SR(\eta, x) = \frac{\eta + x}{1 + \eta}$$

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$$\eta \downarrow \implies SR \downarrow$$

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## Flow-balance startup rates: 1980-1984 and 2003-2007

Measure labor supply growth using working-age population and compute the flow-balance startup rates.

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| in %    | Startup Rate |
|---------|--------------|
| 1980-84 | 12.51        |
| 2003-07 | 10.37        |
| Decline | 2.14         |

The startup rate declined by 2.14 ppts.

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| 1980-84 | 12.51        | 1.67     |
| 2003-07 | 10.37        | 1.11     |
| Decline | 2.14         | 0.56     |

Working-age population growth rate declined by 0.56 ppts.

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| in %    | Startup Rate | $\eta_t$ | $SR(\eta_t, \bar{x}_{80s})$ |
|---------|--------------|----------|-----------------------------|
| 1980-84 | 12.51        | 1.67     | 10.91                       |
| 2003-07 | 10.37        | 1.11     | 10.42                       |
| Decline | 2.14         | 0.56     | 0.49                        |

Decline in  $\eta$  explains **1/4** of the decline in the startup rate.

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|---------|--------------|----------|---------------------------|-------|
| 1980-84 | 12.51        | 1.67     | 10.91                     | 9.43  |
| 2003-07 | 10.37        | 1.11     | 10.42                     | 8.47  |
| Decline | 2.14         | 0.56     | 0.49                      | 0.96  |

Exit rate,  $x$ , also declined in the same period.



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| in %    | Startup Rate | $\eta_t$ | $SR(\eta, \bar{x}_{80s})$ | $x_t$ | $SR(\eta_t, x_t)$ |
|---------|--------------|----------|---------------------------|-------|-------------------|
| 1980-84 | 12.51        | 1.67     | 10.91                     | 9.43  | 10.91             |
| 2003-07 | 10.37        | 1.11     | 10.42                     | 8.47  | 9.48              |
| Decline | 2.14         | 0.56     | 0.49                      | 0.96  | 1.43              |

Declines in  $\eta$  and  $x$  roughly account for **2/3** of the decline.

# Limitations of the stylized framework

Various simplifications:

- ▶ exit is exogenous and not linked to changes in  $\eta$
- ▶ firm size is fixed and there is no incumbent employment growth
- ▶ there is no heterogeneity in firm behavior by age/size

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Need an equilibrium model with entry, exit, and labor supply growth to evaluate the demographic channel quantitatively.

An equilibrium framework

# Model ingredients

Hopenhayn and Rogerson (1993) with labor supply growth

- ▶ Household grows at rate  $\eta$
- ▶ Continuum of incumbent firms have DRS technology with idiosyncratic productivity
- ▶ Firms face fixed operating costs and are subject to quadratic labor adjustment costs
- ▶ Free entry condition equates expected value of startup with entry cost

# Long-run effect of a decline in labor supply growth rate

1. Real wages **do not** change in response to lower labor force growth.
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⇒ in the long run all adjustment to **labor supply shocks** is through the **entry margin**.

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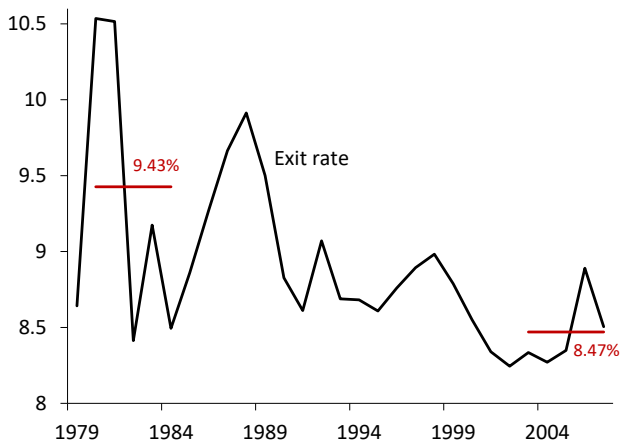
⇒ age composition changes the **aggregate exit rate** despite unchanged incumbent margins

