

# Topics

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- Syntax
- Context-Free Grammars and BNF (Backus–Naur Form)
- Derivation and Parse Tree
- Ambiguity
- Extended BNF

# Syntax and Semantics

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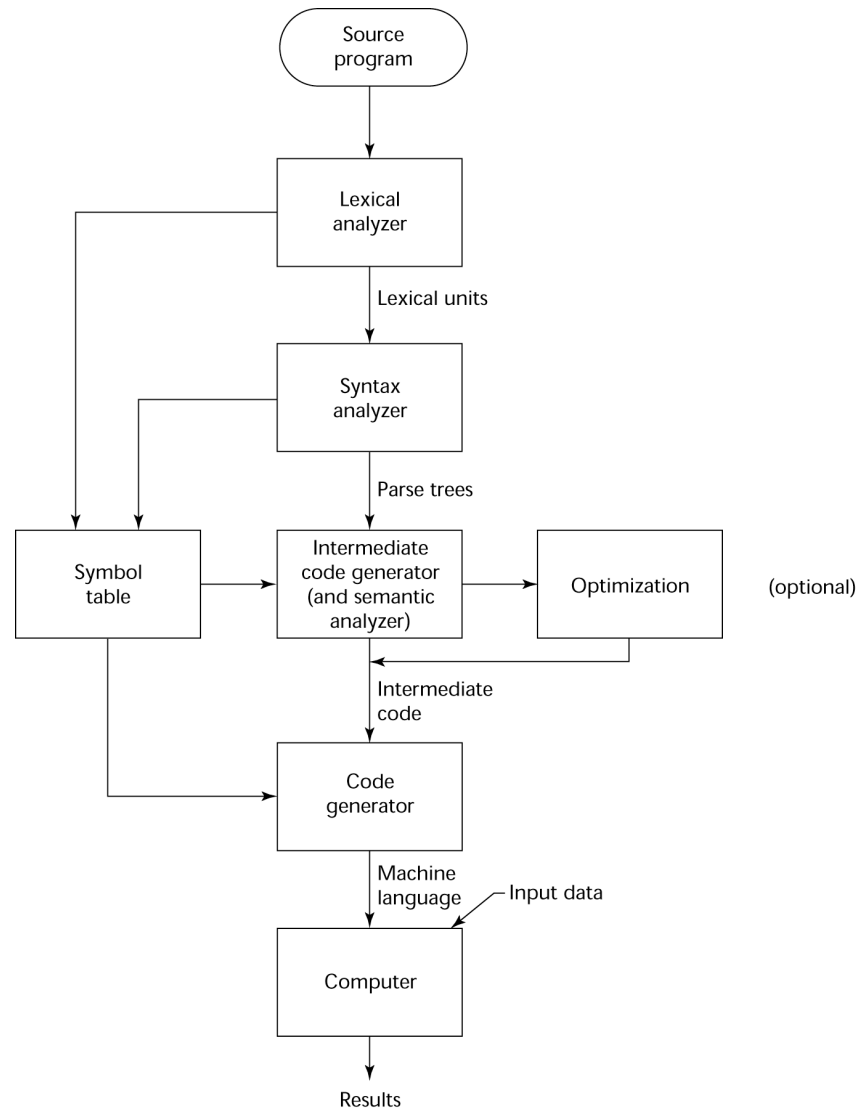
- **Syntax:** the form or structure of the expressions, statements, and program units
- **Semantics:** the meaning of the expressions, statements, and program units
- Syntax and semantics provide a language's definition
  - Users of a language definition
    - Initial evaluators
    - Implementers
    - Programmers (the users of the language)

# The General Problem of Describing Syntax: Terminology

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- A *sentence* is a string of characters over some alphabet
- A *language* is a set of sentences
- A *lexeme* is the lowest level syntactic unit of a language (e.g., \*, sum, begin, 12.3)
- A *token* is a category of lexemes (e.g., identifier)

# The Compilation Process



# Formal Definition of Languages

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- **Recognizers**

- A recognition device reads input strings over the alphabet of the language and decides whether the input strings belong to the language
- Example: syntax analysis part of a compiler
  - Detailed discussion of syntax analysis appears in Chapter 4

- **Generators**

- A device that generates sentences of a language
- One can determine if the syntax of a particular sentence is syntactically correct by comparing it to the structure of the generator

# BNF and Context-Free Grammars

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- Context-Free Grammars
  - Developed by Noam Chomsky (a linguist) in the mid-1950s
  - Language generators, meant to describe the syntax of natural languages
  - Define a class of languages called context-free languages
- Backus-Naur Form (1959)
  - Invented by John Backus to describe the syntax of Algol 58
  - BNF is equivalent to context-free grammars

