

```
In [1]: import pandas as pd
import numpy as np
from tqdm import tqdm
from sklearn.linear_model import LinearRegression
from matplotlib import pyplot as plt
```

```
In [2]: df = pd.read_csv('movieReplicationSet(1).csv')
mean_of_user = df.iloc[:, :400].mean(axis=1, skipna=True)
mean_of_movie = df.iloc[:, :400].mean(axis=0, skipna=True)
for i in range(df.shape[0]):
    for j in range(400):
        if np.isnan(df.iloc[i, j]):
            df.iloc[i, j] = (mean_of_user[i] + mean_of_movie[j]) / 2

# user 896 has no ratings
df = df.drop(896, axis=0)
```

```
In [3]: cod = np.zeros((400, 400))
for movie_idx in tqdm(range(400)):
    for other_movie in range(400):
        if other_movie == movie_idx:
            continue
        train_X = df.iloc[:, other_movie] # 1096
        train_Y = df.iloc[:, movie_idx] # 1096
        reg = LinearRegression().fit(train_X.values.reshape(-1, 1), tr
cod[movie_idx, other_movie] = reg.score(train_X.values.reshape(-1, 1))
```

100%|██████████| 400/400 [01:49<00:00, 3.65it/s]

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In [5]: movies = df.columns[:400]
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In [7]: selected_movies_idxs = cod.max(axis=1).argsort()[185:215]
selected_movies = movies[selected_movies_idxs]
candidate_idxs = np.array(list(set(range(400)) - set(selected_movies_idxs)))
feature_movies_idxs = candidate_idxs[np.random.choice(candidate_idxs.size)]
feature_movies = movies[feature_movies_idxs]

X = df.iloc[:, feature_movies_idxs].values
Y = df.iloc[:, selected_movies_idxs].values
# 80/20 random split
train_idxs = np.random.choice(df.shape[0], int(df.shape[0] * 0.8), replace=False)
test_idxs = np.array(list(set(range(df.shape[0])) - set(train_idxs)))
train_X = X[train_idxs]
train_Y = Y[train_idxs]
test_X = X[test_idxs]
test_Y = Y[test_idxs]
```

In [17]: #3

```
from sklearn.linear_model import Ridge, Lasso
from sklearn.metrics import mean_squared_error

pd.set_option('display.max_colwidth', None)

alpha_to_rmse = dict()
alpha_to_beta = dict()
for alpha in tqdm(np.arange(1, 100, 1)):
    tmp_df = pd.DataFrame()
    for i in range(30):
        reg = Ridge(alpha=alpha).fit(train_X, train_Y[:, i]) # betas
        tmp_df.loc[i, 'target movie'] = selected_movies[i]
        tmp_df.loc[i, 'RMSE'] = mean_squared_error(test_Y[:, i], reg.predict(test_X))
        tmp_df.loc[i, 'COD'] = reg.score(test_X, test_Y[:, i])
        tmp_df.loc[i, 'beta'] = str(reg.coef_)
    # print('alpha =', alpha, 'average RMSE =', tmp_df['RMSE'].mean())
    alpha_to_rmse[alpha] = tmp_df['RMSE'].mean()
    alpha_to_beta[alpha] = tmp_df['beta'].values
    # display(tmp_df)
print('best alpha', min(alpha_to_rmse, key=alpha_to_rmse.get))
print('best beta', alpha_to_beta[min(alpha_to_rmse, key=alpha_to_rmse.get)])
```

100%|██████████| 99/99 [00:07<00:00, 14.01it/s]

