

Population Mean

$$\mu = \frac{\sum_{i=1}^N x_i}{N}$$

standard deviation

$$\sigma = \sqrt{\frac{\sum (x - \mu)^2}{N}}$$

variance

$$\sigma^2 = \frac{\sum (x - \mu)^2}{N}$$

Sample Mean

$$\bar{x} = \frac{\sum_{i=1}^n x_i}{n}$$

standard deviation

$$s = \sqrt{\frac{\sum (x - \bar{x})^2}{n - 1}}$$

variance

$$s^2 = \frac{\sum (x - \bar{x})^2}{n - 1}$$

p^{th} percentile position: $(p/100)(n+1)$

Probability

Complement of Event A: $P(A^c) = P(\text{not } A) = 1 - P(A)$

For mutually exclusive outcomes: $P(A \text{ or } B) = P(A \cup B) = P(A) + P(B)$

Where not mutually exclusive: $P(A \text{ or } B) = P(A \cup B) = P(A) + P(B) - P(A \cap B)$

For Independent outcomes: $P(A \text{ and } B) = P(A \cap B) = P(A)P(B)$

For dependent outcomes: $P(A \text{ and } B) = P(A) * P(B/A)$

Normal Distribution

$$z = \frac{x - \mu}{\sigma} \quad f(x) = \frac{1}{\sigma\sqrt{2\pi}} e^{-\frac{(x - \mu)^2}{2\sigma^2}}$$

Lognormal Distribution

$$X = \ln Y, \quad Y = e^X \quad f(x) = \frac{1}{\sigma x \sqrt{2\pi}} e^{-\frac{1}{2\sigma^2}(\ln x - \mu)^2} \quad E(Y) = e^{\mu + \frac{1}{2}\sigma^2} \quad V(Y) = e^{2\mu + 2\sigma^2} - e^{2\mu + \sigma^2}$$

Combinations

$$\binom{n}{x} = nCx = \frac{n!}{x!(n-x)!}$$

Permutations

$$nP_x = \frac{n!}{(n-x)!}$$

Binomial – $p(x) = \binom{n}{x} p^x (1-p)^{n-x} \quad \mu = np \quad \sigma^2 = np(1-p)$

Hypergeometric $p(x) = \frac{\binom{r}{x} \binom{N-r}{n-x}}{\binom{N}{n}}$

Poisson $P(X = x) = \frac{e^{-\lambda} \lambda^x}{x!} \quad \mu = \lambda = np \quad \mu = \sigma^2$

Exponential $f(x) = \lambda e^{-\lambda x} \quad F(x) = 1 - e^{-\lambda x}$
 $\mu_x = 1/\lambda = \theta \quad \sigma_x^2 = 1/\lambda^2 = \mu_x^2$