# BNF Fundamentals

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- In BNF, abstractions are used to represent classes of syntactic structures—they act like syntactic variables (also called *nonterminal symbols*, or just *nonterminals*)
- *Terminals* are lexemes or tokens
- A rule has a left-hand side (LHS), which is a nonterminal, and a right-hand side (RHS), which is a string of terminals and/or nonterminals

# BNF Fundamentals (continued)

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- Nonterminals are often enclosed in angle brackets
  - Examples of BNF rules:  
`<ident_list> → identifier | identifier, <ident_list>`  
`<if_stmt> → if <logic_expr> then <stmt>`
- Grammar: a finite non-empty set of rules
- A *start symbol* is a special element of the nonterminals of a grammar



# BNF Rules

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- An abstraction (or nonterminal symbol) can have more than one RHS

$$\begin{aligned} \langle \text{stmt} \rangle &\rightarrow \langle \text{single\_stmt} \rangle \\ &\quad | \text{begin } \langle \text{stmt\_list} \rangle \text{ end} \end{aligned}$$

- Syntactic lists can be described using recursion

$$\begin{aligned} \langle \text{ident\_list} \rangle &\rightarrow \text{ident} \\ &\quad | \text{ident}, \langle \text{ident\_list} \rangle \end{aligned}$$

# Derivation

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- A derivation is a repeated application of rules, starting with the start symbol and ending with a sentence (all terminal symbols)

# An Example Grammar

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$\langle \text{program} \rangle \rightarrow \langle \text{stmts} \rangle$

$\langle \text{stmts} \rangle \rightarrow \langle \text{stmt} \rangle \mid \langle \text{stmt} \rangle ; \langle \text{stmts} \rangle$

$\langle \text{stmt} \rangle \rightarrow \langle \text{var} \rangle = \langle \text{expr} \rangle$

$\langle \text{var} \rangle \rightarrow a \mid b \mid c \mid d$

$\langle \text{expr} \rangle \rightarrow \langle \text{term} \rangle + \langle \text{term} \rangle \mid \langle \text{term} \rangle - \langle \text{term} \rangle$

$\langle \text{term} \rangle \rightarrow \langle \text{var} \rangle \mid \text{const}$

# An Example Derivation

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`<program> => <stmts> => <stmt>`  
`=> <var> = <expr>`  
`=> a = <expr>`  
`=> a = <term> + <term>`  
`=> a = <var> + <term>`  
`=> a = b + <term>`  
`=> a = b + const`

# Derivation Terminology

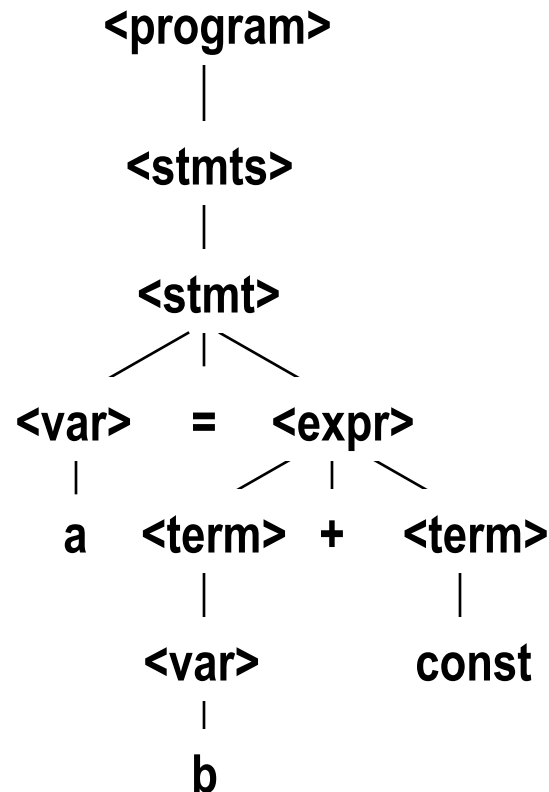
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- Every string of symbols in a derivation is a *sentential form*
- A *sentence* is a sentential form that has only terminal symbols
- A *leftmost derivation* is one in which the leftmost nonterminal in each sentential form is the one that is expanded
- A derivation may be neither leftmost nor rightmost

# Parse Tree

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- A hierarchical representation of a derivation



# Ambiguity in Grammars

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- A grammar is *ambiguous* if and only if it generates a sentential form that has two or more distinct parse trees

