

Diffusion Potential – Nernst Equation Assumptions

- Membrane
 - Constant thickness ✓
 - Homogeneous ~~X~~, but ✓
 - Infinite extent in transverse plane
 - Allows one dimensional solution ✓
- Solutions
 - Well mixed (uniform in space, temperature, etc.) ✓
 - Concentrations do not change as problem moves forward ✓

Diffusion Potential – Nernst Equation

Assumptions, continued

- Ionic mobility and activity coefficient are constant
 - Over time (as problem goes forward) ✓
 - Same in both solutions and in membrane ✗, but ✓
- No net flow of solvent through membrane
 - Osmotic pressure gradient negligible ✓
 - Hydrostatic pressure gradient negligible ✓

$$V_{\text{Nernst}} = \frac{R \cdot T}{z \cdot F} \cdot \ln \left(\frac{[S]_{\text{out}}}{[S]_{\text{in}}} \right)$$

Observations regarding Nernst equation

- $V_{\text{membrane, measured}} = V_{\text{Nernst, calculated}}$
 - Ion is in electro-chemical equilibrium across membrane
 - No net flux of ion across membrane
- $V_{\text{membrane, measured}}$ is same sign as $V_{\text{Nernst, calculated}}$ but is of larger magnitude
 - Electrical force “larger” than chemical force
 - Ion will move in direction of electrical force
- $V_{\text{membrane, measured}}$ is same sign as $V_{\text{Nernst, calculated}}$ but is of smaller magnitude
 - Chemical force “larger” than electrical force
 - Ion will move in direction of chemical force
- $V_{\text{membrane, measured}}$ is of opposite sign to that of $V_{\text{Nernst, calculated}}$ calculated
 - Chemical and electrical forces acting in same direction
 - Ion is not in equilibrium; it will move, driven by both chemical and electrical forces

$$V_{\text{GHK,Na,K,Cl}} = \frac{R \cdot T}{F} \cdot \ln \left(\frac{P_{\text{Na}} \cdot [\text{Na}]_{\text{o}} + P_{\text{K}} \cdot [\text{K}]_{\text{o}} + P_{\text{Cl}} \cdot [\text{Cl}]_{\text{i}}}{P_{\text{Na}} \cdot [\text{Na}]_{\text{i}} + P_{\text{K}} \cdot [\text{K}]_{\text{i}} + P_{\text{Cl}} \cdot [\text{Cl}]_{\text{o}}} \right)$$

$$I = g(E_m - E_N)$$

$$I_K = g_K(E_m - E_K)$$

$$I_{Na} = g_{Na}(E_m - E_{Na})$$

$$I_{Cl} = g_{Cl}(E_m - E_{Cl})$$

$$I_K + I_{Na} + I_{Cl} = 0$$

$$g_K (E_m - E_K) + g_{Na} (E_m - E_{Na}) + g_{Cl} (E_m - E_{Cl}) = 0$$

$$E_m (g_K + g_{Na} + g_{Cl}) = g_K E_K + g_{Na} E_{Na} + g_{Cl} E_{Cl}$$

$$E_m = \frac{g_K}{\Sigma g} E_K + \frac{g_{Na}}{\Sigma g} E_{Na} + \frac{g_{Cl}}{\Sigma g} E_{Cl}$$

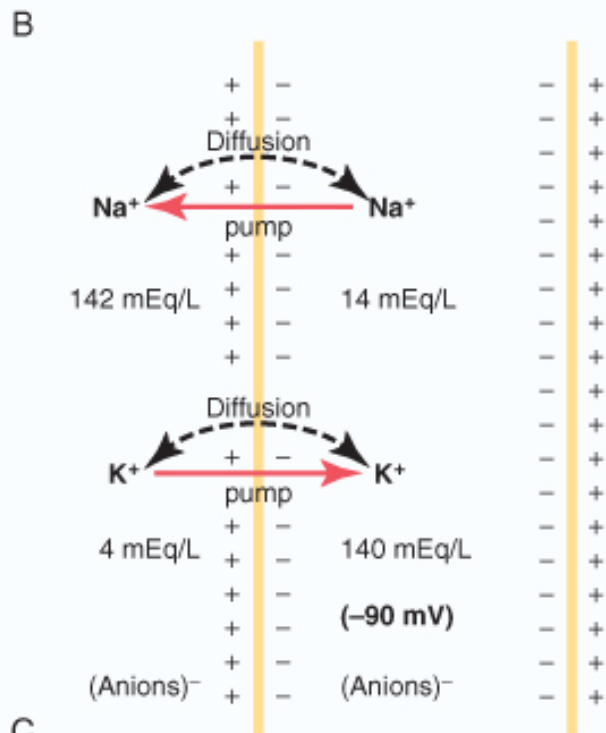
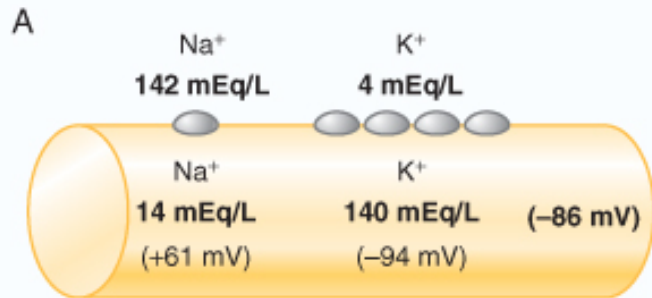
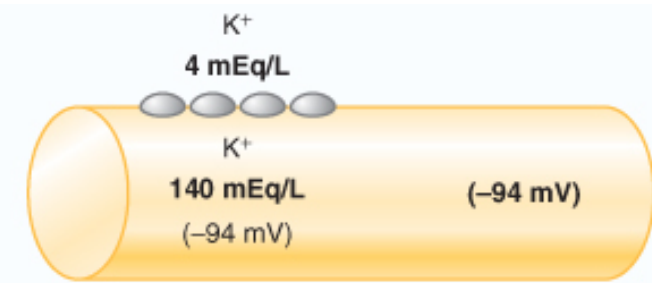


