

Prob of your guess is correct

$$I_G = 1 - \sum (p_i)^2$$

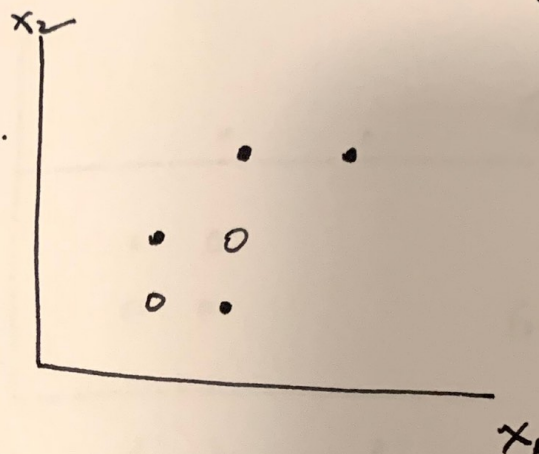
↓
Prob you are right.

w/ no chops.

$$\text{guess white right} = \frac{2}{6}$$

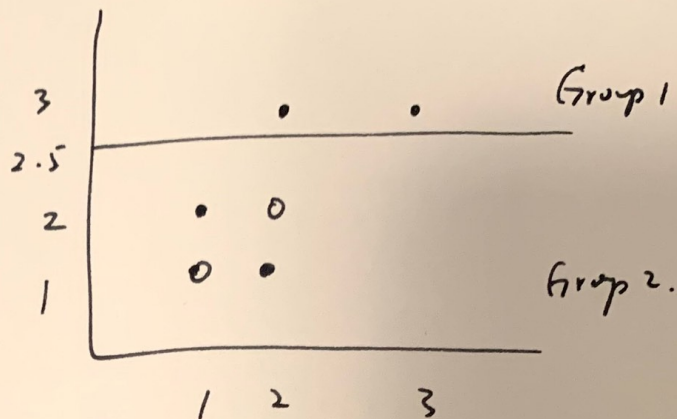
$$\text{guess black} = \frac{4}{6}$$

Decision Tree



$$\therefore I_{\text{root}} = 1 - \left(\left(\frac{2}{6} \right)^2 + \left(\frac{4}{6} \right)^2 \right) \quad \text{ex } 2.48 \approx \text{Entropy}$$

Compute entropy for each group.



$$I_{\text{Group 1}} = 1 - \left(\left(\frac{\text{black}}{2} \right)^2 + \left(\frac{\text{white}}{2} \right)^2 \right) = 0$$

$$I_{\text{Group 2}} = 1 - \left(\left(\frac{\text{black}}{4} \right)^2 + \left(\frac{\text{white}}{4} \right)^2 \right) = 0.5$$

$$I_G = \frac{2}{6} \cdot I_{\text{Group 1}} + \frac{4}{6} I_{\text{Group 2}} = \frac{1}{3} < 0.444$$

total.

∴ Entropy reduce after chopping

