

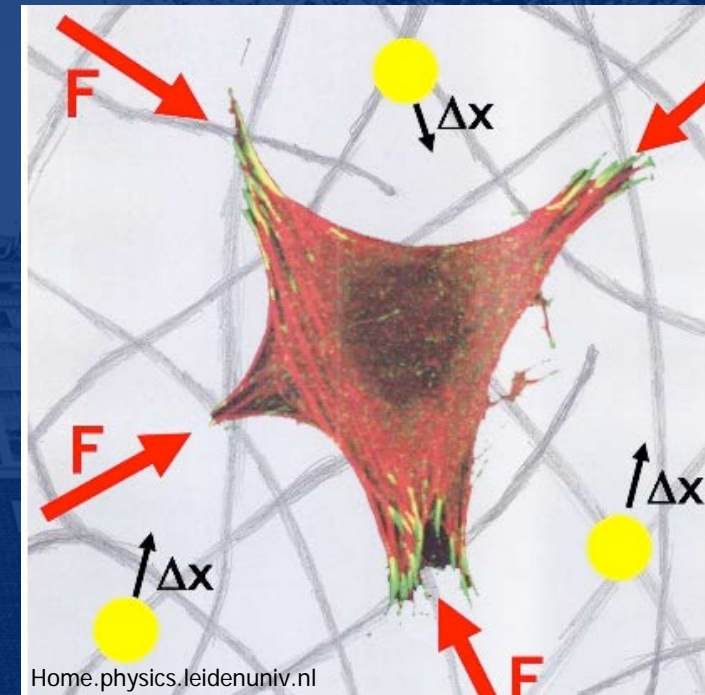


JOHNS HOPKINS

WHITING SCHOOL
of ENGINEERING

Cell and Tissue Engineering

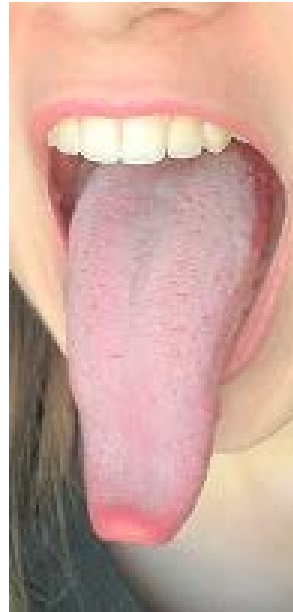