```
best alpha 36
best beta [ '[0.27540373 0.08764685 0.04177319 0.09743275 0.07991411
0.07459153\n 0.00581997 0.05936197 0.01237043 0.05756957] '
'[ 0.23193362 0.04645869 0.05737426 0.18511422 0.11273515 0.02
795966\n -0.00131961 0.04563403 0.06168206 0.05942398] '
'[0.11320316 0.05866095 0.01808954 0.22749806 0.21947683 0.07706078
\n 0.03226618 0.06575423 0.10091374 0.06476627] '
'[0.17397535 0.0412683 0.02821257 0.23037068 0.26265426 0.04807646
\n 0.0365501 0.05242761 0.11355068 0.10117706] '
'[ 0.13821916 0.09616787 -0.04028961 0.23395584 0.1919155 0.03
616793\n 0.02074936 0.00027284 0.11928622 0.04272582] '
'[0.16516807 0.12936614 0.01002407 0.14815316 0.05559277 0.04527951
\n 0.0597851 0.02674717 0.05827291 0.04495979] '
'[0.11409997 0.07835787 0.02332109 0.1835247 0.1714847 0.02394124
\n 0.03876157 0.06917344 0.0285601 0.07532343] '
'[0.29395589 0.05160622 0.00653949 0.01406416 0.23843663 0.04407387
\n 0.01295565 0.0502702 0.05576813 0.06506818] '
'[0.19464127 0.09072303 0.01516825 0.15030911 0.11486133 0.02069522
\n 0.0395127 0.01474578 0.09679885 0.05256486] '
'[0.13885097 0.1055441 0.06574639 0.20399883 0.1049835 0.02112654
\n 0.04169164 0.03086192 0.01607419 0.046982 ] '
'[ 0.10796176 0.03755366 0.09044681 0.06485882 0.29830267 0.01
086905\n -0.00378714 0.0487325 0.03276507 0.12844074] '
'[ 0.10369676 0.10629452 0.01440439 -0.01095554 0.27479238 0.11
103829\n 0.02231255 0.00249096 0.05733368 0.07998716] '
'[ 0.22356695 0.09302971 0.0322176 0.17703413 0.12451654 0.06
008587\n 0.02336353 0.03396192 0.03886774 -0.00898165] '
'[0.12460599 0.08128411 0.06330377 0.07237005 0.21521904 0.05659689
```

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\n 0.04574707 0.04763059 0.0325287 0.06933648] '\n  [ 0.22182195 0.08887876 0.03468051 0.19746261 0.23608273 -0.03\n391944\n  0.05798037 0.00944559 0.06858123 0.04634378] '\n  [0.07861118 0.08111483 0.12596278 0.14625924 0.24720374 0.00455786\n\\n 0.11934981 0.09432717 0.06856199 0.05128079] '\n  [-0.02512949 0.08111158 0.17367689 0.03615305 0.25766113 0.03\n886156\n  0.06334568 0.12636933 0.06620493 0.11555253] '\n  [0.12615266 0.0896007 0.02169502 0.15901395 0.17327258 0.02907719\n\\n 0.03231623 0.03593598 0.05124057 0.01156284] '\n  [0.30430526 0.05618969 0.02439172 0.04599458 0.07971465 0.06461299\n\\n 0.01637845 0.08065363 0.01671786 0.08192025] '\n  [0.0600069 0.04830947 0.03486677 0.18385962 0.19257334 0.06079824\n\\n 0.02845586 0.02075501 0.02434861 0.09144478] '\n  [0.25612172 0.04160295 0.02423072 0.11347432 0.10666645 0.0076274\n\\n 0.02806004 0.07993726 0.04711846 0.01430153] '\n  [ 0.197982 0.13479999 -0.02658617 0.13746845 0.21567261 0.04\n753241\n  0.02006443 0.0143684 0.04495706 0.0635622 ] '\n  [0.21872684 0.08088145 0.02461118 0.13878466 0.18566911 0.0276311\n\\n 0.02000326 0.01191844 0.03982044 0.02346613] '\n  [ 0.25140387 0.02673197 0.05294079 0.01025616 0.1044961 0.05\n308579\n  0.0266806 0.10917876 -0.00251249 0.02989873] '\n  [0.23564803 0.12770464 0.03162274 0.05016529 0.23200145 0.00211983\n\\n 0.00405794 0.01377039 0.11352297 0.08846904] '\n  [0.05766665 0.12888028 0.13989779 0.11484549 0.24272716 0.035894\n\\n 0.0335424 0.07016222 0.03426831 0.06472139] '\n  [0.06640745 0.11912194 0.14374705 0.05320636 0.27624112 0.05277367\n\\n 0.05098512 0.07276778 0.09486472 0.00077893] '\n  [ 0.16606247 0.17132847 -0.01503642 0.17961863 0.13582237 0.03
```

```
284111\n  0.01006616  0.01469663  0.07460837  0.00768566]'\n  '[ 0.31714559  0.06091008  0.00992368  0.13398959  0.14715227  0.00\n377599\n -0.00395105  0.06874858  0.05192719  0.05672794]'\n  '[ 0.19232058  0.07526525  0.00337571  0.1032591   0.28096084  0.00\n657233\n  0.01984696 -0.00045116  0.08856002  0.0981605 ]']
```

