Scales of measurement
Chi-Square GOF test
Chi-Square test of independence
Practice Problem



# 9 — Chi-Squared tests

### 9.1 Scales of measurement

**Definition 9.1** — **Ordinal Data**. There is a clear order in the data set but the distance between data points is unimportant.

**Definition 9.2** — **Interval Data**. Similar to an ordinal set of data in that there is a clear ranking, but each group is divided into equal intervals

**Definition 9.3** — Ratio Data. Similar to interval data except there exists an absolute zero.

**Definition 9.4** — **Nominal Data**. This is the same as qualitative data, where we differentiates between items or subjects based only on their names and/or categories and other qualitative classifications they belong to.

| Type of Data | Example                    | Data   |
|--------------|----------------------------|--|
| Ordinal      | Ranks in a race            | 1st, 2nd, 3rd  |
| Interval     | Temperature in Celsius     | $-10^{\circ} - 0^{\circ}, 1^{\circ} - 10^{\circ}, 11^{\circ} - 20^{\circ}$ |
| Ratio        | Percentage correct on test | 0-10%, 11-20%, 21-30%  |
| Nominal      | Shirt Colors               | Red, Blue, Yellow, White   |

Table 9.1: Examples of different scales of measurement

■ Example 9.1

### 9.2 Chi-Square GOF test

The Chi-Square GOF test allows us to see how well observed values match expected values for a certain variable. In particular we compare the frequencies of our data sets.

## 9.2.1 Chi-Square test of independence

This variation of the Chi-Square test is used to determine if 2 nominal variables are independent. In particular we use the marginal totals.

#### 9.3 Practice Problem

Problem 9.1 A poker-dealing machine is supposed to deal cards at random, as if from an infinite deck. In a test, you counted 1600 cards, and observed the following: table[h]

| Suit     | Count |             |
|----------|-------|-------------|
| Spades   | 404   | _           |
| Hearts   | 420   | Card counts |
| Diamonds | 400   |             |
| Clubs    | 376   |             |

Could it be that the suits are equally likely? Or are these discrepancies too much to be random?