Non-ideal Mechanics in the Human Body



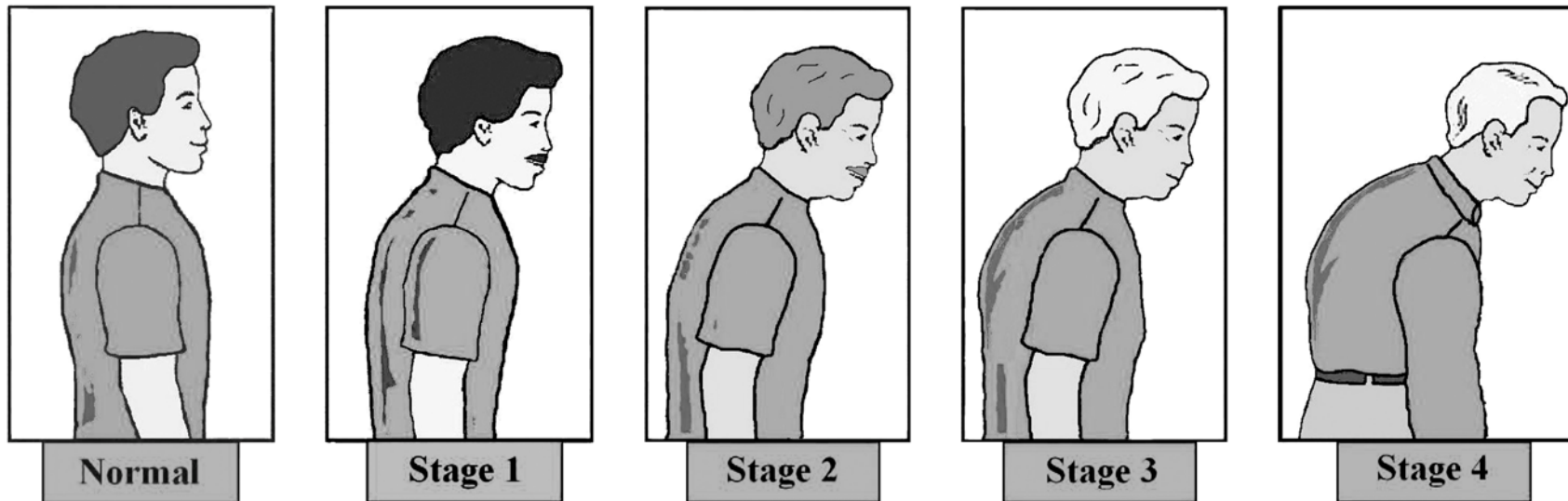
Modeling non-ideal human tissues



Muscular hydrostats are both solid and fluid

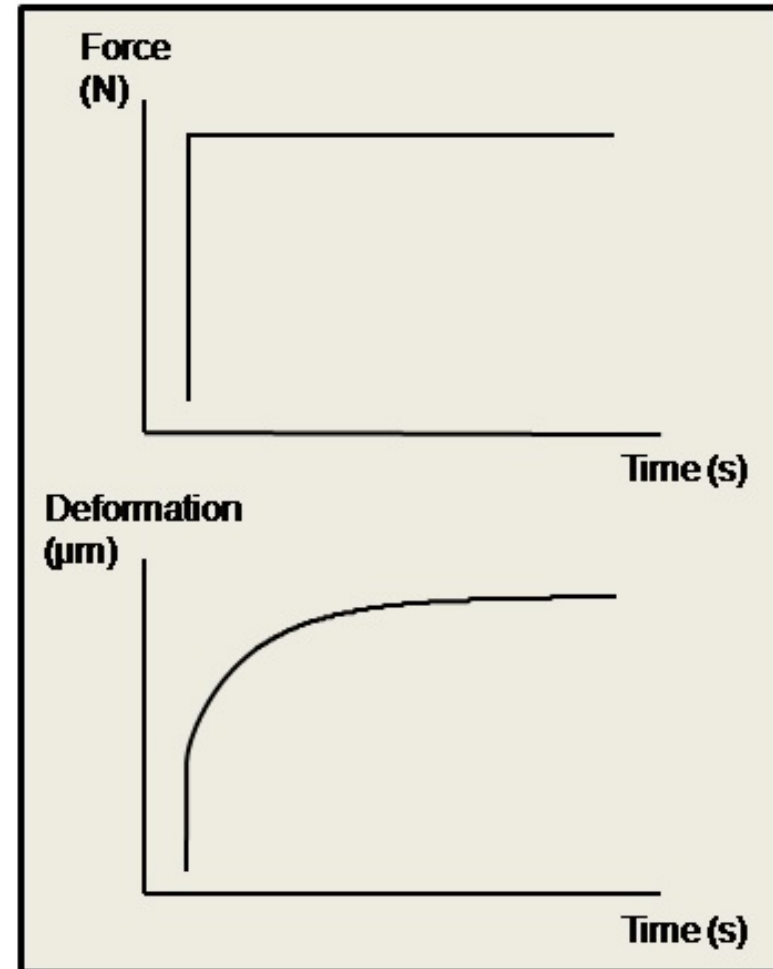