Figure 5-5 Establishment of resting membrane potentials in nerve fibers under three conditions: A, when the membrane potential is caused entirely by potassium diffusion alone; B, when the membrane potential is caused by diffusion of both sodium and potassium ions; and C, when the membrane potential is caused by diffusion of both sodium and potassium ions plus pumping of both these ions by the Na^+-K^+ pump.

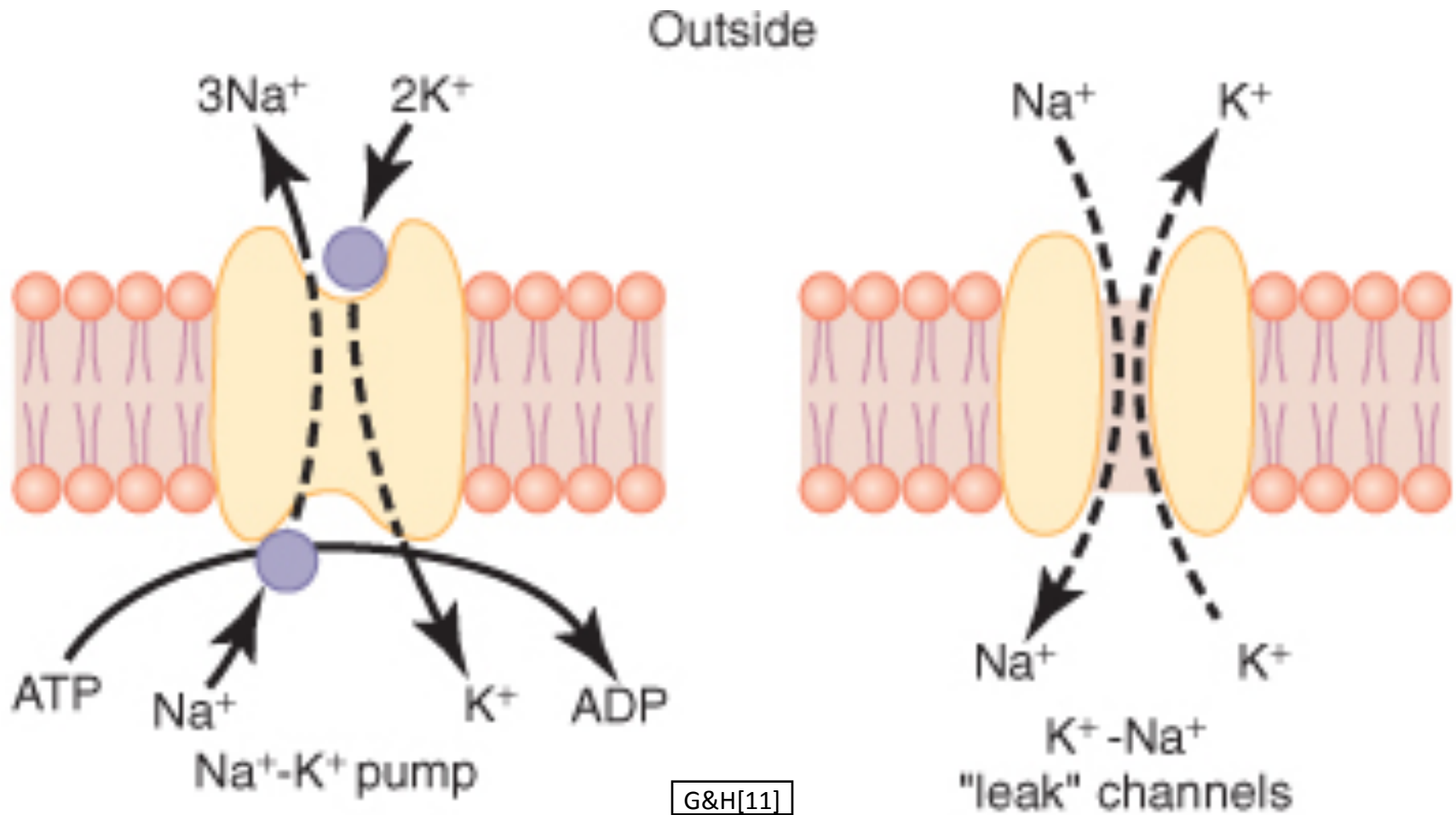


Figure 5-4 Functional characteristics of the Na⁺-K⁺ pump and of the K⁺-Na⁺ "leak" channels. ADP, adenosine diphosphate; ATP, adenosine triphosphate.

END

Video 7, Module 1