In [18]: #4

```
from sklearn.linear_model import Ridge, Lasso
from sklearn.metrics import mean_squared_error

pd.set_option('display.max_colwidth', None)

alpha_to_rmse = dict()
for alpha in tqdm(np.arange(0.001, 0.01, 0.0001)):
    tmp_df = pd.DataFrame()
    for i in range(30):
        reg = Lasso(alpha=alpha).fit(train_X, train_Y[:, i]) # betas
        tmp_df.loc[i, 'target movie'] = selected_movies[i]
        tmp_df.loc[i, 'RMSE'] = mean_squared_error(test_Y[:, i], reg.predict(test_X))
        tmp_df.loc[i, 'COD'] = reg.score(test_X, test_Y[:, i])
        tmp_df.loc[i, 'beta'] = str(reg.coef_)
    # print('alpha =', alpha, 'average RMSE =', tmp_df['RMSE'].mean())
    alpha_to_rmse[alpha] = tmp_df['RMSE'].mean()
    alpha_to_beta[alpha] = tmp_df['beta'].values
    # display(tmp_df)
print('best alpha', min(alpha_to_rmse, key=alpha_to_rmse.get))
print('best beta', alpha_to_beta[min(alpha_to_rmse, key=alpha_to_rmse.get)])
```

100%|██████████| 90/90 [00:05<00:00, 17.82it/s]

```
best alpha 0.003400000000000001
best beta ['[0.35399973 0.08306072 0.03746215 0.09079057 0.07459066
0.0716424\n 0.          0.05331556 0.00243288 0.05004826]''
'[ 0.28424257  0.01940489  0.05253768  0.22631892  0.11638925  0.01
708411\n -0.          0.03862771  0.05473605  0.05164779]''
'[0.10728802 0.03377036 0.00568001 0.28831871 0.28549594 0.06660188
\n 0.02150733 0.05933606 0.09425776 0.05334035]''
'[0.19030786 0.00624084 0.01469234 0.28360791 0.34927666 0.03226227
\n 0.02482976 0.04194357 0.10609162 0.09168546]''
'[ 0.13988793  0.07936229 -0.04138152  0.29479112  0.2345007  0.02
208647\n 0.00793127 -0.          0.11500249  0.02543138]''
'[0.19527794 0.13553795 0.00267488 0.17705919 0.03479084 0.03971591
\n 0.0547559 0.02106518 0.05533857 0.03871745]''
'[0.11520371 0.06537877 0.01347788 0.22805724 0.21843231 0.01209633
\n 0.03092495 0.06495369 0.01582734 0.06882094]''
'[ 0.37145699  0.02898865  0.          -0.          0.32307551  0.03
143005\n 0.00144355  0.03751338  0.04360592  0.04845934]''
'[0.23517426 0.08307483 0.00641632 0.17447122 0.12758222 0.00976987
\n 0.0314868 0.0054951 0.09677838 0.04385027]''
'[0.15186134 0.1000623 0.06312305 0.26240319 0.11051922 0.01082034
\n 0.03393842 0.02399719 0.00402959 0.03795552]''
'[ 0.11017916  0.01688681  0.08558525  0.03183052  0.42869848  0.\n-0.          0.03904622  0.01483111  0.12349844]''