Biological tissues: creep and stress relaxation behaviors



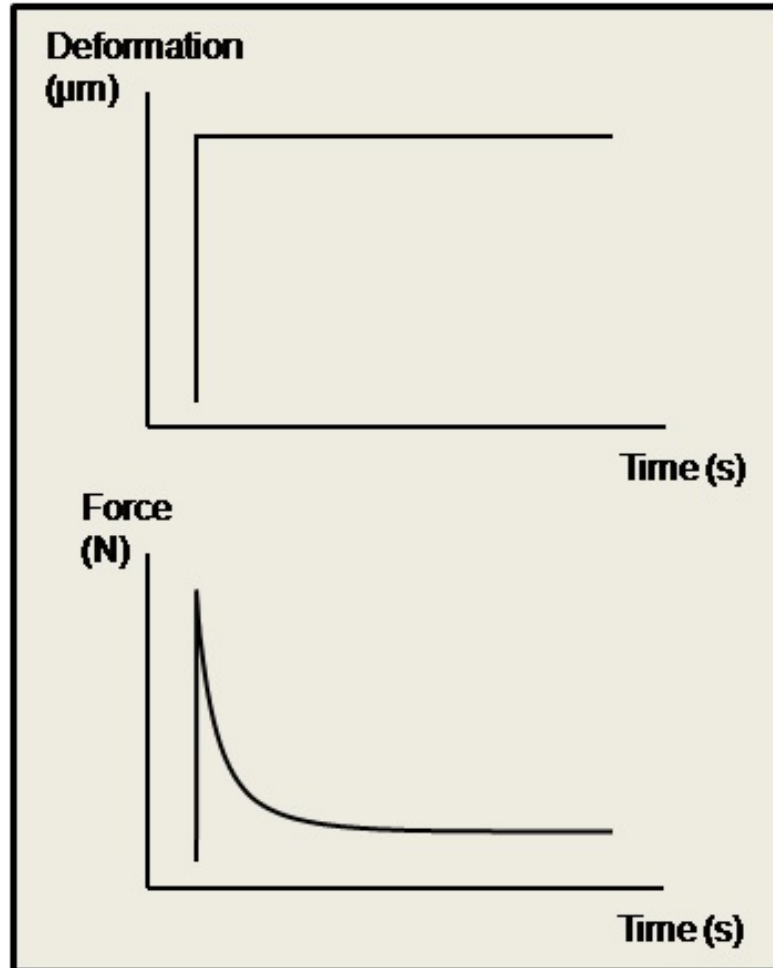
Biological tissues: creep and stress relaxation behaviors

