

David Pick
CM 2403
Formal Methods

OK 2a) Holds

OK 2b) $p = \{\text{Thing\$1} \rightarrow \text{Thing\$0}\}$, $q = \{\text{Thing\$0} \rightarrow \text{Thing\$0}\}$, $s = \{\text{Thing\$0}, \text{Thing\$1}\}$
 $(s.(p - q) = \{\text{Thing\$0}, \text{Thing\$1}\}) \neq (s.p - s.q = \{\})$

OK 2c) $p = \{\text{Thing\$1} \rightarrow \text{Thing\$0}, \text{Thing\$1} \rightarrow \text{Thing\$1}\}$, $q = \{\text{Thing\$0} \rightarrow \text{Thing\$0}, \text{Thing\$0} \rightarrow \text{Thing\$1}\}$,
 $s = \{\text{Thing\$0}, \text{Thing\$1}\}$
 $(s.(p \& q) = \{\}) \neq (s.p \& s.q = \{\text{Thing\$0}, \text{Thing\$1}\})$

(-1) Model missing from submission doc but present in repository

3)

OK // Problem A.1.5

module homework/hw3_2

sig Node {}

//each node has 1 parent except for root node

//root node has no parent

//there is only 1 root node

//two nodes can't have the same children

//you can reach all nodes from the root node

//nodes can have 0 or more children

pred isTree[r: Node -> Node] {

//one n1: Node | n1->n1 in r //1 node without parent

//two nodes can't have the same child

all n1, n2: Node | n1->n2 in r implies not n2->n1 in r

all n1, n2, n3: Node |

n1->n2 in ^r and n2->n3 in r implies not n3->n1 in r

one n1: Node | no n2: Node | n2->n1 in r

all n1: Node | lone n2: Node | n2->n1 in r

}

run isTree for 4

4)

// Problem A.1.10

// Written by David Pick

module homework/hw3_3

abstract sig Name {

address: set Addr + Name

}

sig Alias, Group extends Name {}

sig Addr {}

```

// invariants
fact {
  // Put your answers to a and b here, plus the
  // additional invariant noted below.

  //there is no name, that has itself in the address
OK all n: Name | not n in n.^address

  //all names eventually map to an address
  //All names (in the domain of the address relation) eventually map to an address.
OK all n: address.univ |
  one a: Addr |
  a in n.^address

  //alias's must map to only 1 address or name
OK all a: Alias | #a.^address < 2
}

// simulation constraints
pred show[] {
  // Put your answers to c and d here.

  // You may want to add additional constraints to make
  // the generated instances more interesting.

  //the address book has at least two levels.
  //a name must be connected to a name, which is then connected to
  //either another name or and address
OK some n1, n2: Name, a: Addr | n1->n2 in address and n2->a in address

  //some groups are non-empty
OK some g: Group | some g.address
  some g: Group | no g.address
  //Group.address :> Name
  //
  //Alias.^address
}

run show for 3 but 6 Name
OK 4 e) Group.address :> Name
OK 4 f) Group-address.univ
OK 4 g) Alias.^address

6) 4 hours

```