Untitled

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Table 1: Characteristic of Exponential, Weibull and Gompertz distributions

| | Distribution | | |
|-------------------------------------|---|---|--|
| | Exponential | Weibull | Gompertz |
| Scale Parameter | $\lambda > 0$ | $\lambda > 0$ | $\lambda > 0$ |
| Shape Parameter | | $\gamma > 0$ | $\alpha \in (-\infty, \infty)$ |
| Baseline Hazard function | $h_0(t) = \lambda$ | $h_0(t) = \lambda \gamma t^{\gamma - 1}$ | $h_0(t) = \lambda \exp(\alpha t)$ |
| Cumulative Baseline Hazard Function | $H_0(t) = \lambda t$ | $H_0(t) = \lambda t^{\gamma}$ | $H_0(t) = \frac{\lambda}{\alpha} (e^{\alpha t} - 1)$ |
| Inverse Cumulative Hazard Function | $H^{-1}(t) = \lambda^{-1}t$ | $H^{-1}(t) = (\lambda^{-1}t)^{\frac{1}{\gamma}}$ | $H^{-1}(T) = \frac{1}{\alpha} \log \left(1 + \frac{\alpha}{\lambda}t\right)$ |
| Survival Time T | $T = -\frac{\log(U)}{\lambda e^{X\beta}}$ | $T = \left(-\frac{\log(U)}{\lambda e^{X\beta}}\right)^{\frac{1}{\gamma}}$ | $T = \frac{1}{\alpha} log[1 - \frac{\alpha \log(U)}{\lambda e^{X\beta}}]$ |

Cumulative Distribution Function & $F(t) = 1 - e^{t\lambda e^{X\beta}}$ & $F(t) = 1 - e^{-\lambda t^{\gamma} e^{X\beta}}$ & $F(t) = 1 - e^{-\frac{\lambda}{\alpha}(e^{\alpha} - 1)e^{X\beta}}$