Creep

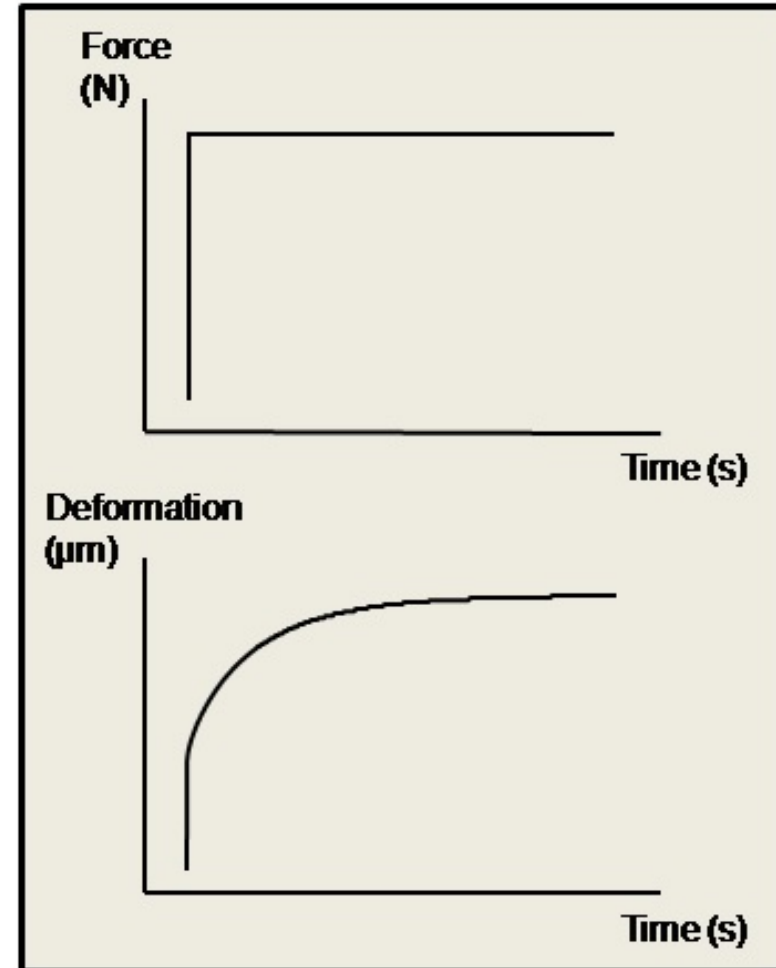


Biological tissues: creep and stress relaxation behaviors

Relaxation

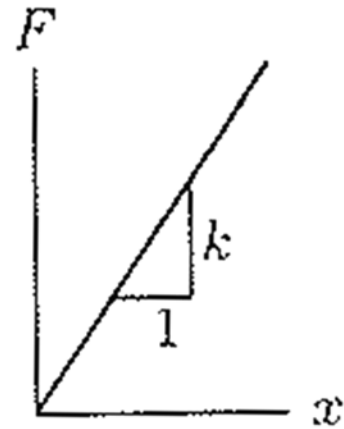
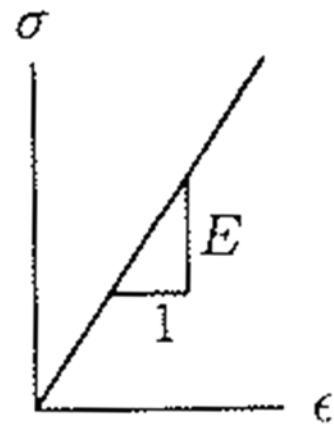
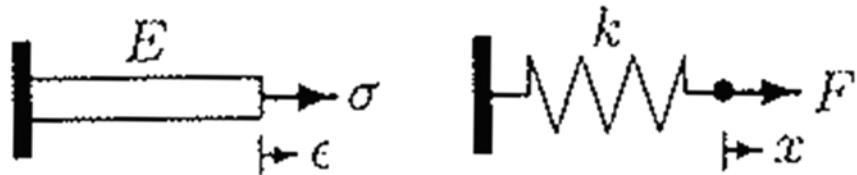


Creep



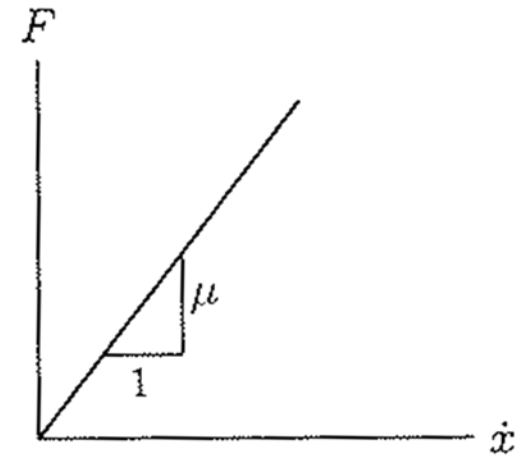
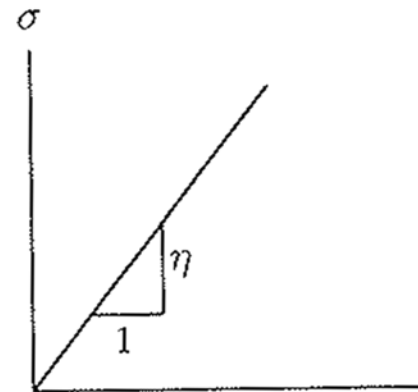
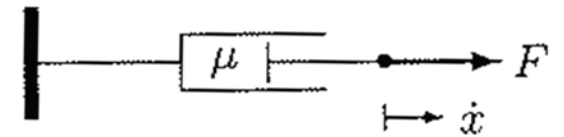
Modeling viscoelastic materials with springs and dashpots

$$\sigma = E\varepsilon \quad F = kx$$



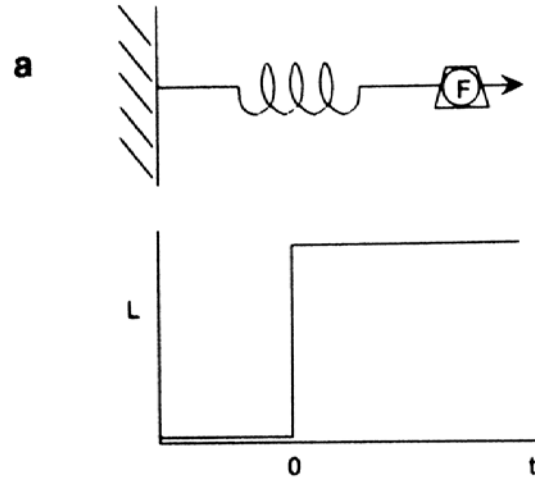
$$\sigma = \eta \dot{\varepsilon}$$

$$F = \eta \frac{dx}{dt}$$

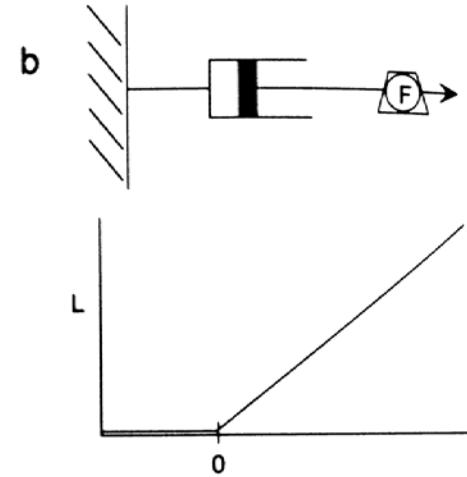


Modeling viscoelastic materials with springs and dashpots

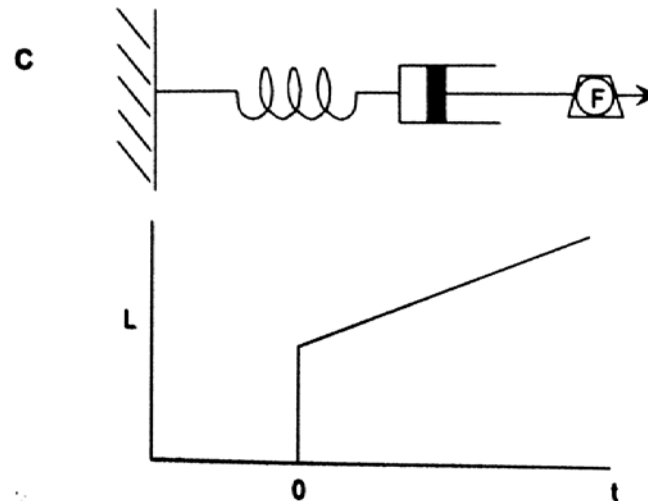
Spring Model



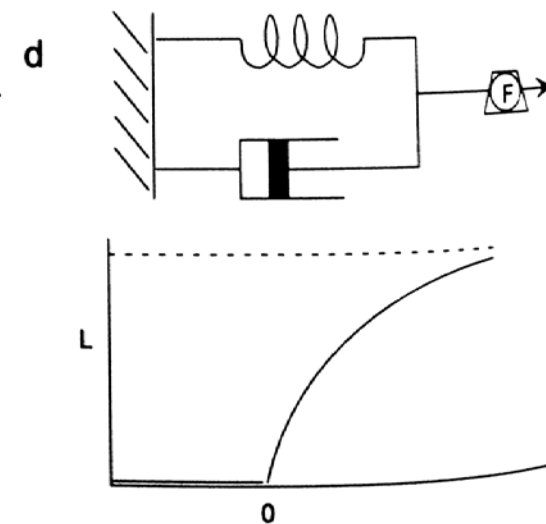
Dashpot Model



Maxwell Model

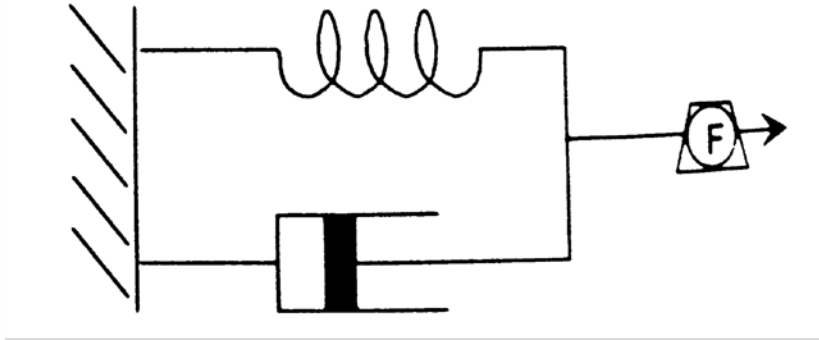


Voigt Model



Deriving differential equations for viscoelastic models

Voigt Model



$$F = kx \quad \text{spring}$$

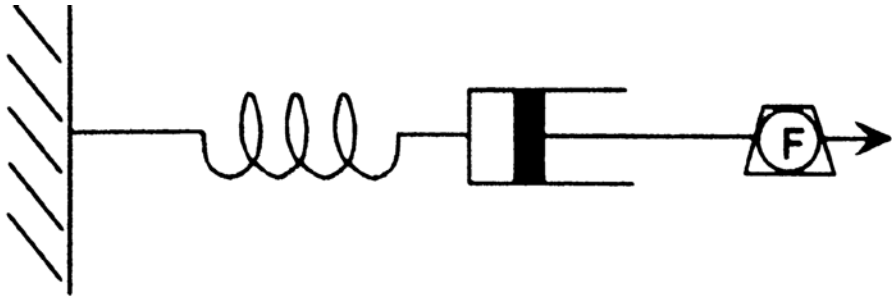
$$F = \eta \frac{\delta x}{\delta t} \quad \text{dashpot}$$

$$F = F_1 + F_2$$

$$F = kx + \eta \frac{\delta x}{\delta t}$$

Deriving differential equations for viscoelastic models

Maxwell Model



$$F = kx \quad \text{spring}$$

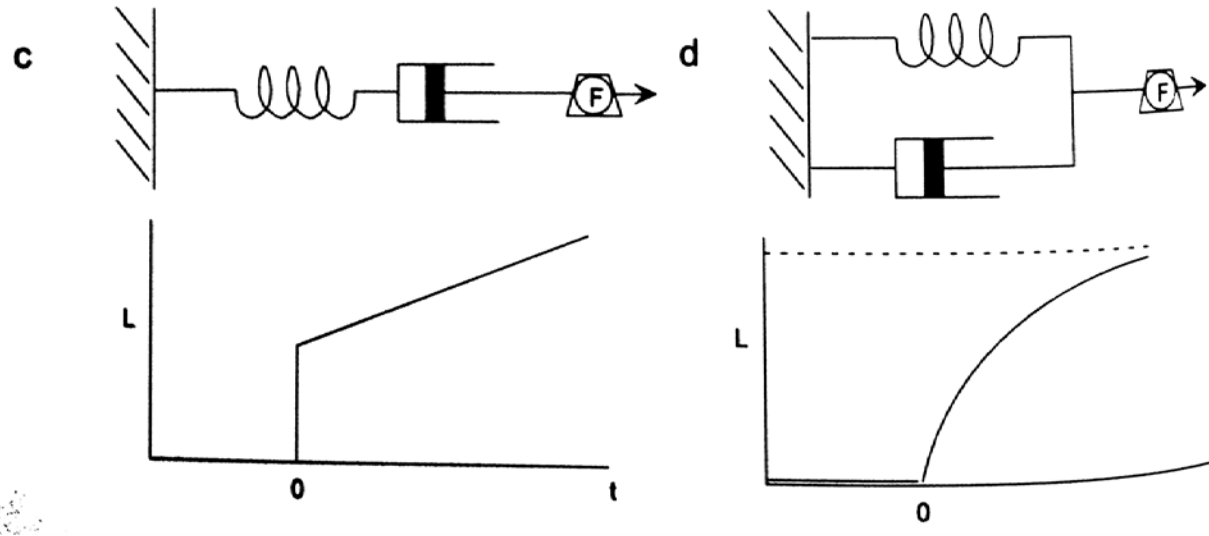
$$F = \eta \frac{\delta x}{\delta t} \quad \text{dashpot}$$

$$x = x_1 + x_2 \quad \frac{dx}{dt} = \frac{dx_1}{dt} + \frac{dx_2}{dt}$$

$$\frac{dx}{dt} = \frac{dF / dt}{k} + \frac{F}{\eta}$$

Review and rewind

Viscoelastics modeling





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