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# Harvardx: PH125.3 - (3) Data Science: Probability
# SECTION 1: DISCRETE PROBABILITY
# ASSESSMENTS
# # # ASSESSMENT 1.1: INTRODUCTION TO DISCRETE PROBABILITY
# # EXERCISE 1 - Probability of cyan
# # EXERCISE 2 - Probability of not cyan
# # EXERCISE 3 - Sampling without replacement
# # EXERCISE 4 - Sampling with replacement
# # # ASSESSMENT 1.1: INTRODUCTION TO DISCRETE PROBABILITY - DATACAMP
# # EXERCISE 1 - Probability of cyan - generalized
# Assign a variable `p` as the probability of choosing a cyan ball
from the box
# Print the variable `p` to the console
# # EXERCISE 2 - Probability of not cyan - generalized
# `p` is defined as the probability of choosing a cyan ball from a
box containing: 3 cyan balls, 5 magenta balls, and 7 yellow balls.
# Using variable `p`, calculate the probability of choosing any ball
that is not cyan from the box
# # EXERCISE 3 - Sampling without replacement - generalized
# The variable `p_1` is the probability of choosing a cyan ball from
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the box on the first draw.

- # Assign a variable `p_2` as the probability of not choosing a cyan ball on the second draw without replacement.
- # Calculate the probability that the first draw is cyan and the second draw is not cyan using p_1 and p_2 .
- # # EXERCISE 4 Sampling with replacement generalized
- # The variable 'p_1' is the probability of choosing a cyan ball from the box on the first draw.
- # Assign a variable 'p_2' as the probability of not choosing a cyan ball on the second draw with replacement.
- # Calculate the probability that the first draw is cyan and the second draw is not cyan using p_1 and p_2 .
- # # # ASSESSMENT 1.2: COMBINATIONS & PERMUTATIONS DATACAMP
- # # EXERCISE 1 Independence
- # # EXERCISE 2 Sampling with replacement
- # Assign the variable 'p_yellow' as the probability that a yellow ball is drawn from the box.
- # Using the variable 'p_yellow', calculate the probability of drawing a yellow ball on the sixth draw. Print this value to the console.
- # # EXERCISE 3 Rolling a die
- # Assign the variable 'p_no6' as the probability of not seeing a 6 on

a single roll.

Calculate the probability of not seeing a 6 on six rolls using `p_no6`. Print your result to the console: do not assign it to a variable.

EXERCISE 4 - Probability the Celtics win a game
Assign the variable `p_cavs_win4` as the probability that the Cavs
will win the first four games of the series.

Using the variable `p_cavs_win4`, calculate the probability that the Celtics win at least one game in the first four games of the series.

EXERCISE 5 - Monte Carlo simulation for Celtics winning a game # This line of example code simulates four independent random games where the Celtics either lose or win. Copy this example code to use within the `replicate` function.

The variable 'B' specifies the number of times we want the simulation to run. Let's run the Monte Carlo simulation 10,000 times.

Use the `set.seed` function to make sure your answer matches the expected result after random sampling.

Create an object called `celtic_wins` that replicates two steps for B iterations: (1) generating a random four-game series `simulated_games` using the example code, then (2) determining whether the simulated series contains at least one win for the Celtics. Put these steps on separate lines.

Calculate the frequency out of B iterations that the Celtics won at least one game. Print your answer to the console.

- # # EXERCISE 1 The Cavs and the Warriors
- # Assign a variable 'n' as the number of remaining games.
- # Assign a variable `outcomes` as a vector of possible game outcomes, where 0 indicates a loss and 1 indicates a win for the Cavs. outcomes <- c(0,1)
- # Assign a variable `l` to a list of all possible outcomes in all remaining games. Use the `rep` function on `list(outcomes)` to
- # Create a data frame named 'possibilities' that contains all combinations of possible outcomes for the remaining games.
- # Create a vector named 'results' that indicates whether each row in the data frame 'possibilities' contains enough wins for the Cavs to win the series.
- # Calculate the proportion of 'results' in which the Cavs win the series. Print the outcome to the console.
- # # EXERCISE 2 The Cavs and the Warriors Monte Carlo
 # The variable `B` specifies the number of times we want the
 simulation to run. Let's run the Monte Carlo simulation 10,000
 times.
- # Use the `set.seed` function to make sure your answer matches the expected result after random sampling.
- # Create an object called `results` that replicates for `B` iterations a simulated series and determines whether that series contains at least four wins for the Cavs.
- # Calculate the frequency out of `B` iterations that the Cavs won at least four games in the remainder of the series. Print your answer to the console.
- # # EXERCISE 3 A and B play a series part 1
 # Let's assign the variable 'p' as the vector of probabilities that

Given a value 'p', the probability of winning the series for the underdog team B can be computed with the following function based on a Monte Carlo simulation:



Apply the 'prob_win' function across the vector of probabilities that team A will win to determine the probability that team B will win. Call this object 'Pr'.

Plot the probability 'p' on the x-axis and 'Pr' on the y-axis.

EXERCISE 4 - A and B play a series - part 2

Given a value 'p', the probability of winning the series for the underdog team \$B\$ can be computed with the following function based on a Monte Carlo simulation:



Assign the variable 'N' as the vector of series lengths. Use only odd numbers ranging from 1 to 25 games.

Apply the 'prob_win' function across the vector of series lengths to determine the probability that team B will win. Call this object `Pr`.

Plot the number of games in the series 'N' on the x-axis and 'Pr' on the y-axis.