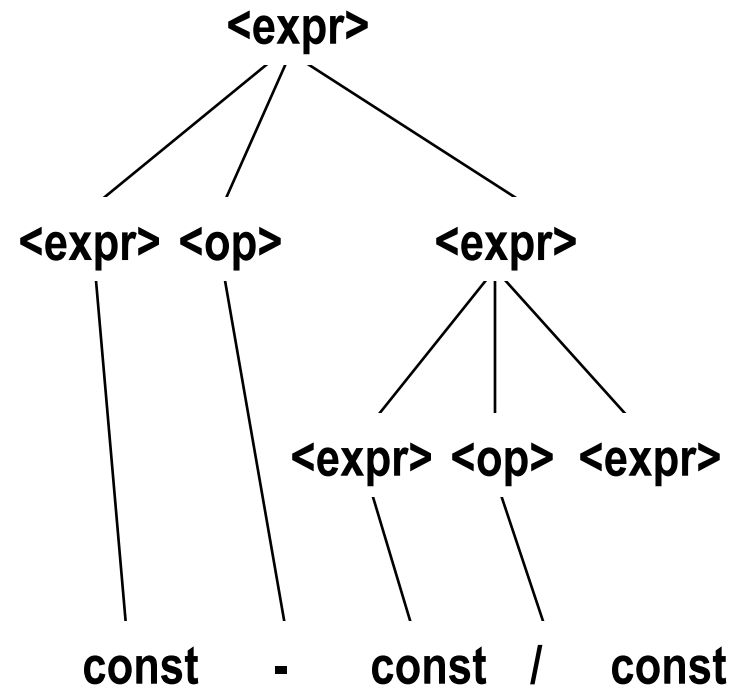
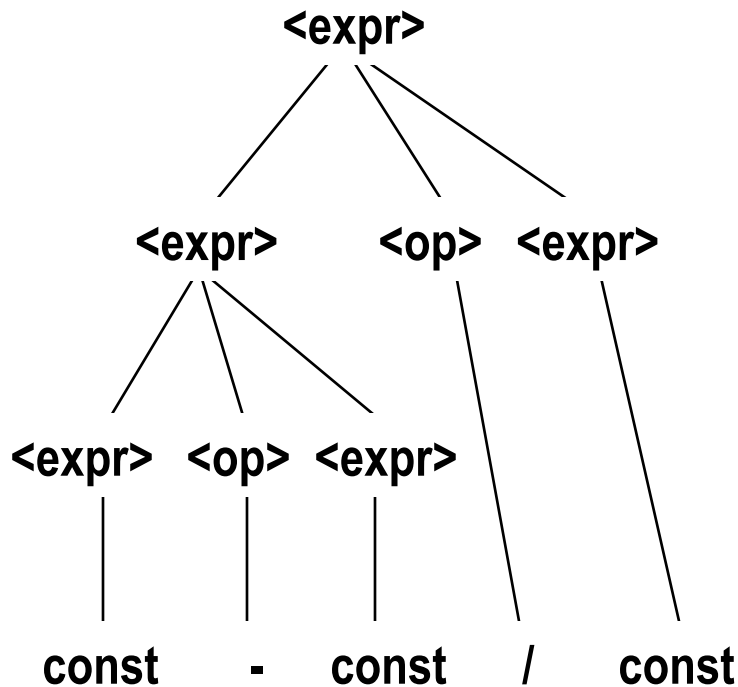
# An Ambiguous Expression Grammar

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$\langle \text{expr} \rangle \rightarrow \langle \text{expr} \rangle \langle \text{op} \rangle \langle \text{expr} \rangle \mid \text{const}$

$\langle \text{op} \rangle \rightarrow / \mid -$

What is  $8-4/2$ ?



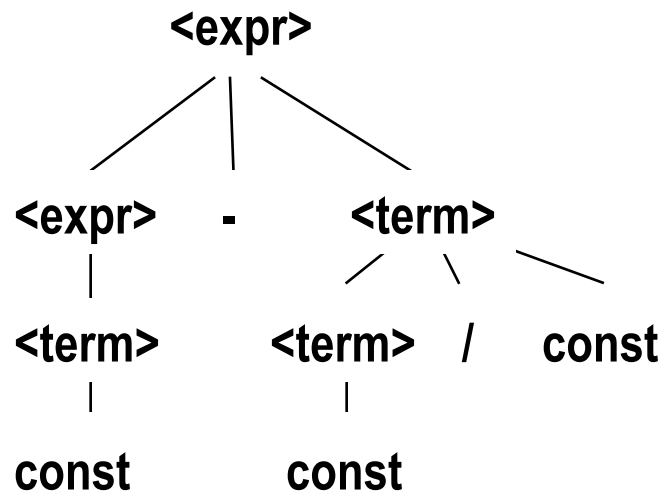


# An Unambiguous Expression Grammar

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- If we use the parse tree to indicate precedence levels of the operators, we cannot have ambiguity