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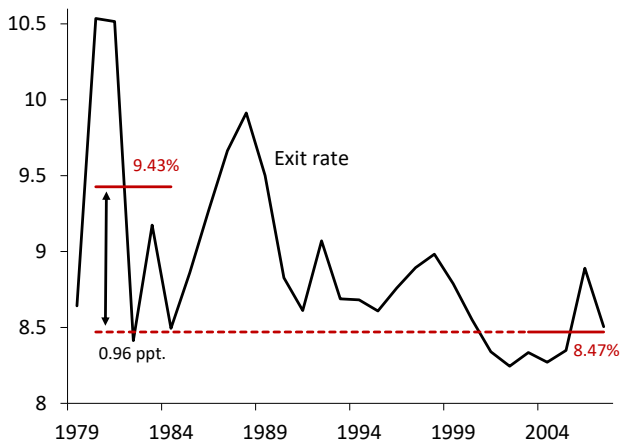
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Compare the balanced growth path of the economy corresponding to **high  $\eta$**  (1980-84) and **low  $\eta$**  (2003-07)

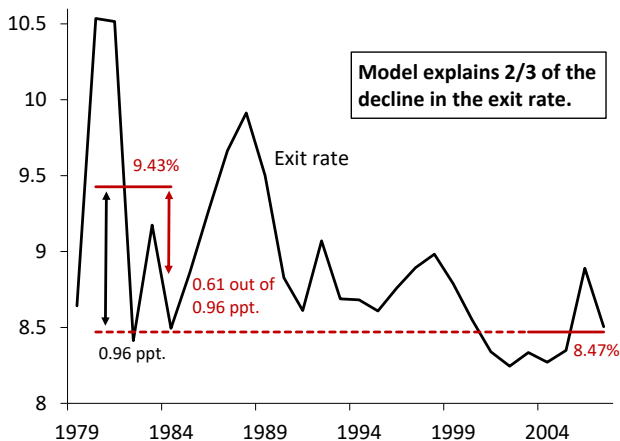
## The decline in the exit rate: data vs model



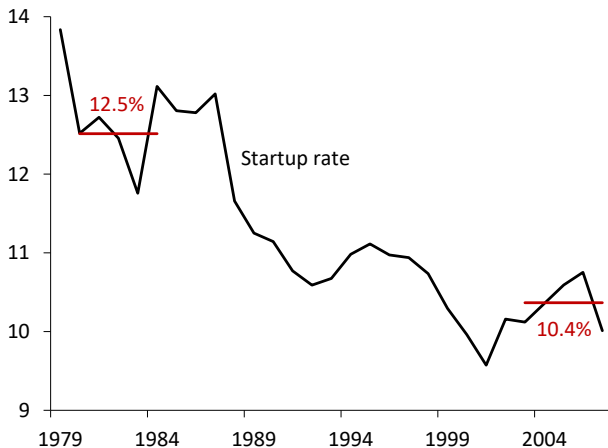
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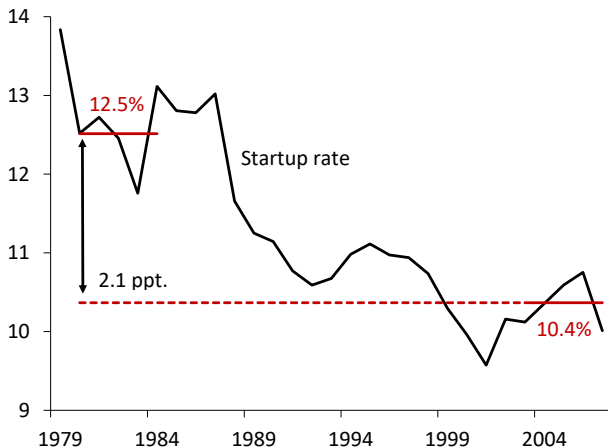
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## The decline in the startup rate: data vs model

