

## Correlation and Regression Formulas (rev 4\_15)

Equation of a line  $y = \hat{\beta}_0 + \hat{\beta}_1 x$

$$\text{where } \hat{\beta}_1 = \frac{\sum_{i=1}^n (x_i - \bar{x})(y_i - \bar{y})}{\sum_{i=1}^n (x_i - \bar{x})^2} \quad \text{or} \quad \hat{\beta}_1 = \frac{\sum_{i=1}^n x_i y_i - n \bar{x} \bar{y}}{\sum_{i=1}^n x_i^2 - n \bar{x}^2} \quad \hat{\beta}_0 = \bar{y} - \hat{\beta}_1 \bar{x}$$

$$r = \frac{\sum_{i=1}^n (x_i - \bar{x})(y_i - \bar{y})}{\sqrt{\sum_{i=1}^n (x_i - \bar{x})^2} \sqrt{\sum_{i=1}^n (y_i - \bar{y})^2}} \quad r = \frac{\sum x_i y_i - \frac{(\sum x_i)(\sum y_i)}{n}}{\sqrt{\left( \sum x_i^2 - \frac{(\sum x_i)^2}{n} \right) \left( \sum y_i^2 - \frac{(\sum y_i)^2}{n} \right)}}$$

### ANOVA

$$SSE = \sum_{i=1}^n (y_i - \hat{y})^2 \text{ with } v=n-2$$

$$SST = \sum_{i=1}^n (y_i - \bar{y})^2 \text{ with } v=n-1$$

$$SSR = SST - SSE \text{ with } v=1$$

$$MS = SS/v \quad F_0 = \frac{MS_{regression}}{MS_{error}} \quad \text{reject if } F_0 > F_{\alpha, 1, n-2}$$

$$r^2 = \frac{SSR}{SST}$$