$\langle \text{expr} \rangle \rightarrow \langle \text{expr} \rangle - \langle \text{term} \rangle \mid \langle \text{term} \rangle$   
 $\langle \text{term} \rangle \rightarrow \langle \text{term} \rangle / \text{const} \mid \text{const}$



# Associativity of Operators

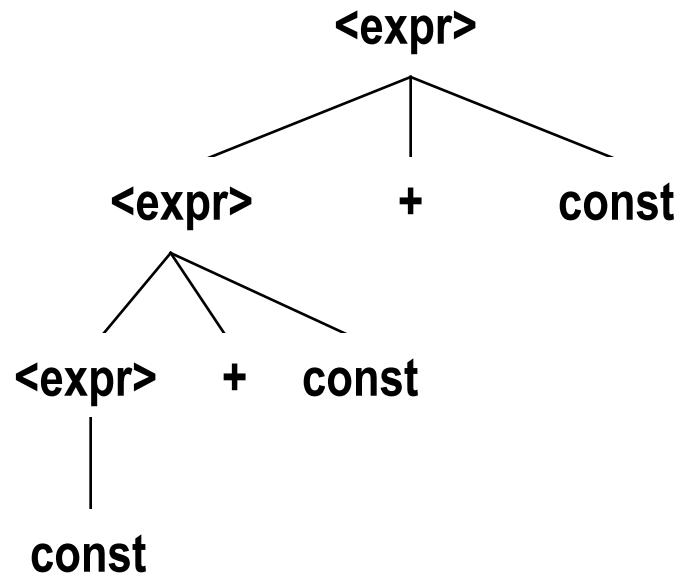
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- Operator associativity can also be indicated by a grammar

$\langle \text{expr} \rangle \rightarrow \langle \text{expr} \rangle + \langle \text{expr} \rangle \mid \text{const}$  (ambiguous)

$\langle \text{expr} \rangle \rightarrow \langle \text{expr} \rangle + \text{const} \mid \text{const}$  (unambiguous)

How to compute  $3+4+5$ ?



# Unambiguous Grammar for Selector

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- **Java if-then-else grammar**

```
<if_stmt> -> if (<logic_expr>) <stmt>  
           | if (<logic_expr>) <stmt> else <stmt>
```

**Ambiguous!**

**if (<logic\_expr>) if (<logic\_expr>) <stmt> else <stmt>**

- **An unambiguous grammar for if-then-else**

```
<stmt> -> <matched> | <unmatched>
```

```
<matched> -> if (<logic_expr>) <matched> else <matched>  
           | a non-if statement
```

```
<unmatched> -> if (<logic_expr>) <stmt>  
              | if (<logic_expr>) <matched> else <unmatched>
```

# Extended BNF

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- Optional parts are placed in brackets [ ]

`<proc_call> -> ident [ (<expr_list>) ]`

- Alternative parts of RHSs are placed inside parentheses and separated via vertical bars

`<term> → <term> (+|-) const`

- Repetitions (0 or more) are placed inside braces { }

`<ident> → letter {letter|digit}`

# BNF and EBNF

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- BNF

$$\begin{aligned}\langle \text{expr} \rangle &\rightarrow \langle \text{expr} \rangle + \langle \text{term} \rangle \\ &| \langle \text{expr} \rangle - \langle \text{term} \rangle \\ &| \langle \text{term} \rangle\end{aligned}$$
$$\begin{aligned}\langle \text{term} \rangle &\rightarrow \langle \text{term} \rangle * \langle \text{factor} \rangle \\ &| \langle \text{term} \rangle / \langle \text{factor} \rangle \\ &| \langle \text{factor} \rangle\end{aligned}$$

- EBNF

$$\begin{aligned}\langle \text{expr} \rangle &\rightarrow \langle \text{term} \rangle \{ (+ \mid -) \langle \text{term} \rangle \} \\ \langle \text{term} \rangle &\rightarrow \langle \text{factor} \rangle \{ (* \mid /) \langle \text{factor} \rangle \}\end{aligned}$$

# Reading Assignment

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- Read Sections 3.1, 3.2 and 3.3