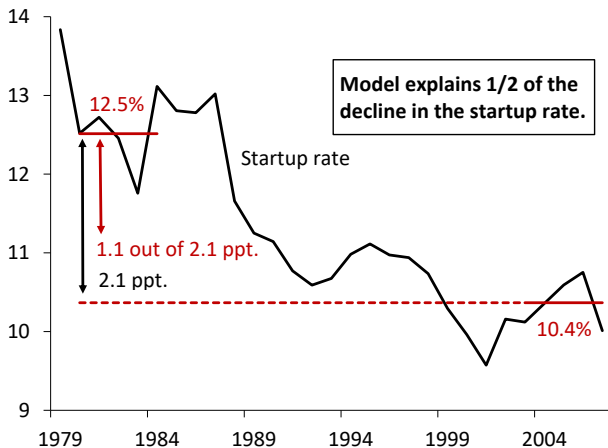


## The decline in the startup rate: data vs model





## The decline in the startup rate: data vs model



## Other channels in the model

Compute the change required for each channel to explain full decline in the startup rate

|                                      | Data      | Labor<br>supply GR |
|--------------------------------------|-----------|--------------------|
| Required change                      |           | -1.2ppts           |
| $\Delta$ startup size                | +1.3%     | 0                  |
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| Required change                      |           | -1.2ppts           | +59.47%       |
| $\Delta$ startup size                | +1.3%     | 0                  | +11.77%       |
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## Other channels in the model

Compute the change required for each channel to explain full decline in the startup rate

|                                      | Data      | Labor<br>supply GR | Entry<br>cost | Operating<br>cost |
|--------------------------------------|-----------|--------------------|---------------|-------------------|
| Required change                      |           | -1.2ppts           | +59.47%       | -45.28%           |
| $\Delta$ startup size                | +1.3%     | 0                  | +11.77%       | -47.16%           |
| $\Delta$ exit rate (age 3, size <50) | -0.17ppts | 0                  | -1.16ppts     | -1.39ppts         |

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Required changes are substantial and have counterfactual implications for other margins of firm dynamics

Testing the demographic channel in the  
cross-section

## Cross-state variation in labor supply shifts

$$SR_{st} = \beta \mathbf{g}_{st} + \text{State FE}_s + \text{Year FE}_t + \epsilon_{st}$$



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Generate exogenous movements in labor supply growth,  $\mathbf{g}_{st}$ .

- ▶ Fertility instrument ( $IV_1$ ): predict state-level labor supply growth with 20 year lags of birth rates
- ▶ Migration instrument ( $IV_2$ ): predict state-level labor supply growth with lagged inter-state migration patterns

## Labor supply growth and start-up rate in cross-section

|                                   | OLS                | $IV_1$            | $IV_2$            | $IV_1$ & $IV_2$    |
|-----------------------------------|--------------------|-------------------|-------------------|--------------------|
| Labor supply growth<br>(20-64, %) | 0.60***<br>(0.054) | 0.78***<br>(0.25) | 1.18***<br>(0.18) | 1.04***<br>(0.218) |
| Observations                      | 1,316              | 1,316             | 1,316             | 1,316              |
| $R^2$                             | 0.90               | 0.89              | 0.85              | 0.87               |
| F-stat                            | -                  | 24.88             | 14.99             | 13.39              |

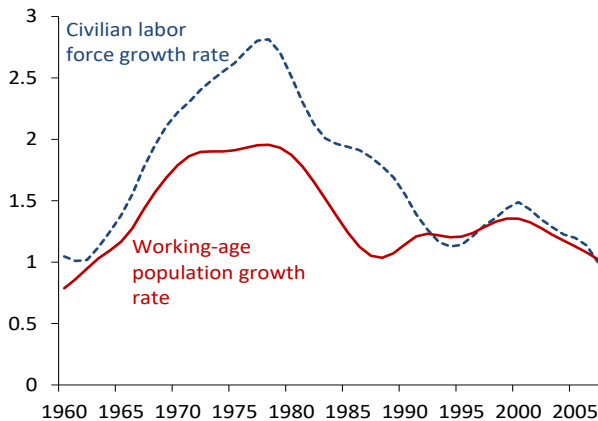
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- ▶ The data support a causal effect of the demographic channel.
- ▶ The effect is robust to detailed industry controls, using different measure of labor supply, and adding state-specific trends.
- ▶ Accounts for between 20 to 30 percent of the decline if the elasticity estimates are applied to the aggregate data.