'[ 9.40255337e-02 9.95855095e-02 2.58832297e-04 -0.00000000e+00\n3.79828170e-01 1.04639912e-01 1.10396272e-02 -0.00000000e+00\n4.
22342870e-02 6.69747464e-02]''
'[ 0.26965546  0.07988065  0.02287452  0.21064915  0.1325225  0.05
185484\n 0.01400669  0.02490351  0.02847982 -0.00291786]'
```

```
' [0.13782788 0.07830002 0.0587317 0.05027437 0.29946197 0.04983954
\n 0.03984488 0.03958913 0.01976232 0.05865316] '
' [ 0.25974505 0.0699356 0.02407657 0.22564459 0.30859688 -0.03
955727\n 0.04848697 0. 0.05497061 0.02745394] '
' [ 0.06200502 0.06852263 0.12629086 0.15834307 0.33641488 -0.\n
0.11766042 0.08935594 0.0553327 0.03481868] '
' [-0.01088757 0.07300643 0.17797892 0. 0.35717403 0.02
868402\n 0.05792379 0.12185049 0.05415508 0.1067278 ] '
' [0.13513606 0.08243232 0.01268882 0.18798928 0.22489861 0.01811914
\n 0.0235254 0.02833165 0.04212795 0. 0.01342455 0.07879634 0.06157932
' [0.39996332 0.04690359 0.01795939 0.01342455 0.07879634 0.06157932
\n 0.01091482 0.07649877 0.00917257 0.0790986 ] '
' [0.03986424 0.02940483 0.02674348 0.23323632 0.25534202 0.05266985
\n 0.02055267 0.01294608 0.01053157 0.08804751] '
' [3.26815182e-01 2.38763837e-02 1.75290224e-02 1.19161393e-01\n 1.1
9684198e-01 0.00000000e+00 2.16132348e-02 7.60072086e-02\n 4.1769312
5e-02 4.52451696e-05] '
' [ 0.23296441 0.13672125 -0.02379449 0.13690477 0.28595006 0.03
707673\n 0.00776319 0. 0.03072477 0.0465746 ] '
' [0.26782921 0.07054786 0.01629657 0.14863494 0.2455354 0.01575679
\n 0.00963322 0. 0.02878356 0.0054724 ] '
' [ 0.32198492 0.00666568 0.04884657 0. 0.11477949 0.04
686317\n 0.02078401 0.10761295 -0. 0.01799848] '
' [ 0.28983878 0.12967343 0.02164028 0. 0.312312 -0.\n
-0. 0. 0.10811877 0.07609464] '
' [0.03600472 0.13570671 0.14253752 0.11290922 0.33832849 0.02591815
\n 0.02418937 0.06300623 0.01859214 0.0499253 ] '
' [ 0.04930985 0.12370995 0.14408791 0.0118841 0.38827013 0.04
```

```
407355\n 0.04369237  0.06440638  0.0860947  -0.          ]'  
' [ 0.18594225  0.18054065 -0.01035722  0.20897919  0.15037876  0.02  
249703\n 0.          0.00248287  0.06686776 -0.          ]'  
' [ 0.40459122  0.03747488  0.          0.13245572  0.17007618 -0.\n-0.00085546  0.06107533  0.04114752  0.04490943]'  
' [ 0.22187451  0.05964707 -0.          0.0798845  0.38545173 -0.\n0.00895587 -0.00335505  0.07718467  0.08431927]']
```

In []: