1 Python correction

```
1 from skimage.io import imread # read input image
import numpy as np
3 import matplotlib.pyplot as plt
5 from scipy.spatial import Delaunay # Delaunay triangulation
```

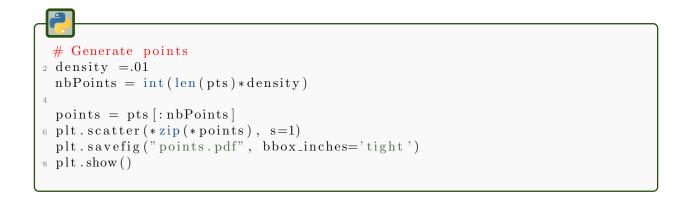
1.1 Point pattern

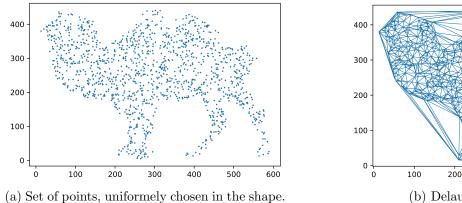
The image is first loaded.

```
A = imread('camel.png')
m,n = A.shape
```

All coordinates of pixels constituting the shape are extracted. The following code mainly consist of array manipulation.

Then, given a certain density, points are randomly chosen in the shape. They are displayed in Fig.1.





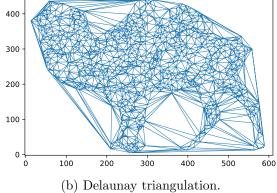


Figure 1: Set of points and its Delaunay triangulation.

1.2 Delaunay triangulation

The Delaunay triangulation is simply obtained by the following code. The result is presented in Fig.1.

```
tri = Delaunay(points)

# Display result
4 plt.triplot(points[:,0], points[:,1], tri.simplices, lw=.5)
plt.show()
```

1.3 Alpha-solid

In order to build the alpha-solid, the circum-radii of all triangles should be computed. A rather simple way to do this is to use the class Triangle of sympy.geometry. The use of progressbar displays a progress bar, as the computation might take a long time. The sympy module is a symbolic computation module, and does not an optimal algorithm for this task.

Then, given a radius, one can filter the triangles. The results are presented in Fig.2.

```
for R in progressbar.progressbar([5,10, 50, 100, 100000]):

r = np.array(radius) < R

fig = plt.figure()
    plt.triplot(points[:,0], points[:,1], tri.simplices[r], lw=.5)
    plt.scatter(points[:,0], points[:,1], c='y', s=10)
    plt.show()
```

1.4 To go further

There exist a python module dedicated to alpha-shapes. Here is a solution that uses it:

```
import alphashape
import matplotlib.pyplot as plt
from descartes import PolygonPatch
```

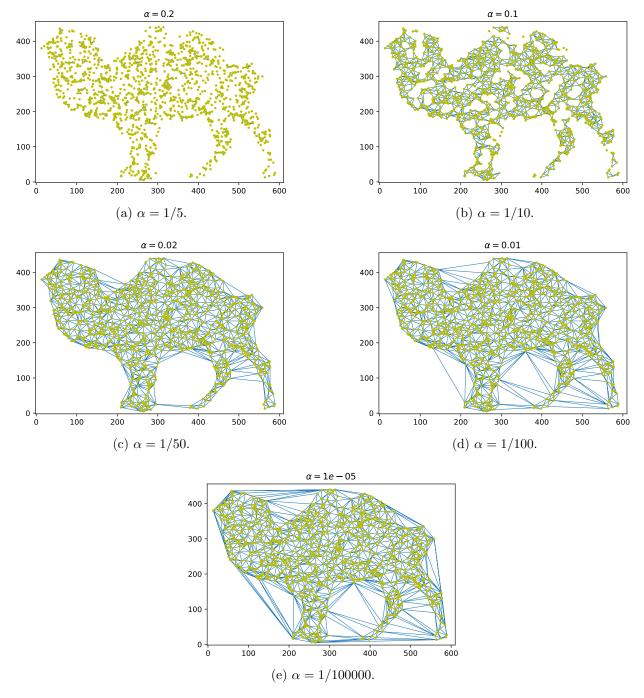


Figure 2: Different alpha-solids.

```
for R in progressbar.progressbar([5, 10, 50, 100, 100000]):

# Generate the alpha shape

alpha_shape = alphashape.alphashape(points, 1/R)

# Initialize plot
fig, ax = plt.subplots()

# Plot input points
ax.scatter(*zip(*points), s=1)

# Plot alpha shape
ax.add_patch(PolygonPatch(alpha_shape, alpha=.2))
plt.title(fr"$\alpha={R}$")
plt.show()
```

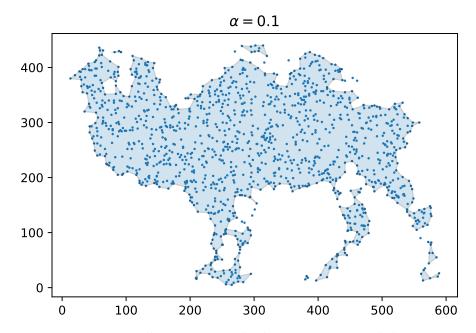


Figure 3: Illustration with the alphashape module.