Testing the demographic channel in the  
time-series

## Rising labor supply growth rate in 1960-1980



## Implications for the 1960-1980 period

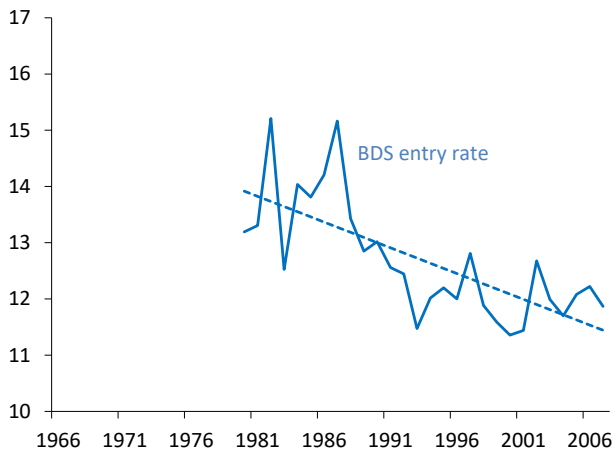
Startup rates should have been rising with labor supply growth.

We test this time-series implication using data from the County Business Patterns (CBP).

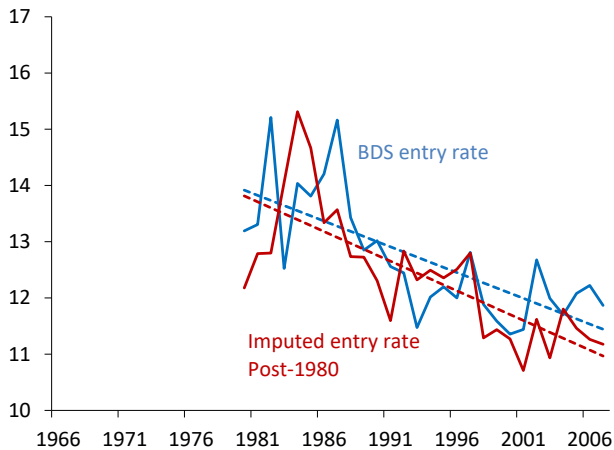
- ▶ CBP has been published annually since 1964.
- ▶ New method to impute establishment entry rate from CBP cross sections

**Key idea: impute gross entry rate from observed net establishment entry rate and statistical model for exit rate**

# Historical establishment entry rates

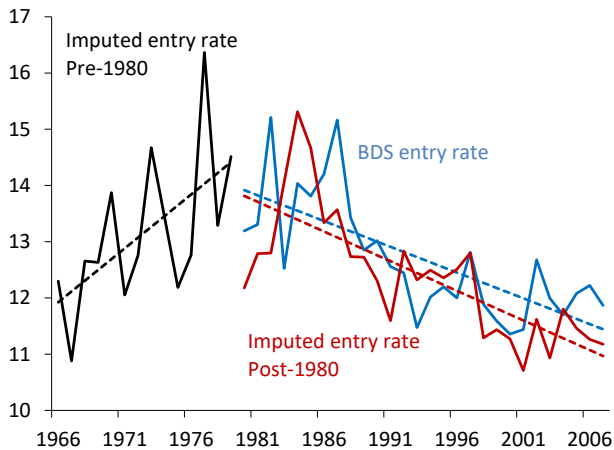


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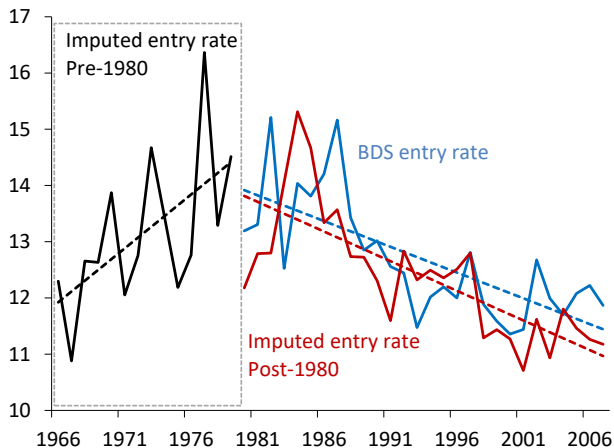




# Historical establishment entry rates



## Pattern consistent with the demographic channel



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1. Calibrated model implies that around half of the decline in entry can be explained solely by the demographic channel.
2. We tested this hypothesis using cross-sectional variation in labor supply growth and found that the data support a significant causal effect.
3. Earlier data support the relationship we have established in the post-1980 data.